

# Exam Winter Semester 2022

## Student Group

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# Exam Winter Semester 2022

## Additional permitted Aids

- non-programmable calculator,
- formulary (2 DIN A4 pages)

## Hits

- The duration of the exam is 60 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.

## Tasks

### Exercise E1 Resistance of a Wire by Resistivity

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. Heating elements are used to heat wires with a temperature of  $180^\circ\text{C}$ . The electric

power dissipation (= heat flow) of  $P=40\text{ W}$  is necessary.

Calculate the current  $I$  needed to operate for heating elements.

The Nichrome wire has a resistivity of  $1.10 \cdot 10^{-6}\ \Omega\text{ m}$ .

The heating element is  $3\text{ m}$  long and has a diameter of  $3.57\text{ mm}$ .

Calculate the resistance  $R$  of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \\ &= \sqrt{\frac{P}{R}} = \sqrt{\frac{40\text{ W}}{0.33\ \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad \& \quad A = r^2 \cdot \pi = \\ &= \frac{1}{4} d^2 \cdot \pi \quad \& \quad R = \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad \& \quad R = \\ &= 1.10 \cdot 10^{-6}\ \Omega\text{ m} \cdot \frac{4 \cdot 3\text{ m}}{(3.57 \cdot 10^{-3}\text{ m})^2 \cdot \pi} \end{aligned}$$

[electrical\\_engineering\\_and\\_electronics:task\\_rj0r6j4apumukrj6\\_with\\_calculation\\_resistivity, power, exam ee1 ws2022](#)

**Exercise E2 Temperature-dependent Resistance**  
**(written test, approx. 6 % of a 60-minute written test, WS2022)**

2. A digital display explains a kitchen refrigerator's temperature sensor. The sensor has a resistance of  $10 \text{ k}\Omega$  at  $25^\circ\text{C}$ . Its temperature coefficients are:  $\alpha = 0.01 \text{ } \frac{1}{\text{K}}$  and  $\beta = 71 \cdot 10^{-6} \text{ } \frac{1}{\text{K}^2}$ .

Result: The temperature inside the refrigeration system can reach down to  $-40^\circ\text{C}$ .

Calculate the resistance of the thermistor at  $-40^\circ\text{C}$ .

$$R = 6.5 \text{ k}\Omega$$

The power transfer is reduced by a factor of 10. Therefore, a solution is to use a heat sink.

