

# Exam Winter Semester 2022

## Student Group

First Name	Surname	Matrikel Nr.

## Table of Contents

<b>Exam Summer Semester 2021</b> .....	2
Additional permitted Aids .....	2
Hits .....	2
Tasks .....	2
Exercise E4 Charging Capacitors (written test, approx. 16 % of a 60-minute written test, WS2022) .....	2
Exercise E6 Impedances at different Frequencies (written test, approx. 18 % of a 60-minute written test, WS2022) .....	3
Exercise E5 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022) .....	4
Exercise E7 Complex Impedance Circuit (written test, approx. 15 % of a 60-minute written test, WS2022) .....	5

# Exam Summer Semester 2021

## Additional permitted Aids

- non-programmable calculator,
- formulary (4 one-sided DIN A4 pages)

## Hits

- The duration of the exam is 120 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.
- Sub-tasks, which are independently solvable are marked with: (independent)
- Sub-tasks, which are hard are marked with: (hard)

## Tasks

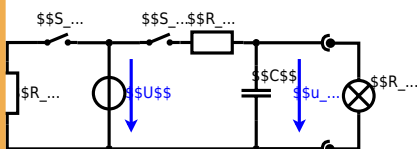
### Exercise E4 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (with the realisation) is in the picture. For  $t < 0$  the switch  $S_1$  is open and the voltage across the capacitor is again  $0 \text{ V}$  at the moment  $t_0 = 0 \text{ s}$  when the switch  $S_1$  is closed. Calculate the voltage  $u_c(t_2)$  across the capacitor at  $t_2 = 1 \text{ ms}$  after closing the switch.

**Resolution**  
 Hint: To solve this, first create an equivalent linear voltage source from  $U$ ,  $R_1$ , and  $R_2$ .

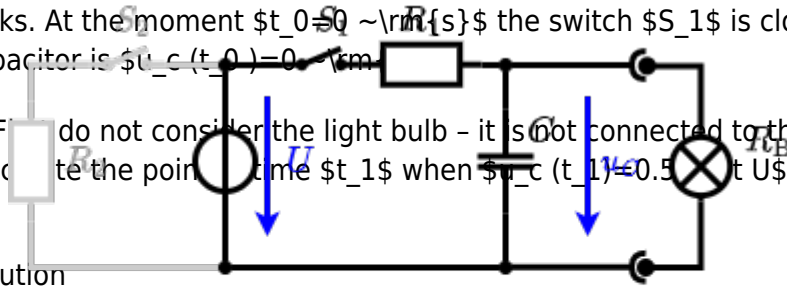
**Solution**  
 The ideal voltage source  $U$  is in series with the resistor  $R_1$  and the resistor  $R_2$  is in parallel with the capacitor. On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting  $R_2$ .



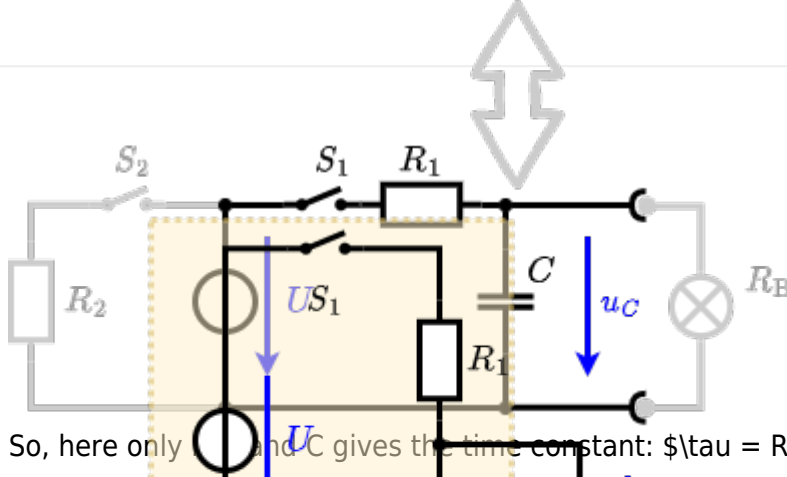
The circuit contains a voltage source  $U = 12 \text{ V}$ , a switch  $S_1$ , a resistor of  $R_1 = 20 \text{ }\Omega$  and a capacitor of  $C = 100 \text{ }\mu\text{F}$ . The switch  $S_2$  to an additional consumer  $R_2$  will be considered to be open for the first

asks. At the moment  $t_0 = 0 \text{ s}$  the switch  $S_1$  is closed, the voltage across the capacitor is  $u_c(t_0) = 0 \text{ V}$ .

1. Do not consider the light bulb - it is not connected to the RC circuit. Calculate the point in time  $t_1$  when  $u_c(t_1) = 0.5 \cdot U$ .



