

# Exam Summer Semester 2024

## Student Group

First Name	Surname	Matrikel Nr.

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# Exam Summer Semester 2024

## Additional permitted Aids

- non-programmable calculator,
- formulary (4 one-sided DIN A4 pages)

## Hits

- The duration of the exam is 120 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.

## Tasks

### Exercise E1 Electrostatics I

(written test, approx. 8 % of a 120-minute written test, SS2024)

Given is the arrangement of the charges as in the picture below. The charges of the previous exercise are  $q_1 = 1 \text{ nC}$ . Which value needs  $q_4$  to have to get a resulting force of  $0 \text{ nN}$  on  $q_0$ ?

Path:  $q_0 = -1 \text{ nC}$

- $q_1 = -5 \text{ nC}$

Path:  $E_4 = 917 \text{ V/m}$

$$\vec{F}_{01} = \left( \begin{array}{c} 917 \\ 0 \\ 0 \end{array} \right) \text{ nN}$$

In the beginning the are 5 components, we can not calculate the resulting magnitude of the force.

$$|\vec{F}_{01}| = \sqrt{F_{01,x}^2 + F_{01,y}^2 + F_{01,z}^2} = \sqrt{917^2 + 0^2 + 0^2} = 917 \text{ nN}$$

$$|\vec{F}_{04}| = \sqrt{F_{04,x}^2 + F_{04,y}^2 + F_{04,z}^2} = \sqrt{E_4^2 \cdot |q_0|^2} = E_4 \cdot |q_0|$$

$$|\vec{F}_{01}| = |\vec{F}_{04}| \Rightarrow 917 \text{ nN} = E_4 \cdot |q_0|$$

$$E_4 = \frac{917 \text{ nN}}{|q_0|} = \frac{917 \cdot 10^{-9} \text{ N}}{1 \cdot 10^{-9} \text{ C}} = 917 \text{ V/m}$$

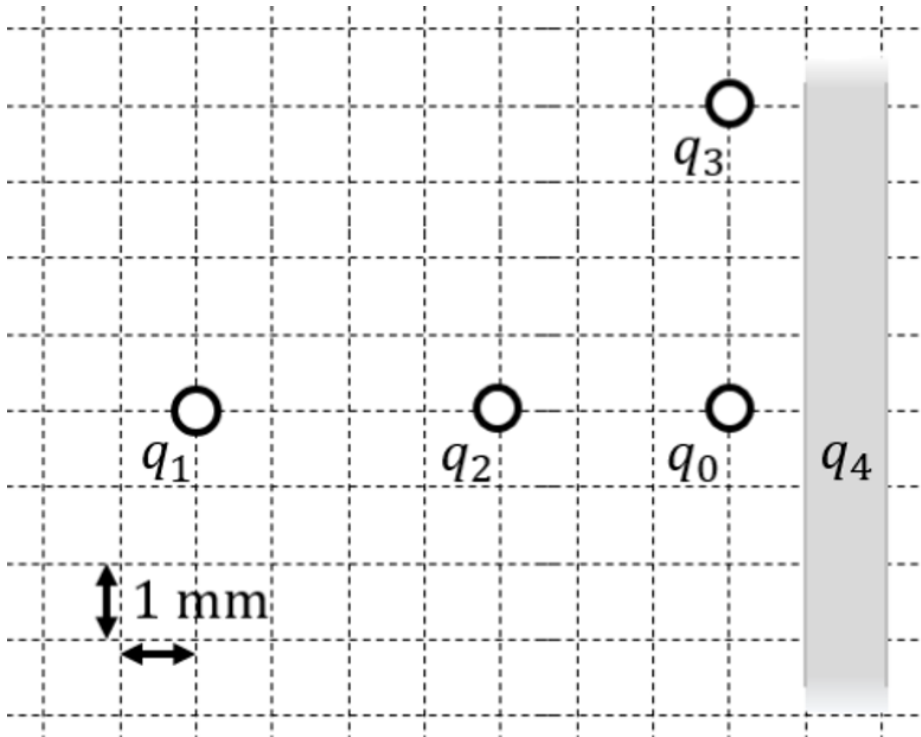
$$|\vec{F}_{01}| = |\vec{F}_{04}| \Rightarrow 917 \text{ nN} = E_4 \cdot |q_0|$$

$$\frac{917 \text{ nN}}{1 \cdot 10^{-9} \text{ C}} = E_4 \Rightarrow E_4 = 917 \text{ V/m}$$

$$917 \text{ nN} = E_4 \cdot 1 \text{ nC} \Rightarrow E_4 = 917 \text{ V/m}$$

$$917 \text{ nN} = E_4 \cdot 1 \text{ nC} \Rightarrow E_4 = 917 \text{ V/m}$$

$$917 \text{ nN} = E_4 \cdot 1 \text{ nC} \Rightarrow E_4 = 917 \text{ V/m}$$



1. Calculate the single forces  $\vec{F}_{01}$ ,  $\vec{F}_{02}$ ,  $\vec{F}_{03}$ , on the charge  $q_0$ !

Path

First, calculate the magnitude of the forces, like  $\vec{F}_{01}$ .

The force  $\vec{F}_{01}$  is purely on the  $x$ -axis and therefore equal to

$$\begin{aligned} F_{01,x} &= \frac{1}{4\pi\epsilon_0} \cdot \frac{q_1 \cdot q_0}{r_{01}^2} \\ &= \frac{1}{4\pi \cdot 8.854 \cdot 10^{-12} \text{ As/Vm}} \cdot \frac{1 \cdot 10^{-9} \text{ C} \cdot 5 \cdot 10^{-9} \text{ C}}{(7 \cdot 10^{-3} \text{ m})^2} \\ &= 917. \dots \cdot 10^{-6} \frac{\text{As}^2 \cdot \text{Vm}}{\text{As} \cdot \text{m}^2} = 917. \dots \cdot 10^{-6} \frac{\text{VA}}{\text{m}} = 917. \dots \cdot 10^{-6} \frac{\text{Ws}}{\text{m}} \\ &= 917. \dots \mu\text{N} \quad \text{(to the right)} \end{aligned}$$

Similarly, we get for  $\vec{F}_{02}$  and  $\vec{F}_{03}$

$$\begin{aligned} \vec{F}_{02} &= F_{02,x} = -1997. \dots \mu\text{N} \quad \text{(to the right)} \\ \vec{F}_{03} &= F_{03,y} = -1123. \dots \mu\text{N} \quad \text{(to the top)} \end{aligned}$$

**Exercise E2 Electrostatics I**  
**(written test, approx. 8 % of a 120-minute written test, SS2024)**

2. What is the magnitude of the force that acts on the charge  $q_0$ ? The values of the point charges are  $q_1 = 1 \text{ nC}$ ,  $q_2 = 1 \text{ nC}$ ,  $q_0 = 1 \text{ nC}$ ,  $q_4 = 1 \text{ nC}$ . Which value needs  $E_4$  to have to get a resulting force of  $0 \text{ N}$  on  $q_0$ ?

Path:  $q_0 = -1 \text{ nC}$

- $q_1 = 5 \text{ nC}$

Path:  $E_4 = 500 \text{ V/m}$

$$\vec{F}_{01} = \left( \begin{array}{c} +197 \\ 0 \\ 0 \end{array} \right) \mu\text{N}$$

In the  $x$ -direction, we cannot calculate the resulting magnitude of the force.

$$\vec{F}_{02} = \left( \begin{array}{c} -197 \\ 0 \\ 0 \end{array} \right) \mu\text{N}$$

The force  $F_{03}$  is in the  $y$ -direction.

$$\vec{F}_{03} = \left( \begin{array}{c} 0 \\ -197 \\ 0 \end{array} \right) \mu\text{N}$$

From this field, the force  $\vec{F}_{04}$  from  $q_4$  on  $q_0$ :

$$|\vec{F}_{01}| = |E_4| \cdot |q_0| \rightarrow E_4 = \frac{|\vec{F}_{01}|}{|q_0|} = \frac{917 \cdot 10^{-6} \text{ N}}{1 \cdot 10^{-9} \text{ C}} = 917 \cdot 10^3 \frac{\text{V}}{\text{m}}$$

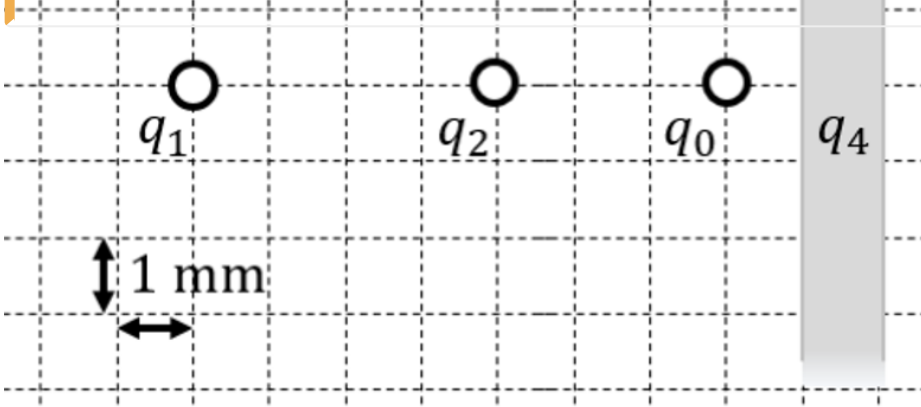
$$= 917 \cdot 10^3 \frac{\text{V}}{\text{m}}$$

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$$= 917 \cdot 10^3 \frac{\text{V}}{\text{m}}$$

$$= 917 \cdot 10^3 \frac{\text{V}}{\text{m}}$$



1. Calculate the single forces  $\vec{F}_{01}$ ,  $\vec{F}_{02}$ ,  $\vec{F}_{03}$ , on the charge  $q_0$ !

Path

First, set up a coordinate system. Here, I choose  $x$  pointing to the right (positive values to the right) and  $y$  pointing upwards (positive values upwards).