Therefore, with constant  $U$  and increasing  $R$  the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

```

\begin{align*} R &= R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) && | \\ \text{with } \Delta T &= T_{\text{end}} - T_{\text{start}} && \\ R &= 10 \text{ k}\Omega \cdot \left(1 + 0.01 \frac{1}{\text{K}} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \cdot 10^{-6} \frac{1}{\text{K}^2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2\right) && \\ &= 6.5 \text{ k}\Omega && \end{align*}

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[electrical\\_engineering\\_and\\_electronics:task\\_70jg4yzznocarsq\\_with\\_calculation](#)  
[temperature dependent resistance, power, heat, exam ee1 ws2022](#)

**Exercise E3 Pure Resistor Network Simplification**  
**(written test, approx. 13 % of a 60-minute written test, WS2022)**

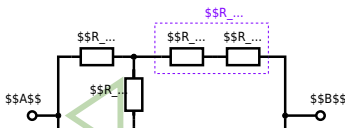
The following circuit is given.  $R_1 = 20 \text{ }\Omega$ ,  $R_2 = 10 \text{ }\Omega$ ,  $R_3 = 10 \text{ }\Omega$ ,  $R_4 = 10 \text{ }\Omega$ ,  $R_5 = 10 \text{ }\Omega$ ,  $R_6 = 10 \text{ }\Omega$ ,  $R_7 = 10 \text{ }\Omega$ ,  $R_8 = 10 \text{ }\Omega$ ,  $R_9 = 10 \text{ }\Omega$ ,  $R_{10} = 10 \text{ }\Omega$ ,  $R_{11} = 10 \text{ }\Omega$ ,  $R_{12} = 10 \text{ }\Omega$ ,  $R_{13} = 10 \text{ }\Omega$ ,  $R_{14} = 10 \text{ }\Omega$ ,  $R_{15} = 10 \text{ }\Omega$ ,  $R_{16} = 10 \text{ }\Omega$ ,  $R_{17} = 10 \text{ }\Omega$ ,  $R_{18} = 10 \text{ }\Omega$ ,  $R_{19} = 10 \text{ }\Omega$ ,  $R_{20} = 10 \text{ }\Omega$ .

Result:  $R_{\text{eq}} = 13.8 \text{ }\Omega$ .

Solution

$$R_{\text{eq}} = 13.8 \text{ }\Omega$$

Now a wye-delta transformation is necessary.

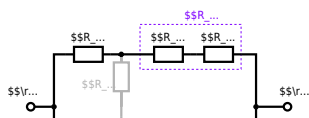


Since  $R_2=R_3$  and based on the equations for the transformation, the transformed  $R_Y$  is given as: 
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \Omega)^2}{3 \cdot 100 \Omega} = \frac{1}{3} \cdot 100 \Omega = 33.33 \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series: 
$$R_{eq} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{eq} = 33.33 \Omega + (33.33 \Omega + 400 \Omega) \parallel (33.33 \Omega + 100 \Omega)$$

1. The switch shall now be open. Calculate the equivalent resistance  $R_{eq}$  between A and B.

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1 + R_3) \parallel (R_2 + R_4) \parallel R_5$$

$$R_{\text{eq}} = (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel 500 \, \Omega$$

$$R_{\text{eq}} = (500 \, \Omega) \parallel (200 \, \Omega) \parallel 500 \, \Omega$$

$$R_{\text{eq}} = \frac{500 \, \Omega \cdot 200 \, \Omega}{500 \, \Omega + 200 \, \Omega} \parallel 500 \, \Omega$$

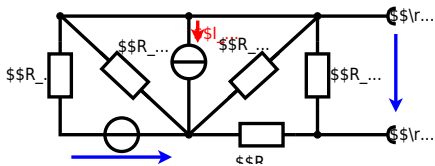
[electrical\\_engineering\\_and\\_electronics:task\\_x357drkaqv84jnsc\\_with\\_calculation](#)  
[network simplification, exam ee1 ws2022](#)

**Exercise E3 Equivalent linear Source**  
**(written test, approx. 14 % of a 60-minute written test, WS2022)**

The circuit in the following has to be simplified.  
 Result