Solution



So, here only  $U$  and  $C$  gives the time constant:  $\tau = R_1 \cdot C$

The following formula describes the time course of  $u_c(t)$  which has to be  $u_c(t_1) = 0.5 \cdot U$ :  

$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to  $(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5)$

An equivalent linear voltage source can be given with  $U$ ,  $R_1$ , and  $R_B$  as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is:  $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$  The internal resistance is given by substituting the ideal voltage source with its resistance ( $R_i = 0 \Omega$ , short-circuit).  

$$R_i = R_1 \parallel R_B = 10 \Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1 \text{ ms} / (10 \Omega \cdot 100 \mu\text{F})})$$

**Exercise E6 Impedances at different Frequencies**  
**(written test, approx. 18 % of a 60-minute written test, WS2022)**

2. A RC circuit with resistor values  $R_1 = 1 \text{ k}\Omega$  and  $R_2 = 10 \text{ k}\Omega$  is shown in the following circuit (of 3S)  $U = 10 \text{ V}$ .  
 Result:  $f_1 = 200 \text{ kHz}$  (high-pass characteristic)  $Z = 50 \sqrt{3} \Omega$  through  $R_1$ .  
 $C_1 = 40 \text{ nF}$  at  $f_1 = 4 \text{ MHz}$ .

Solution

$$R_1 = 1.00 \Omega$$

**Solution**

A series circuit means that the current is constant on every component. Parallel circuit means that the voltage is the same on  $R_3$  and  $C_3$ .

$$\underline{U} = \underline{U}_3 + \underline{U}_C$$

$$\underline{U} = \underline{I} \cdot R_3 + \underline{I} \cdot X_C$$

So it gets clear that perpendicular components can be summed over  $\sqrt{a^2 + b^2}$  instead, since  $R_3$  is  $\sqrt{a^2 + b^2}$ .

Therefore the resulting current of the parallel circuit is given as:

$$I = \sqrt{I_3^2 + I_C^2}$$

$$I = \sqrt{I_3^2 + I_C^2}$$

This can be rearranged to get  $R_3$ :

$$R_3 = \frac{U}{I} - X_C$$

Back to the first formula:

$$I = \frac{U}{\sqrt{R_3^2 + X_C^2}}$$

**Exercise E5 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)**

2. Calculate the phase angle and the effective value of the current through the components. ( $R$  and  $X_L$ ) shall be given.

After analysis, the full dimensional complex impedance has to be extracted and given in phase form  $Z = |Z| \angle \theta$ .

**Solution**

.. Calculation of physical values of the components.

$$Z = R + j\omega L = 10 + j20 \Omega$$

**Solution**

$$I = \frac{U}{Z} = \frac{50 \angle 0^\circ}{10 + j20} = 2.5 \angle -63.4^\circ \text{ A}$$

The current and voltage are in phase since the  $Z$  is purely real resulting in  $\theta = 0^\circ$ .

Therefore, the component  $R$  is in phase with the  $\omega$  and  $X_L$  is  $90^\circ$  ahead.

$$I = \frac{50}{\sqrt{10^2 + 20^2}} = \frac{50}{\sqrt{500}} = 2.24 \text{ A}$$

The phase angle  $\theta$  can be calculated as:

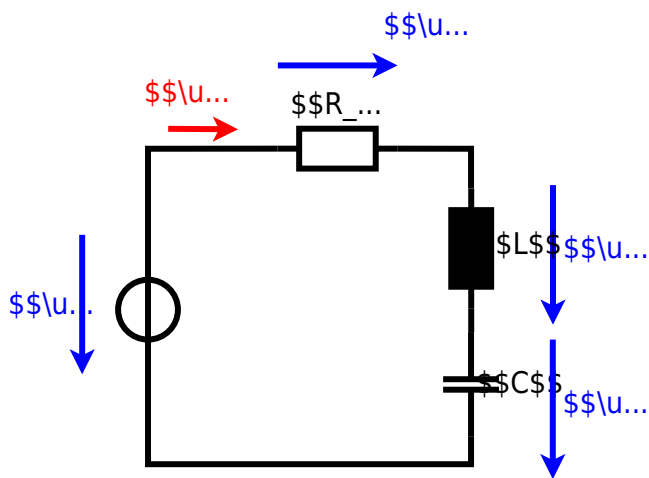
$$\theta = \arctan\left(\frac{\text{Im}(Z)}{\text{Re}(Z)}\right) = \arctan\left(\frac{20}{10}\right) = 63.4^\circ$$

With the complex part comes the complex value  $Z = 10 + j20 \Omega$ .

$$\theta = \arctan\left(\frac{20}{10}\right) = 63.4^\circ$$







From:  
<https://mexle.te.hs-heilbronn.de/> - **MEXLE Wiki**

Permanent link:  
[https://mexle.te.hs-heilbronn.de/electrical\\_engineering\\_and\\_electronics\\_2/ws2022\\_exam?rev=1775224434](https://mexle.te.hs-heilbronn.de/electrical_engineering_and_electronics_2/ws2022_exam?rev=1775224434)

Last update: **2026/04/03 15:53**