Then, calculate the magnitude of the forces, like  $\vec{F}_{01}$  (force on  $q_0$  from  $q_1$ ).

The force  $\vec{F}_{01}$  is purely on the  $x$ -axis and therefore equal to  $F_{01,x}$ .

$$\vec{F}_{01} = F_{01,x} =$$

$$\frac{1}{4\pi\epsilon_0} \cdot \frac{q_1 \cdot q_0}{r_{01}^2} =$$

$$\frac{1}{4\pi \cdot 8.854 \cdot 10^{-12} \text{ As/Vm}} \cdot \frac{1 \cdot 10^{-9} \text{ C} \cdot 5 \cdot 10^{-9} \text{ C}}{(7 \cdot 10^{-3} \text{ m})^2} =$$

$$= 917 \cdot 10^3 \frac{\text{V}}{\text{m}}$$

$917. \cdot 10^{-6} \frac{\text{As}^2 \cdot \text{Vm}}{\text{As} \cdot \text{m}^2} = 917. \cdot 10^{-6} \frac{\text{VAs}}{\text{m}} = 917. \cdot 10^{-6} \frac{\text{Ws}}{\text{m}}$ 
 $\quad \&= +917. \mu\text{N}$

Since both  $q_0$  and  $q_1$  have the same sign for their charges, they are repelling each other. Therefore, The force  $\vec{F}_{01}$  points to the right (positive value).

Similarly, we get for  $\vec{F}_{02}$  and  $\vec{F}_{03}$

$$\vec{F}_{02} = F_{02,x} \quad \&= -1123. \mu\text{N} \quad \vec{F}_{03} = F_{03,y} \quad \&= -1123. \mu\text{N}$$

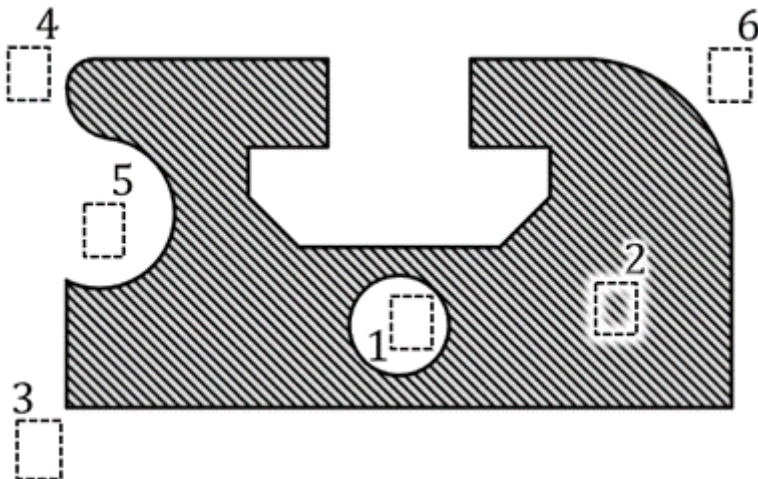
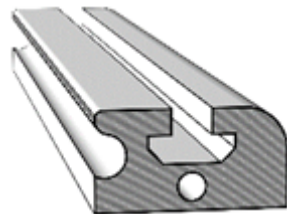
Since  $q_0$  and  $q_2$  have the different sign for their charges, they are attract each other. Therefore, The force  $\vec{F}_{02}$  points to the left (negative value).  
 Since  $q_0$  and  $q_3$  have the different sign for their charges, they are attract each other. Therefore, The force  $\vec{F}_{03}$  points downwards (negative value).

**Exercise E2 Electrostatics II**  
**(written test, approx. 10 % of a 120-minute written test, SS2024)**

You must analyze an aluminum profile for usage in an environment critical for electrostatic discharge.

The figure on the right shows the cross-section of the aluminum element (hatched). During the application, it might get charged up. All areas in white consist of air (= dielectric).

Six designated areas are shown by dashed frames and numbers n, which are partly inside the object.



Arrange the designated areas clearly according to ascending field strengths  $|\vec{E}_n|$  (absolute magnitude)! Indicate also, if designated areas have quantitatively the same field strength.

Result

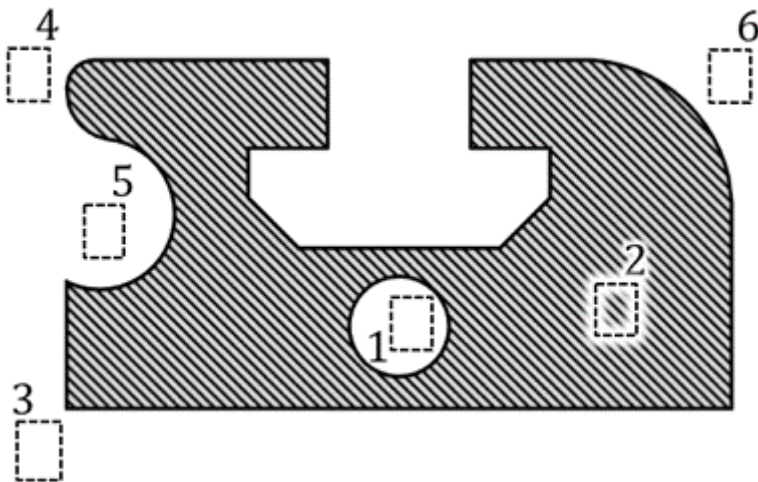
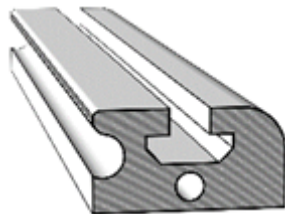
$$|E_1|=|E_2|=0 < |E_5| < |E_6| < |E_4| < |E_3|$$

**Exercise E1 Electrostatics II**  
**(written test, approx. 10 % of a 120-minute written test, SS2024)**

You must analyze an aluminum profile for usage in an environment critical for electrostatic discharge.

The figure on the right shows the cross-section of the aluminum element (hatched). During the application, it might get charged up. All areas in white consist of air (= dielectric).

Six designated areas are shown by dashed frames and numbers n, which are partly inside the object.



Arrange the designated areas clearly according to ascending field strengths  $|\vec{E}_n|$  (absolute magnitude)! Indicate also, if designated areas have quantitatively the same field strength.

Result

$$|E_1|=|E_2|=0 < |E_5| < |E_6| < |E_4| < |E_3|$$

**Exercise E3 Capacitor**

(written test, approx. 12 % of a 120-minute written test, SS2024)

0. Calculate the capacitance of the capacitor described in the problem for the given data. The results are applied.

The contaminant has  $\epsilon_{r,c} > \epsilon_{r,air}$ , while the distance between the plates remains the same. Give a generalized formula

Path

$$C_2 = f(A, d, x, \epsilon_{r,c}, \epsilon_{r,air})$$

$$Q = \frac{U}{\frac{1}{\epsilon_0 \epsilon_{r,c}} \frac{A}{d-x} + \frac{1}{\epsilon_0 \epsilon_{r,air}} \frac{x}{d}}$$

There are two ways now. Either:

$$Q = C \cdot U = 1.1 \cdot 10^{-6} \text{ F} \cdot 3.3 \text{ V} = 3.63 \cdot 10^{-6} \text{ C}$$

Or:

$$Q = D \cdot A = 146 \cdot 10^{-6} \text{ C/m}^2 \cdot 25 \cdot 10^{-4} \text{ m}^2 = 3.65 \cdot 10^{-6} \text{ C}$$

The displacement field is given by:

$$D = \epsilon_0 \epsilon_{r,c} \frac{U}{d-x} = \epsilon_0 \epsilon_{r,air} \frac{U}{x}$$

$$\epsilon_{r,c} \frac{1}{d-x} = \epsilon_{r,air} \frac{1}{x}$$

$$C = \frac{1}{\frac{1}{\epsilon_0 \epsilon_{r,c}} \frac{A}{d-x} + \frac{1}{\epsilon_0 \epsilon_{r,air}} \frac{x}{d}}$$

With

$$C_{air} = \epsilon_0 \epsilon_{r,air} \frac{A}{d}$$

$$\frac{1}{C} = \frac{1}{\epsilon_0 \epsilon_{r,c}} \frac{A}{d-x} + \frac{1}{\epsilon_0 \epsilon_{r,air}} \frac{x}{d}$$

$$C = \frac{1}{\frac{1}{\epsilon_0 \epsilon_{r,c}} \frac{A}{d-x} + \frac{1}{\epsilon_0 \epsilon_{r,air}} \frac{x}{d}}$$

- In the following, such a sensor is given with:
- Plate area:  $A = 25 \text{ mm}^2$
  - Distance between both plates:  $d = 200 \text{ μm}$
  - Air between the plates:  $\epsilon_{r,air} = 1$
  - Supply voltage:  $3.3 \text{ V}$
  - Boundary effects on the end of the layers shall be ignored in the following calculations.

$$\epsilon_0 = 8.854 \cdot 10^{-12} \text{ F/m}$$

1. Calculate the capacity  $C$ .

Path

$$C = \epsilon_0 \epsilon_{r,c} \frac{A}{d-x} = 8.854 \cdot 10^{-12} \text{ F/m} \cdot 1 \cdot \frac{25 \cdot 10^{-6} \text{ m}^2}{200 \cdot 10^{-6} \text{ m}}$$

$$10^{-6} \{ \sim \text{m m} \} \} \end{align*}$$

**Exercise E1 Capacitor**  
**(written test, approx. 12 % of a 120-minute written test, SS2024)**

0. Calculate the capacitance of a capacitor with two parallel plates of length  $l = 25 \text{ cm}$  and width  $b = 10 \text{ cm}$ . The distance between the plates is  $d = 200 \text{ } \mu\text{m}$ . The space between the plates is filled with a dielectric material with a relative permittivity  $\epsilon_r = 3.3$ . The plates are connected to a power source with a voltage  $U = 3.3 \text{ V}$ . The results are rounded to two decimal places.