$$U_s = U_{AB} = 4.5 \, \text{V}$$

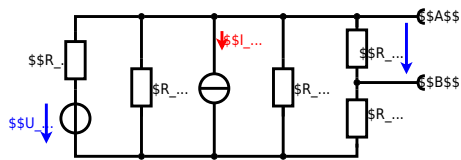
$$R_i = R_{AB} = 6 \, \Omega$$



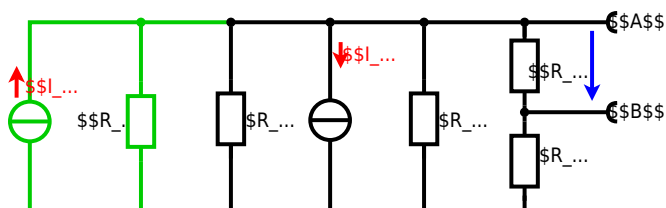
Calculated the internal resistance  $R_{\text{int}}$  and the source voltage  $U_{\text{oc}}$  of an equivalent linear voltage source on the connectors  $\text{A}$  and  $\text{B}$ .  $R_1=5.0 \text{ } \Omega$ ,  $U_2=6.0 \text{ V}$ ,  $R_3= 10 \text{ } \Omega$ ,  $I_4=4.2 \text{ A}$ ,  $R_5=10 \text{ } \Omega$ ,  $R_6=7.5 \text{ } \Omega$ ,  $R_7=15 \text{ } \Omega$  Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of  $U_2$  and  $R_1$  can be transformed into a current source  $I_2 = \frac{U_2}{R_1}$  and  $R_1$ :



Now a lot of them can be combined. The resistors  $R_1$ ,  $R_3$ ,  $R_5$  are in parallel, like also  $I_2$  and  $I_4$ :

$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_{24}}{R_1} - I_4$$

The resulting circuit can again be transformed:



Here, the  $U_{24}$  is calculated by  $I_{24}$  as the following:

$$U_{24} = I_{24} \cdot R_{67}$$

$$U_{AB} = U_{24} \cdot \left( \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} \right) - I_4 \cdot R_1 || R_3 || R_5$$

On the right side of the last circuit, there is a voltage divider given by  $R_{135}$ ,  $R_6$ , and  $R_7$ .

Therefore the voltage between  $A$  and  $B$  is given as:

$$U_{AB} = U_{24} \cdot \left( \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} \right) - \left( \frac{U_2}{R_1} - I_4 \right) \cdot R_1 || R_3 || R_5$$

For the internal resistance  $R_i$  the ideal voltage source is substituted by its resistance ( $=0\Omega$ , so a short-circuit):

$$R_{AB} = R_7 || (R_6 + R_1 || R_3 || R_5)$$

with  $R_1 || R_3 || R_5 = 5\Omega || 10\Omega || 10\Omega = 5\Omega || 5\Omega = 2.5\Omega$ :

$$U_{AB} = \left( \frac{6.0V}{5.0\Omega} - 4.2\Omega \right) \cdot \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega}$$

$$R_{AB} = 15\Omega || (7.5\Omega + 2.5\Omega)$$

[electrical\\_engineering\\_and\\_electronics:task\\_6tqtqtque1e2nf2c7\\_with\\_calculation](#)  
[dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022](#)

**Exercise E4 Charging Capacitors**  
**(written test, approx. 16 % of a 60-minute written test, WS2022)**

The circuit below (reality) also consists of  $R_1 = 6\Omega$ ,  $R_2 = 20\Omega$  and a capacitor  $C = 2\mu F$  as indicated in the figure. The switch  $S_1$  is open. The voltage across the capacitor is again  $0V$  at the moment  $t_0 = 0s$  when the switch  $S_1$  is closed. Calculate the voltage  $u_c(t_2)$  across the capacitor at  $t_2 = 1ms$  after closing the switch.

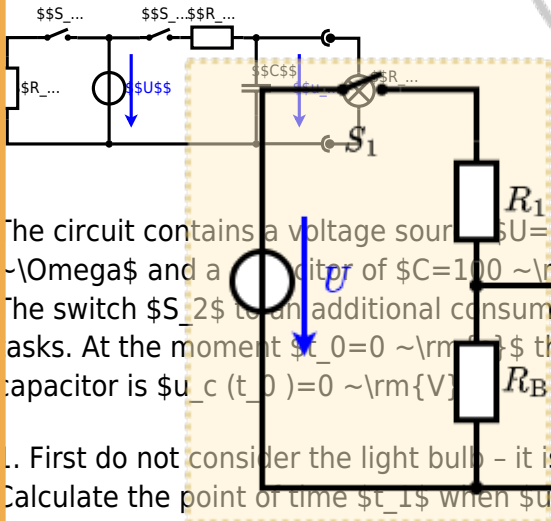
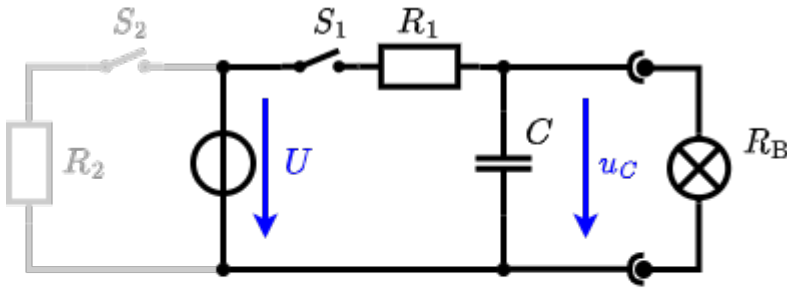
**Result:** To solve this, first create an equivalent linear voltage source from  $U$ ,  $R_1$ , and  $R_2$ .

$$U_{\Delta} = \frac{U \cdot R_2}{R_1 + R_2} = \frac{12V \cdot 20\Omega}{6\Omega + 20\Omega} = 4.615V$$