The contaminant has  $\epsilon_{r,c} > \epsilon_{r,air}$ , while the distance between the plates remains the same. Give a generalized formula for the capacitance  $C$  as a function of  $\epsilon_{r,c}$  and  $\epsilon_{r,air}$ .

Path

$$C = f(A, d, x, \epsilon_{r,c}, \epsilon_{r,air})$$

$$Q = \frac{\epsilon_0 \epsilon_{r,c} A U}{d-x} + \frac{\epsilon_0 \epsilon_{r,air} A U}{x}$$

There are two ways now. Either:  $Q = C U = 1.1 \text{ nF} \cdot 3.3 \text{ V} = 3.63 \text{ nC}$  Or:  $Q = D A = 146 \text{ nC/m} \cdot 25 \text{ cm} = 3.65 \text{ nC}$

The displacement field is given by:  $D = \epsilon_0 \epsilon_{r,c} \frac{U}{d-x} + \epsilon_0 \epsilon_{r,air} \frac{U}{x}$

As a result, the capacitance  $C$  is now  $C = \frac{Q}{U} = \frac{146 \text{ nC/m} \cdot 25 \text{ cm}}{3.3 \text{ V}} = 1.1 \text{ nF}$

Therefore:  $C = \frac{1}{\frac{1}{\epsilon_0 \epsilon_{r,air}} + \frac{1}{\epsilon_0 \epsilon_{r,c}}}$

$$\begin{aligned} C_{air} &= \epsilon_0 \epsilon_{r,air} \frac{A}{d-x} \\ C_{c} &= \epsilon_0 \epsilon_{r,c} \frac{A}{x} \\ C &= \epsilon_0 \epsilon_{r,c} \frac{A}{x} + \epsilon_0 \epsilon_{r,air} \frac{A}{d-x} \end{aligned}$$

- In the following such a sensor is given with:
- Plate area:  $A = 25 \text{ cm}^2$
  - Distance between both plates:  $d = 200 \text{ } \mu\text{m}$
  - Air between the plates:  $\epsilon_{r,air} = 1$
  - Supply voltage:  $U = 3.3 \text{ V}$
  - Boundary effects on the end of the layers shall be ignored in the following calculations.

$$\epsilon_0 = 8.854 \cdot 10^{-12} \text{ F/m}$$

1. Calculate the capacity  $C$ .

Path

$$C = \epsilon_0 \epsilon_r \frac{A}{d} = 8.854 \cdot 10^{-12} \text{ As/Vm} \cdot 1 \cdot \frac{25 \cdot 10^{-6} \text{ m}^2}{200 \cdot 10^{-6} \text{ m}}$$

### Exercise E4 Magnetic Field Lines

(written test, approx. 6 % of a 120-minute written test, SS2024)

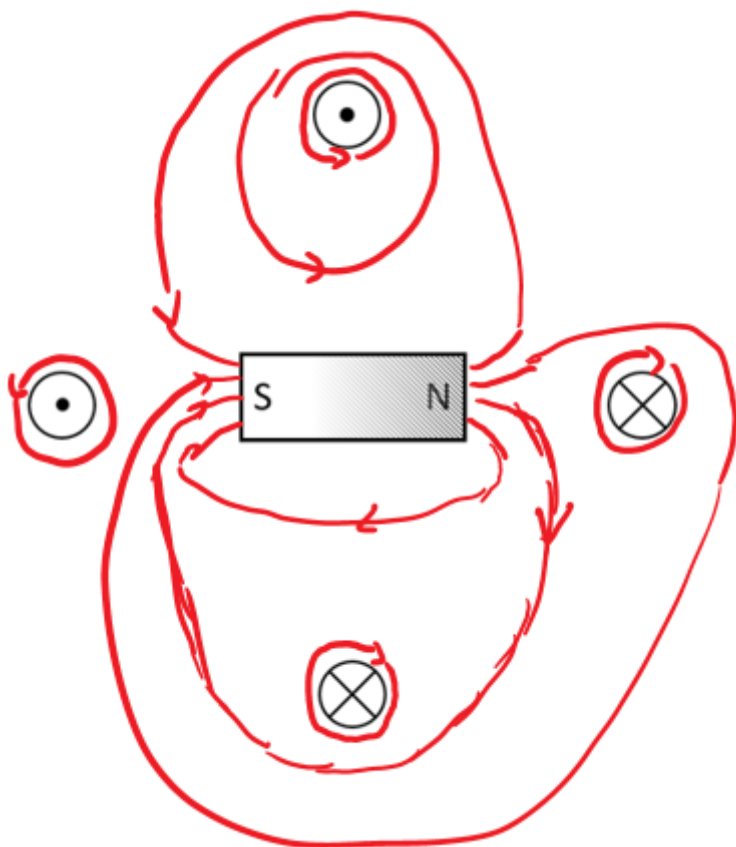
The following setup of a permanent magnet affects the H-field, based on the fundamental definition of the H-field.

- Four conductors are located perpendicular to the plane of the diagram

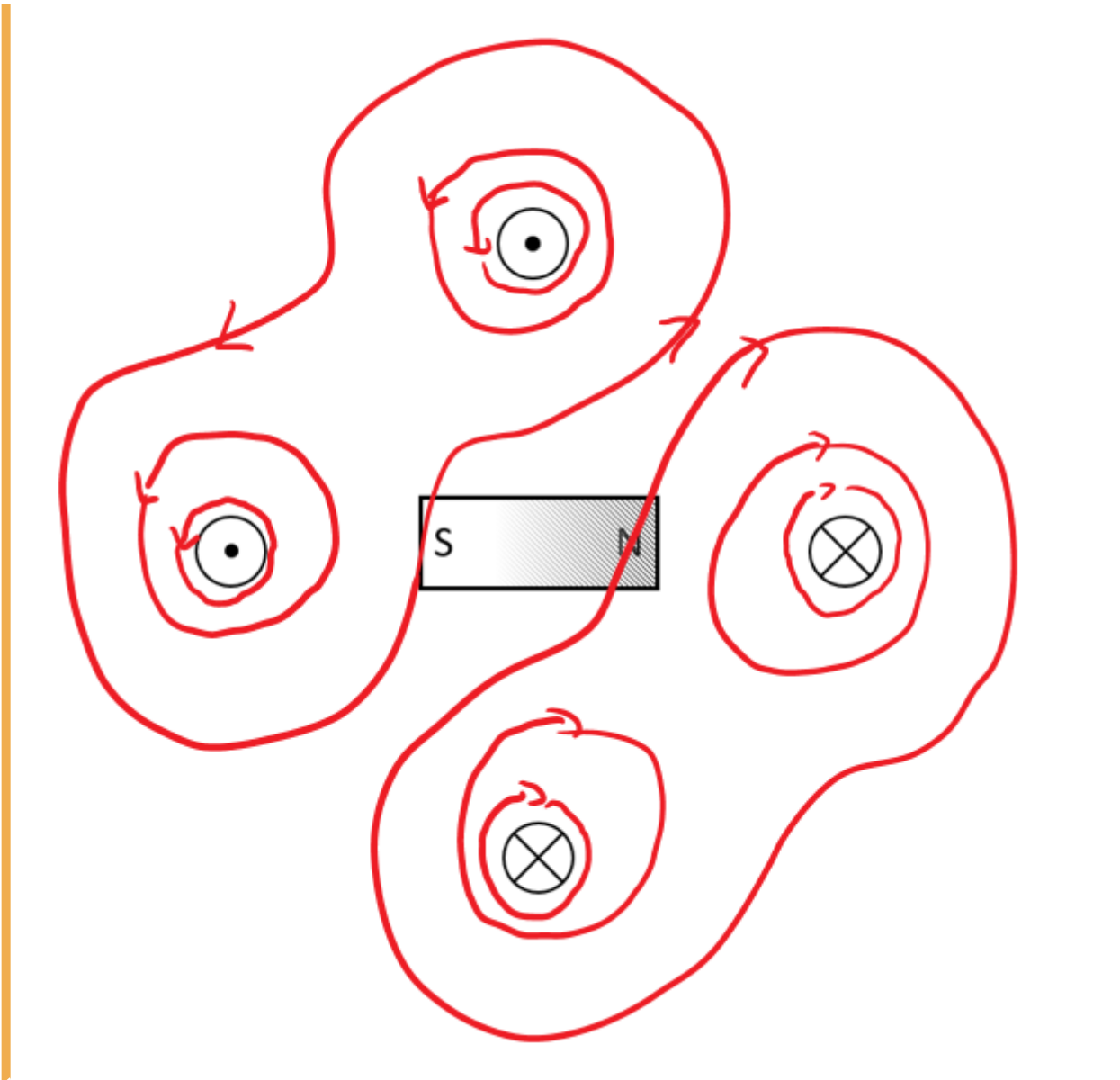
Result: All of them conduct a current with the same magnitude, but not in the same direction.

- A permanent magnet is located in between the conductors.

- The H-field is defined by currents  $\sum I = \int H \{ \text{r m d} \} s$  .
- In the permanent magnet, there are no free currents.
- The bound currents (of the permanent magnet) create also an H field.
- This exits on the north pole and enters the magnet on the south pole (similar to the B-field)\_
- $H = B/\mu$
- The H-field from task 1 gets distracted



st 10 field lines of the H-field and density for the shown



**Exercise E1 Magnetic Field Lines**  
**(written test, approx. 6 % of a 120-minute written test, SS2024)**

The following setup is given. A permanent magnet affects the H-field, based on the fundamental definition of the H-field.

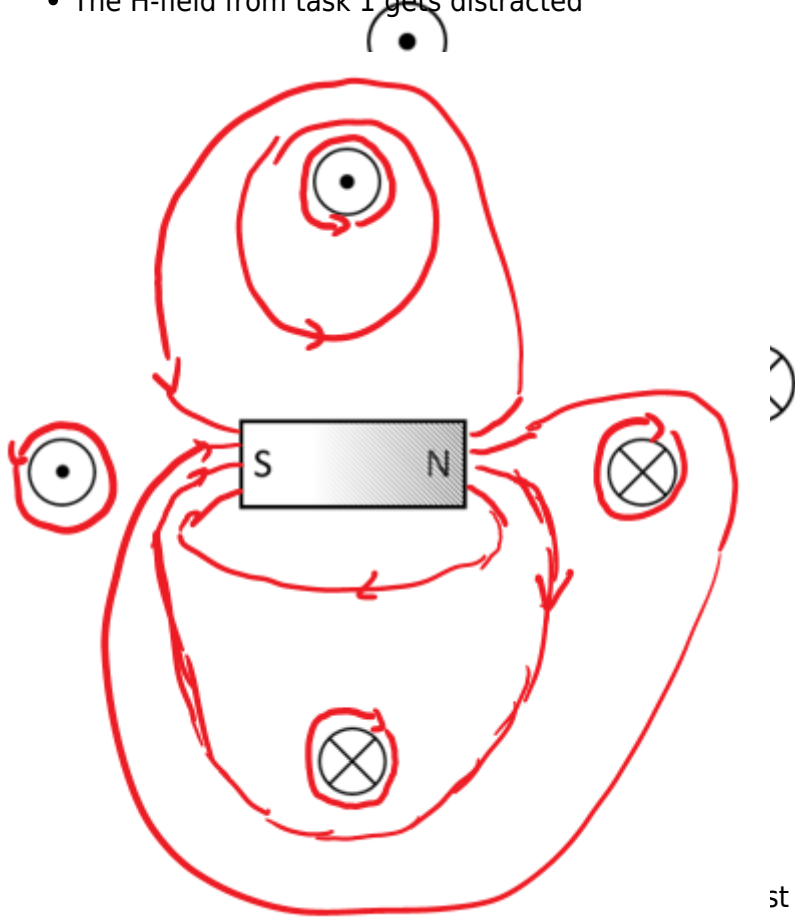
- Four conductors are located perpendicular to the plane of the diagram

Result: All of them conduct a current with the same magnitude, but not in the same direction.

- A permanent magnet is located in between the conductors.

- The H-field is defined by currents  $\sum I = \int \mathbf{H} \cdot d\mathbf{s}$ .
- In the permanent magnet, there are no free currents.
- The bound currents (of the permanent magnet) create also an H field.
- This exits on the north pole and enters the magnet on the south pole (similar to the B-field)

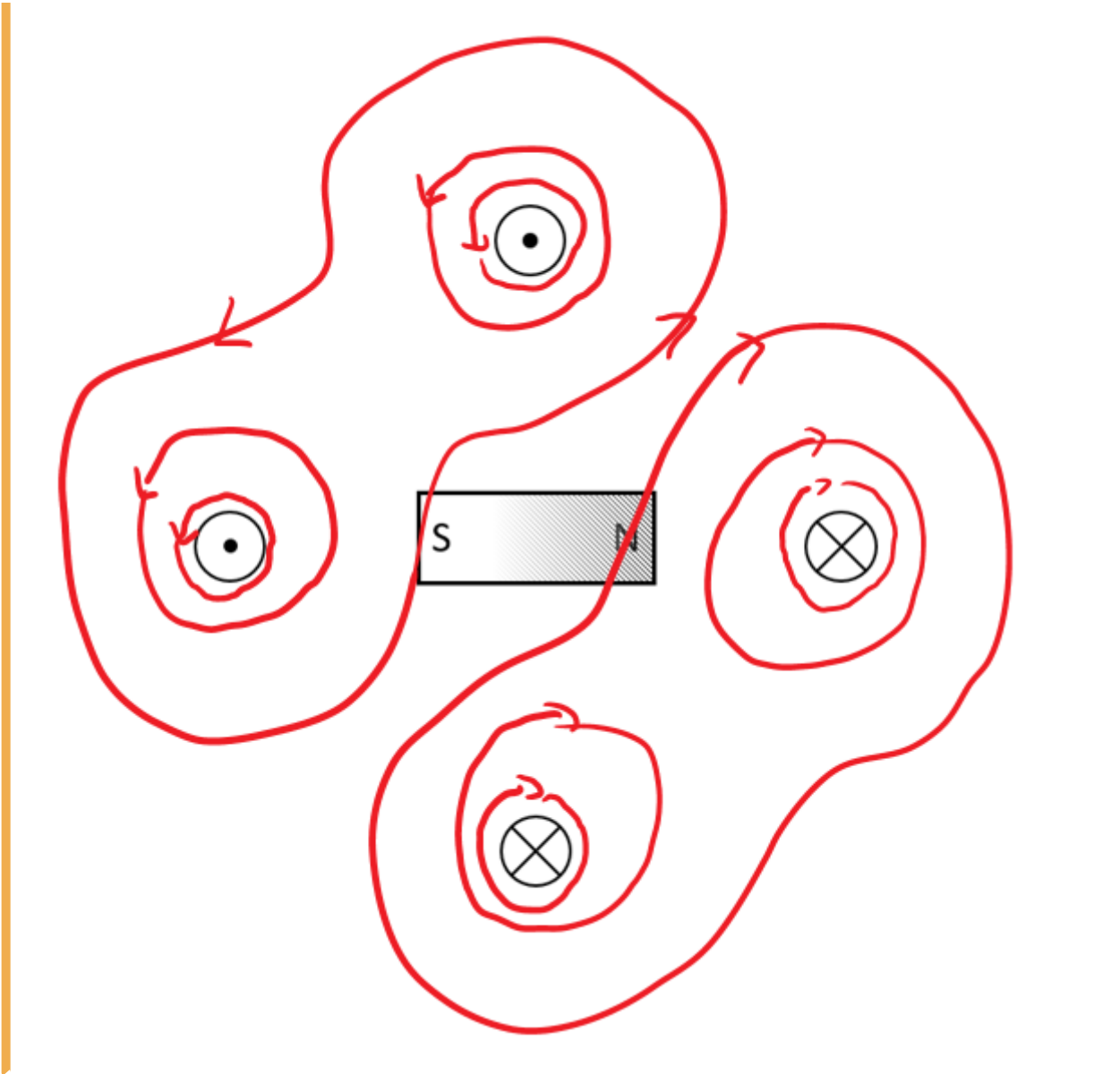
- $H = B/\mu$
- The H-field from task 1 gets distracted



... D  
qua  
area.

st 10 field lines of the H-field  
and density for the shown

Result



**Exercise E5 Fields of an coax Cable**  
 (written test, approx. 12 % of a 120-minute written test, SS2024)

2. For the graph of the magnitude of the magnetic field  $B$  with radial distance  $r$  of the diagram 4.06 shows the result for a coax cable with the origin  $r=0$  in the center of the inner conductor. The diagram is labeled as follows:

path • Inner conductor:  $+3.3 \text{ mA}$ ,  $+10 \text{ nC}$  (current into the plane of the path diagram)

- for  $(0.1 \text{ mm} | 0)$ :  $B_{\text{in}} = 3.28 \dots \text{ A/m}$
- Outer conductor:  $-3.3 \text{ mA}$ ,  $0 \text{ nC}$  (current out of the plane of diagram)
- for  $(0.55 \text{ mm} | 0)$ :  $B_{\text{out}} = 0.985 \dots \text{ A/m}$

The magnitude of the electric displacement field  $D$  can be calculated by:  $\int D \cdot dA = Q$ .

Here, for any position radial to the center, the surrounding area is the surface of a cylindrical shape (here for simplicity without the round endings).

- For the charges  $Q$  within the surface of the conductor there is no  $D$  field within the conductor. within a circle with the radius  $r$ .

$\propto x)$  is proportional to the area within this radius. Therefore, The formula  $H = \frac{I}{2 \pi \cdot r}$  gets  $H(x) = \frac{I}{2 \pi \cdot x} \cdot \pi \cdot x^2$ .  
 So, we get for  $D_{\text{in}}$  at  $(0.1 \text{ mm} | 0)$ ,  $D_{\text{out}}$  at  $(0.55 \text{ mm} | 0)$  and  $D_{\text{out}}$  at  $(0.55 \text{ mm} | 0)$  within the outer conductor one also gets a linear proportionality with a similar approach.

$$D_{\text{in}} = \frac{Q}{2 \pi \cdot r_{\text{in}} \cdot l} = \frac{10 \cdot 10^{-9} \text{ C}}{2 \pi \cdot \{0.1 \cdot 10^{-3} \text{ m}\} \cdot 0.5 \text{ m}}$$

$$D_{\text{out}} = \frac{Q}{2 \pi \cdot r_{\text{out}} \cdot l} = \frac{10 \cdot 10^{-9} \text{ C}}{2 \pi \cdot \{0.55 \cdot 10^{-3} \text{ m}\} \cdot 0.5 \text{ m}}$$

Hint: For the direction, one has to consider the sign of the enclosed charge. By this, we see that the  $D$ -field is positive.  
 But here, again only the magnitude was questioned!

.. What is the magnitude of the magnetic field strength  $H$  at  $(0.1 \text{ mm} | 0)$  and  $(0.55 \text{ mm} | 0)$ ?

Path

The magnitude of the magnetic field strength  $H$  can be calculated by:  $H = \frac{I}{2 \pi \cdot r}$   
 So, we get for  $H_{\text{in}}$  at  $(0.1 \text{ mm} | 0)$ , and  $H_{\text{out}}$  at  $(0.55 \text{ mm} | 0)$ :

$$H_{\text{in}} = \frac{I}{2 \pi \cdot r_{\text{in}}} = \frac{+3.3 \text{ A}}{2 \pi \cdot \{0.1 \cdot 10^{-3} \text{ m}\}}$$

$$H_{\text{out}} = \frac{I}{2 \pi \cdot r_{\text{out}}} = \frac{+3.3 \text{ A}}{2 \pi \cdot \{0.55 \cdot 10^{-3} \text{ m}\}}$$

Hint: For the direction, one has to consider the right-hand rule. By this, we see that the  $H$ -field on the right side points downwards.  
 Therefore, the sign of the  $H$ -field is negative.  
 But here, only the magnitude was questioned!

**Exercise E6 Fields of an coax Cable**  
**(written test, approx. 12 % of a 120-minute written test, SS2024)**

2. With the graph of the magnitude of the electric field strength  $E$  in  $\text{V/m}$  at  $r = 0.6 \text{ mm}$  and  $r = 0.6 \text{ mm}$  (see  $r = 0$  mm) is shown. The origin  $(0,0)$  is in the center of the cable. Describe the dimensions and label the diagram.

Path

- Inner conductor:  $+3.3 \text{ mA}$ ,  $+10 \text{ nC}$  (current into the plane of the path diagram)
- Outer conductor:  $-3.3 \text{ mA}$ ,  $0 \text{ nC}$  (current out of the plane of diagram)
- for  $(0.1 \text{ mm} | 0)$ :  $E_{\text{I}} = 528 \text{ V/m}$
- for  $(0.55 \text{ mm} | 0)$ :  $E_{\text{O}} = 6.985 \text{ V/m}$

The magnitude of the electric displacement field  $D$  can be calculated by:  $\int D \cdot dA = Q_{\text{enc}}$ .

Here, in any position  $r$  (at the center), the surrounding area is the surface of a cylindrical shape (here for simplicity without the round endings).

Since the charge is spread on the surface of the conductor, it is not much different from a point charge within a circle with the radius  $r$ .

This is proportional to the area within this radius. Therefore, the formula  $H = \frac{I}{2\pi r}$  is used.

So, we get for  $H_{\text{I}}$  at  $r = 0.1 \text{ mm}$ , and  $H_{\text{O}}$  at  $r = 0.55 \text{ mm}$ .

For  $r$  within the outer conductor one also gets a linear proportionality with a similar approach:  $H = \frac{I_{\text{enc}}}{2\pi r}$ .

Hint: For the direction, one has to consider the sign of the enclosed charge. By this, we see that the  $D$ -field is positive.

But here, again only the magnitude was questioned!

.. What is the magnitude of the magnetic field strength  $H$  at  $(0.1 \text{ mm} | 0)$  and  $(0.55 \text{ mm} | 0)$ ?

Path

The magnitude of the magnetic field strength  $H$  can be calculated by:  $H = \frac{I}{2\pi r}$

So, we get for  $H_{\text{I}}$  at  $(0.1 \text{ mm} | 0)$ , and  $H_{\text{O}}$  at  $(0.55 \text{ mm} | 0)$

$\sim \text{mm} \mid 0$ ):

$$\begin{aligned} H_{\text{rmi}} &= \frac{I}{2 \pi \cdot r_{\text{rmi}}} \quad \&= \frac{+3.3 \text{ A}}{2 \pi \cdot \{0.1 \cdot 10^{-3} \sim \text{m}\}} \\ H_{\text{ro}} &= \frac{I}{2 \pi \cdot r_{\text{ro}}} \quad \&= \frac{+3.3 \text{ A}}{2 \pi \cdot \{0.55 \cdot 10^{-3} \sim \text{m}\}} \end{aligned}$$

Hint: For the direction, one has to consider the right-hand rule. By this, we see that the  $H$ -field on the right side points downwards. Therefore, the sign of the  $H$ -field is negative. But here, only the magnitude was questioned!

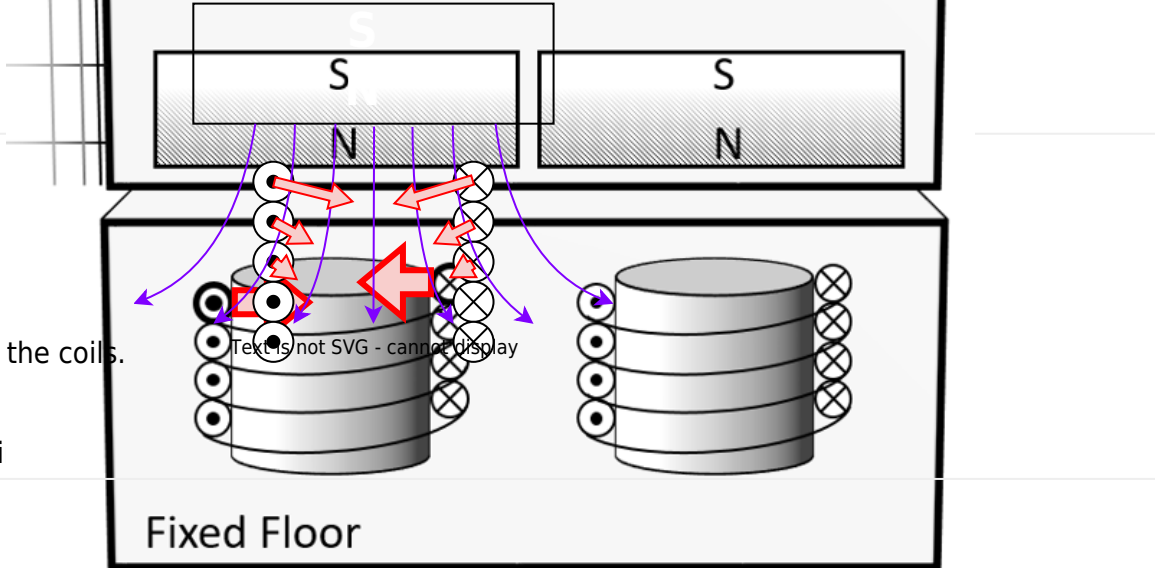
**Exercise E7 Lorentz Force**  
**(written test, approx. 8 % of a 120-minute written test, SS2024)**

2. Do not write the system for the left side, that is, do not write the current  $I$  in the image. To do this, the resulting force vector is plotted in the image for all sides of the shuttle (see image).

Result

Path

Since the result  $F_{\text{Dreh}} = 0$  has to be perpendicular to  $B$ -field and conductor, the force has to point to the left or the right.  
 For a homogeneous  $B$ -field ("constant magnetic field of the shuttle"), the Lorentz forces cancel each other out.  
 The Lorentz force can only have a lifting effect in an inhomogeneous field. In this case, the sum of the forces results in a repulsing force, see image. Besides boundary effects, The field gets also inhomogeneous, by the additional field of



- current  $I = 1.6 \text{ A}$
- magnetic field of the shuttle is homogeneous with  $B = 0.5 \text{ T}$

1. Calculate the magnitude of the resulting force on one coil!

Path

The Lorentz force on a conductor the length  $l$  and the current  $I$  in a  $B$ -field is

$$|\vec{F}_L| = I \cdot l \cdot B \cdot \cos(\angle \vec{B}, \vec{l})$$

$$= I \cdot (N \cdot 2\pi r) \cdot B \cdot \cos(\angle \vec{B}, \vec{l}) \approx 1.6 \text{ A} \cdot (500 \cdot 2\pi \cdot 40 \cdot 10^{-3} \text{ m}) \cdot 0.5 \text{ T} \cdot \cos 90^\circ$$

**Exercise E8 Lorentz Force**  
**(written test, approx. 8 % of a 120-minute written test, SS2024)**

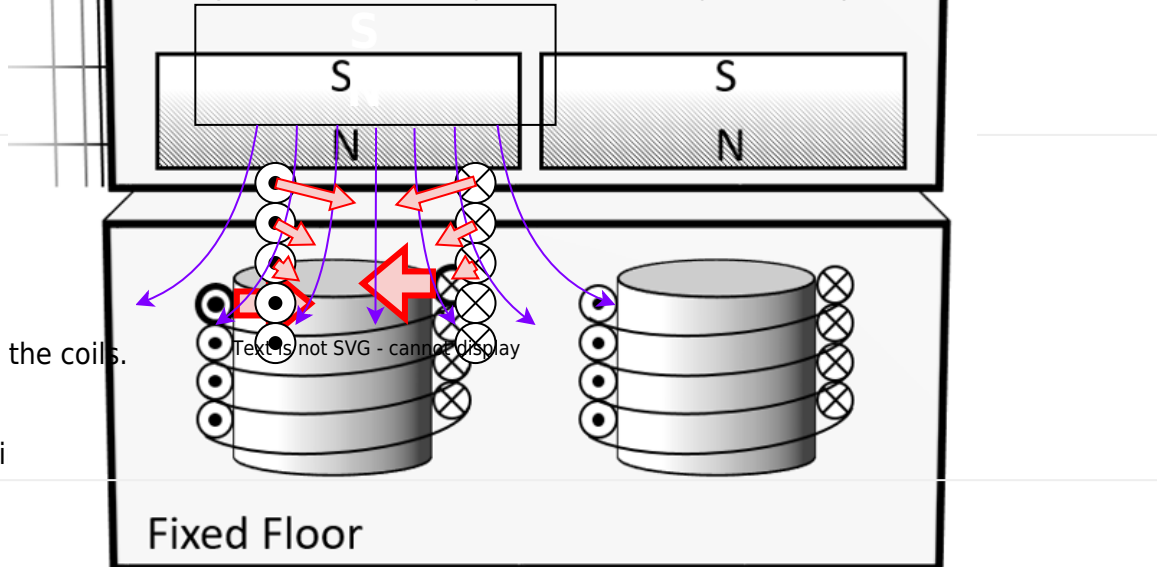
2. Do not calculate the force on the left coil, but on the right coil. The field of the left coil is  $B_{left}$  and the field of the right coil is  $B_{right}$ . The resulting force vector is to be drawn in the image for all sides of the coil (see image).

Result

Path

Since the direction of the current  $I$  has to be perpendicular to  $B$ -field and conductor, the force has to point to the left or the right.  
 From a homogeneous  $B$ -field ("constant magnetic field of the shuttle"), the Lorentz forces cancel each other out.

The Lorentz force can only have a lifting effect in an inhomogeneous field.  
 In this case, the sum of the forces results in a repulsing force, see image.  
 Beside boundary effects, The field gets also inhomogeneous, by the additional field of



- current  $I = 1.6 \text{ A}$
- magnetic field of the shuttle of is homogeneous with  $B = 0.5 \text{ T}$

1. Calculate the magnitude of the resulting force on one coil!

Path

The Lorentz force on a conductor the length  $l$  and the current  $I$  in a  $B$ -field is

$$|\vec{F}_L| = I \cdot l \cdot B \cdot \cos(\angle \vec{B}, \vec{l})$$

$$= I \cdot (N \cdot 2\pi r) \cdot B \cdot \cos(\angle \vec{B}, \vec{l}) = 1.6 \text{ A} \cdot (500 \cdot 2\pi \cdot 40 \cdot 10^{-3} \text{ m}) \cdot 0.5 \text{ T} \cdot \cos 90^\circ$$

### Exercise E9 Magnetic Potential

(written test, approx. 8 % of a 120-minute written test, SS2024)

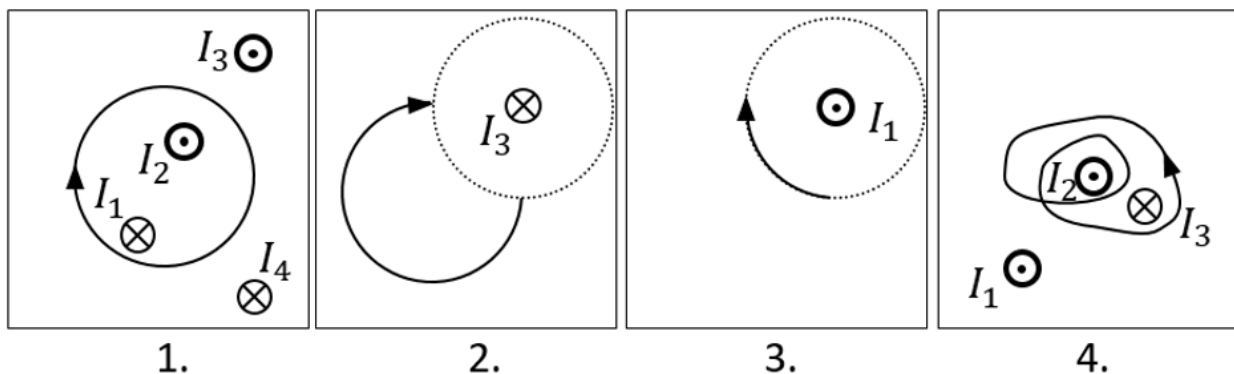
Calculate the magnetic potential difference  $V_{\text{m}}$  for the following paths as shown by the solid lines.

Dotted lines are only for there for symmetry aspects!

The wires conduct the following currents:

- $|I_1| = 2 \text{ A}$
- $|I_2| = 5 \text{ A}$
- $|I_3| = 11 \text{ A}$
- $|I_4| = 7 \text{ A}$

Pay attention to the signs of the currents (given by the diagrams) and of the results!



Result

Based on the right-hand rule and the part of a full revolution the following results:

1. Task:  $+I_1 - I_2 = -3 \text{ A}$
2. Task:  $+\frac{1}{4} I_3 = 11/4 \text{ A}$  (it does not matter which way the path goes from the startpoint to the endpoint, as long as it has the same direction and number of revolutions)

3. Task:  $-\frac{1}{4} I_1 = -0.5 \text{ ~\rm A}$

4. Task:  $+2 I_2 - 1 I_3 = -1 \text{ ~\rm A}$

### Exercise E10 Magnetic Potential

(written test, approx. 8 % of a 120-minute written test, SS2024)

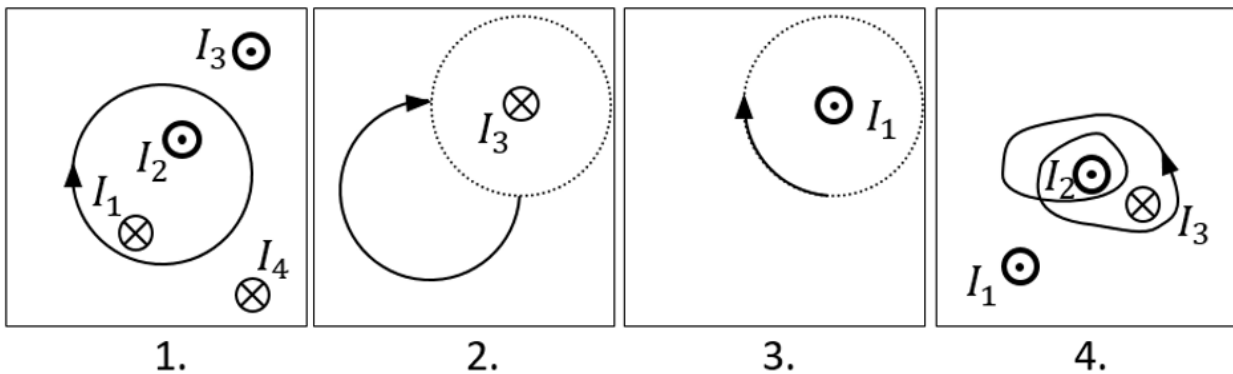
Calculate the magnetic potential difference  $V_{\text{m}}$  for the following paths as shown by the solid lines.

Dotted lines are only for there for symmetry aspects!

The wires conduct the following currents:

- $|I_1| = 2 \text{ ~\rm A}$
- $|I_2| = 5 \text{ ~\rm A}$
- $|I_3| = 11 \text{ ~\rm A}$
- $|I_4| = 7 \text{ ~\rm A}$

Pay attention to the signs of the currents (given by the diagrams) and of the results!



Result

Based on the right-hand rule and the part of a full revolution the following results:

1. Task:  $+I_1 - I_2 = -3 \text{ ~\rm A}$

2. Task:  $+\frac{1}{4} I_3 = 11/4 \text{ ~\rm A}$  (it does not matter which way the path goes from the startpoint to the endpoint, as long as it has the same direction and number of revolutions)

3. Task:  $-\frac{1}{4} I_1 = -0.5 \text{ ~\rm A}$

4. Task:  $+2 \cdot I_2 - 1 \cdot I_3 = -1 \text{ A}$

**Exercise E11 Self-Induction**  
 (written test, approx. 8 % of a 120-minute written test, SS2024)

2. Determine the inductance of a solenoid with a length of  $0.2 \text{ m}$  and a diameter of  $2 \text{ cm}$  if it has  $500$  turns. The current through the coil changes linearly from  $0 \text{ A}$  to  $3 \text{ A}$  in  $0.02 \text{ ms}$ . The arrangement is located in air ( $\mu_r = 1$ ).  
 Path

$\mu_0 = 4\pi \cdot 10^{-7} \text{ Vs/Am}$
$U_{\text{ind}} = 1.32 \text{ mV}$
.. Calculate the (self-)inductance of the coil. For the linear change of the current the formula of the induced voltage can also be linearized: $u_{\text{ind}} = -L \cdot \frac{di}{dt} \implies L = -\frac{u_{\text{ind}} \cdot dt}{di} = -\frac{1.32 \cdot 10^{-3} \text{ V} \cdot 0.02 \cdot 10^{-3} \text{ s}}{3 \text{ A}} = 8.8 \cdot 10^{-7} \text{ H}$
The formula for the induction of a long coil is: $L = \mu_0 \mu_r \cdot N^2 \cdot \frac{A}{l} = 4\pi \cdot 10^{-7} \text{ Vs/Am} \cdot (500)^2 \cdot \frac{\pi \cdot (0.02 \text{ m})^2}{2 \cdot 0.2 \text{ m}} = 1.57 \cdot 10^{-4} \text{ H}$

**Exercise E12 Self-Induction**  
 (written test, approx. 8 % of a 120-minute written test, SS2024)

2. Determine the inductance of a solenoid with a length of  $0.2 \text{ m}$  and a diameter of  $2 \text{ cm}$  if it has  $500$  turns. The current through the coil changes linearly from  $0 \text{ A}$  to  $3 \text{ A}$  in  $0.02 \text{ ms}$ . The arrangement is located in air ( $\mu_r = 1$ ).  
 Path

$\mu_0 = 4\pi \cdot 10^{-7} \text{ Vs/Am}$
$U_{\text{ind}} = 1.32 \text{ mV}$
.. Calculate the (self-)inductance of the coil. For the linear change of the current the formula of the induced voltage can also be linearized: $u_{\text{ind}} = -L \cdot \frac{di}{dt} \implies L = -\frac{u_{\text{ind}} \cdot dt}{di} = -\frac{1.32 \cdot 10^{-3} \text{ V} \cdot 0.02 \cdot 10^{-3} \text{ s}}{3 \text{ A}} = 8.8 \cdot 10^{-7} \text{ H}$
The formula for the induction of a long coil is: $L = \mu_0 \mu_r \cdot N^2 \cdot \frac{A}{l} = 4\pi \cdot 10^{-7} \text{ Vs/Am} \cdot (500)^2 \cdot \frac{\pi \cdot (0.02 \text{ m})^2}{2 \cdot 0.2 \text{ m}} = 1.57 \cdot 10^{-4} \text{ H}$

The formula for the induction of a long coil is: 
$$L = \mu_0 \mu_r N^2 \frac{A}{l} \approx 4\pi \cdot 10^{-7} \frac{\text{Vs/Am}}{\text{m}} \cdot (500)^2 \frac{\text{m}^2}{2 \cdot 10^{-2} \text{ m}}$$

**Exercise E13 Magnetic Circuit**

(written test, approx. 9 % of a 120-minute written test, SS2024)

1. Calculate the resulting current  $I_3$  in the cross-sectional area of  $A=300 \text{ mm}^2$  with an average circumference of  $l=3 \text{ dm}$ .

Path  $l, \Phi$

$$\Phi = 0.884 \cdot 10^{-6} \text{ Wb}$$

First formula of the magnetic resistance in a medium (all core) based on the sources:  

$$R_m = \frac{l}{\mu_0 \mu_r A} = \frac{l}{\mu_0 \mu_r A} = \frac{l}{4\pi \cdot 10^{-7} \text{ Vs/Am} \cdot \mu_r A}$$

To get the flux  $\Phi$ , the Hopkinson's Law can be applied - similar to the Ohm's Law:  

$$\Phi = \frac{NI}{R_m} = \frac{60 \text{ A} \cdot 1200}{0.884 \cdot 10^{-6} \text{ m} \cdot \frac{1}{\mu_0 \mu_r A}} = 67.8 \cdot 10^{-6} \text{ Wb} = 67.8 \cdot 10^{-6} \text{ Vs}$$

On the core, there are three coils with:

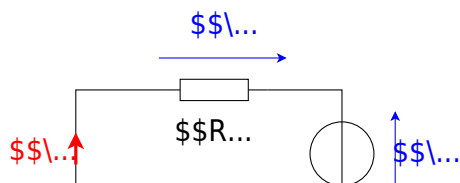
- Coil 1:  $N_1 = 1200$ ,  $I_1 = 100 \text{ mA}$
- Coil 2:  $N_2 = 33$ ,  $I_2 = 3 \text{ A}$
- Coil 3:  $N_3 = 270$ ,  $I_3 = 0.3 \text{ A}$

Refer to the drawing for the direction of the windings, current, and flux!

1. Draw the equivalent magnetic circuit that fully represents the setup. Name all the necessary magnetic resistances, fluxes, and voltages.

### Result

- Since the material, and diameter of the core is constant, one can directly simplify the magnetic resistor into a single  $R_m$ .
- For the orientation of the magnetic voltages  $\theta_1$ ,  $\theta_2$ , and  $\theta_3$ , the orientation of the coils and the direction of the current has to be taken into account by the right-hand rule.
- There is only one flux  $\Phi$
- The magnetic voltages are antiparallel to the flux for sources and parallel for the load.



**Exercise E14 Magnetic Circuit**  
**(written test, approx. 9 % of a 120-minute written test, SS2024)**

1. Calculate the resulting magnetic field  $H$  in the core with the cross-sectional area of  $A=300 \text{ mm}^2$  and an average circumference of  $l=3 \text{ dm}$ .

Result

$\Phi$

$$\Phi = \frac{I_1 N_1}{R} + \frac{I_2 N_2}{R} - \frac{I_3 N_3}{R}$$

$$= \frac{100 \cdot 1200}{0.884 \cdot 10^{-6}} + \frac{3 \cdot 33}{0.884 \cdot 10^{-6}} - \frac{0.3 \cdot 270}{0.884 \cdot 10^{-6}}$$

$$= 13884093.1 \cdot 10^6 \text{ Vs} = 13884093.1 \cdot 10^6 \text{ Vs}$$

To get the flux  $\Phi$ , the Hopkinson's Law can be applied - similar to the Ohm's Law:

$$\Phi = \frac{I_1 N_1}{R} + \frac{I_2 N_2}{R} - \frac{I_3 N_3}{R} = 67.8 \dots \cdot 10^{-6} \text{ Vs} = 67.8 \dots \cdot 10^{-6} \text{ Vs}$$

On the core, there are three coils with:

- Coil 1:  $N_1 = 1200$ ,  $I_1 = 100 \text{ mA}$
- Coil 2:  $N_2 = 33$ ,  $I_2 = 3 \text{ A}$
- Coil 3:  $N_3 = 270$ ,  $I_3 = 0.3 \text{ A}$

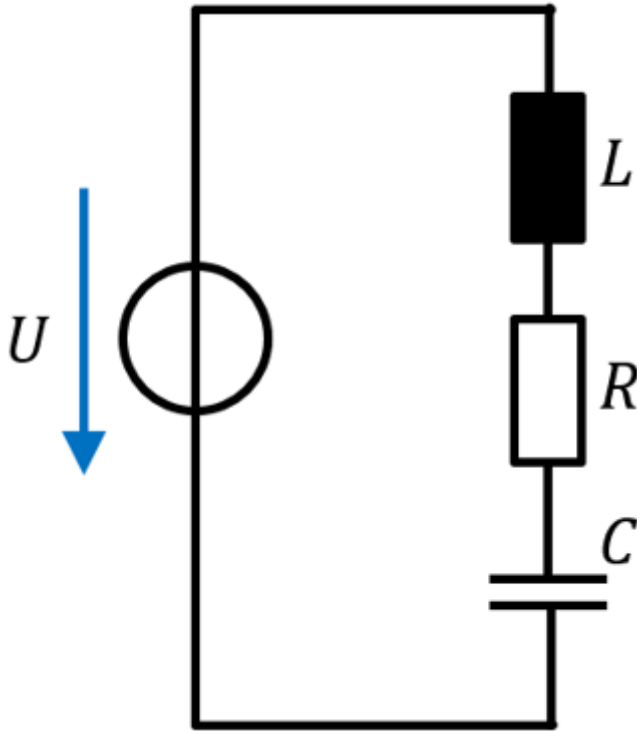
Refer to the drawing for the direction of the windings, current, and flux!

1. Draw the equivalent magnetic circuit that fully represents the setup. Name all the necessary magnetic resistances, fluxes, and voltages.

**Result**

- Since the material, and diameter of the core is constant, one can directly simplify the magnetic resistor into a single  $R \text{ m}$ .
- For the orientation of the magnetic voltages  $\theta_1$ ,  $\theta_2$ , and  $\theta_3$ , the orientation of the coils and the direction of the current has to be taken into account by the right-hand rule.
- There is only one flux  $\Phi$
- The magnetic voltages are antiparallel to the flux for sources and parallel for the load.





A given capacitor shall have the following values:

- $C=10 \text{ nF}$
- $R=20 \text{ m}\Omega$
- $L=1.6 \text{ nH}$

1. What is the impedance  $Z_{RLC}$  of this real capacitor for  $f_0=44 \text{ MHz}$ ? (Phase and magnitude)

Path

The impedance is based on the resistance  $R$  and the reactance  $X_{LC} = \text{Im}(j\omega L - \frac{1}{j\omega C})$ : 
$$\underline{Z}_{RLC} = R + j(\omega L - \frac{1}{\omega C}) = R + j(2\pi f \cdot L - \frac{1}{2\pi f \cdot C})$$

The reactive part is 
$$X_{LC} = 2\pi f \cdot L - \frac{1}{2\pi f \cdot C} = 2\pi \cdot 44 \cdot 10^6 \text{ MHz} \cdot 1.6 \cdot 10^{-9} \text{ nH} - \frac{1}{2\pi \cdot 44 \cdot 10^6 \text{ MHz} \cdot 10 \cdot 10^{-9} \text{ nF}} = +0.08062... \Omega$$

To get the magnitude of the impedance  $|\underline{Z}_{RLC}|$  one can use the Pythagorean Theorem: 
$$|\underline{Z}_{RLC}| = \sqrt{R^2 + X_{LC}^2} = \sqrt{(0.020 \Omega)^2 + (0.08062... \Omega)^2} = 0.0830... \Omega$$

For the phase  $\varphi$  the  $\arctan$  can be applied: 
$$\varphi = \arctan\left(\frac{X_{LC}}{R}\right) = \arctan\left(\frac{0.08062...}{0.020}\right)$$

$$\frac{\omega}{0.020 \omega} \right) \parallel \hat{=} 1.3276 \dots \hat{=} +76^\circ$$

**Exercise E16 Magnetic Circuit**  
 (written test, approx. 10 % of a 120-minute written test, SS2024)

2. For a sinusoidal voltage  $U_C = 100 \text{ V}$  and a frequency  $f_0 = 44 \text{ MHz}$  the voltage across the capacitor is  $U_R = 5 \text{ V}$ . The voltage across the inductor is  $U_L = 79 \text{ V}$ . What is the capacitance  $C$  in the shown circuit?

Path

$U_C = 100 \text{ V}$

- $f_0 = 44 \text{ MHz}$
- $U_R = 5 \text{ V}$
- $U_L = 79 \text{ V}$

The formula for the resonance frequency  $f_r$  is:

$$f_r = \frac{1}{2\pi\sqrt{LC}}$$

The voltage across the ideal capacitor is  $U_C = U \cdot \frac{1}{Q} = 100 \text{ V} \cdot \frac{1}{19.78} = 5.05 \text{ V}$

The voltage across the inductor is  $U_L = U \cdot Q = 100 \text{ V} \cdot 19.78 = 1978 \text{ V}$

The voltage across the resistor is  $U_R = U \cdot \frac{R}{Z} = 100 \text{ V} \cdot \frac{R}{\sqrt{R^2 + X_L^2 + X_C^2}} = 5 \text{ V}$

A given capacitor shall have the following values:

- $C = 10 \text{ nF}$
- $R = 20 \text{ m}\Omega$
- $L = 1.6 \text{ nH}$

1. What is the impedance  $Z_{RLC}$  of this real capacitor for  $f_0 = 44 \text{ MHz}$ ? (Phase and magnitude)

Path

The impedance is based on the resistance  $R$  and the reactance  $X_{LC} = \dots$

$$j\omega(X_L - X_C) = R + j\omega(X_L - X_C) \\ = R + j(\omega L - \frac{1}{\omega C}) \\ = R + j(2\pi f L - \frac{1}{2\pi f C})$$

The reactive part is

$$X_{LC} = 2\pi f L - \frac{1}{2\pi f C} \\ = 2\pi \cdot 44 \cdot 10^6 \cdot 1.6 \cdot 10^{-9} - \frac{1}{2\pi \cdot 44 \cdot 10^6 \cdot 10 \cdot 10^{-9}} \\ = +0.08062... \Omega$$

To get the magnitude of the impedance  $|Z_{RLC}|$  one can use the Pythagorean Theorem:

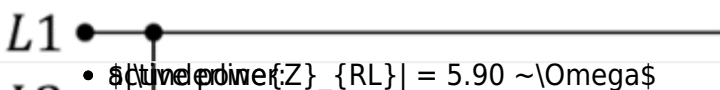
$$|Z_{RLC}| = \sqrt{R^2 + X_{LC}^2} \\ = \sqrt{(0.020 \Omega)^2 + (0.08062... \Omega)^2} = 0.0830... \Omega$$

For the phase  $\varphi$  the  $\arctan$  can be applied:

$$\varphi = \arctan\left(\frac{X_{LC}}{R}\right) = \arctan\left(\frac{0.08062... \Omega}{0.020 \Omega}\right) = 1.3276... \text{ rad} = +76^\circ$$

**Exercise E17 Magnetic Circuit**  
**(written test, approx. 10 % of a 120-minute written test, SS2024)**

2. Calculate the real power, the apparent power, and the reactive power of the 400 V / 50 Hz three-phase power net. Each single string has a resistor  $R=5 \Omega$  and an inductance of  $L=10 \text{ mH}$ .



•  $|Z_{RL}| = 5.90 \Omega$   
 •  $\varphi = 76.73^\circ$   
 The apparent power  $S$  is given by  $S = 3 \cdot U_s \cdot I_s = 3 \cdot \frac{U_s^2}{|Z_{RL}|} = 3 \cdot \frac{(230 \text{ V})^2}{5.90 \Omega} = 26.898 \text{ kVA}$   
 The active power is  $P = S \cdot \cos \varphi = 26.898 \cdot 0.8467 = 22.775 \text{ kW}$   
 The reactive power is  $Q = \sqrt{S^2 - P^2} = \sqrt{(26.898 \text{ kVA})^2 - (22.775 \text{ kW})^2} = 14.310 \text{ kVAr}$

1. Calculate the  $\cos \varphi$ , and the magnitude of the impedance  $|Z|$  for a single string.

Path

The phase  $\varphi$  is given by: 
$$\varphi = \arctan \left( \frac{X_L}{R} \right) = \arctan \left( \frac{2\pi \cdot f \cdot L}{R} \right) = \arctan \left( \frac{2\pi \cdot 50 \text{ Hz} \cdot 10 \cdot 10^{-3} \text{ H}}{5 \Omega} \right) = 0.5609 \dots \hat{=} +32^\circ$$

With this, the  $\cos \varphi$  becomes 
$$\cos \varphi = \cos(0.5609 \dots) = 0.84673 \dots$$

The impedance is given by: 
$$|Z_{RL}| = \sqrt{X_L^2 + R^2} = \sqrt{(2\pi \cdot f \cdot L)^2 + R^2} = \sqrt{(2\pi \cdot 50 \text{ Hz} \cdot 10 \cdot 10^{-3} \text{ H})^2 + (5 \Omega)^2} = 5.905 \dots \Omega$$

**Exercise E18 Magnetic Circuit**  
**(written test, approx. 10 % of a 120-minute written test, SS2024)**

2. Calculate the real power, the apparent power, and the reactive power of the 400 V / 50 Hz three-phase power net. Each single string has a resistor  $R=5 \Omega$  and an inductance of  $L=10 \text{ mH}$ .

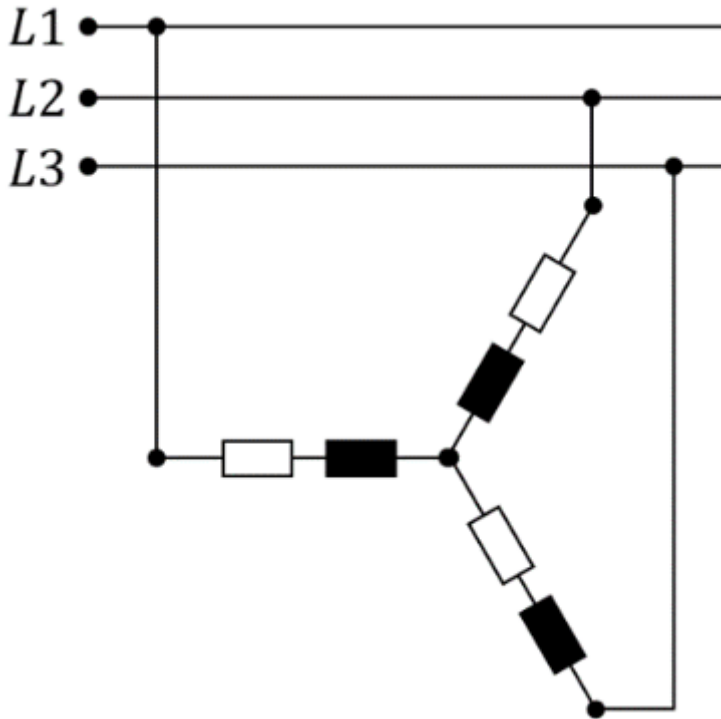
Path

- $|Z_{RL}| = 5.90 \Omega$
- $P = 22.775 \text{ kW}$

The apparent power  $S$  is given by 
$$S = 3 \cdot U_s \cdot I_s = 3 \cdot \frac{U_s^2}{|Z_{RL}|} = 3 \cdot \frac{(230 \text{ V})^2}{5.90 \Omega} = 26.898 \dots \text{ kVA}$$

The active power is 
$$P = S \cdot \cos \varphi = 26.898 \dots \cdot 0.84673 \dots = 22.775 \dots \text{ kW}$$

The reactive power is 
$$Q = \sqrt{S^2 - P^2} = \sqrt{(26.898 \dots \text{ kVA})^2 - (22.775 \dots \text{ kW})^2} = 14.310 \dots \text{ kVar}$$



1. Calculate the  $\cos \varphi$ , and the magnitude of the impedance  $|Z|$  for a single string.

Path

The phase  $\varphi$  is given by: 
$$\varphi = \arctan \left( \frac{X_L}{R} \right) = \arctan \left( \frac{2\pi \cdot f \cdot L}{R} \right) = \arctan \left( \frac{2\pi \cdot 50 \text{ Hz} \cdot 10 \cdot 10^{-3} \text{ H}}{5 \Omega} \right) = 0.5609 \dots \hat{=} +32^\circ$$

With this, the  $\cos \varphi$  becomes 
$$\cos \varphi = \cos(0.5609 \dots) = 0.84673 \dots$$

The impedance is given by: 
$$\underline{|Z|_{RL}} = \sqrt{X_L^2 + R^2} = \sqrt{(2\pi \cdot f \cdot L)^2 + R^2} = \sqrt{(2\pi \cdot 50 \text{ Hz} \cdot 10 \cdot 10^{-3} \text{ H})^2 + (5 \Omega)^2} = 5.905 \dots \Omega$$

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