**Solution:** The internal resistance  $R_i$  is given by substituting the ideal voltage source with its internal resistance  $R_2$  and short-circuiting the ideal voltage source  $U$ .

$$R_i = R_2 || R_1 = \frac{20\Omega \cdot 6\Omega}{20\Omega + 6\Omega} = 4.615\Omega$$

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting  $R_2$ .



The circuit contains a voltage source  $U=12 \text{ V}$ , a switch  $S_1$ , a resistor of  $R_1=20 \text{ }\Omega$  and a capacitor of  $C=100 \text{ }\mu\text{F}$ .  
 The switch  $S_2$  to an additional consumer  $R_2$  will be considered to be open for the first tasks. At the moment  $t_0=0 \text{ s}$  the switch  $S_1$  is closed, the voltage across the capacitor is  $u_c(t_0)=0 \text{ V}$ .  
 ... First do not consider the light bulb - it is not connected to the RC circuit.  
 Calculate the point of time  $t_1$  when  $u_c(t_1)=0.5 \cdot U$ .

An equivalent linear voltage source can be given with  $U$ ,  $R_1$ , and  $R_B$  as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is:  $U_s = U \cdot \frac{R_B}{R_1 + R_B} = 1/2 \cdot U$   
 The internal resistance is given by substituting the ideal voltage source with its resistance ( $R_i = 0 \text{ }\Omega$ , short-circuit).  
 $R_i = R_1 \parallel R_B = 10 \text{ }\Omega$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2 / (R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1 \text{ ms} / (10 \text{ }\Omega \cdot 100 \text{ }\mu\text{F})})$$



So, here only  $R_1$  and  $C$  gives the time constant:  $\tau = R_1 \cdot C$

The following formula describes the time course of  $u_c(t)$  which has to be  $u_c(t_1)=0.5 \cdot U$ :  
 $u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$   
 It has to be rearranged to  $(1 - e^{-t/\tau}) = 0.5$   
 $e^{-t/\tau} = 0.5 \implies t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$

charging capacitors, dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022

**Exercise E5 Analyzing complex Impedances**  
(written test, approx. 14 % of a 60-minute written test, WS2022)

2. Calculate the phase angle  $\varphi$  of the voltage  $\underline{U}$  across the load impedance  $Z_L$  through the components ( $R$  and  $X_L$ ) shall be given.

After analysis, the full bidirectional complex impedance values extracted and digitized in handwritten LaTeX:  $\underline{U} = \left( \frac{1}{\sqrt{2}} \sqrt{0.24^2 + (4.68 \sim \Omega)^2} \right) \cdot \cos(\varphi) \cdot \sin(\omega t + \varphi)$

.. Calculate the physical values of the load components.  
Solution  $\begin{aligned} R &= 1.00 \sim \Omega \\ X_L &= 4.68 \sim \Omega \end{aligned}$

Solution  
$$\underline{U} = \frac{\underline{U}}{\underline{Z}} \implies \underline{U} = \{50 \sim \text{V}\} \cdot \frac{1}{\sqrt{2} \cdot \sqrt{0.24^2 + (4.68 \sim \Omega)^2}} \cdot \cos(\varphi) \cdot \sin(\omega t + \varphi)$$
  
The voltage across the capacitor is  $\underline{U}_C = \frac{1}{j\omega C} \cdot \underline{I} = -j \cdot 4.68 \sim \Omega \cdot \underline{I}$   
resulting in  $\underline{U}_C = -j \cdot 4.68 \sim \text{V}$   
Therefore, the component  $4.68 \sim \Omega$  is a capacitor with the same absolute value of  $4.68 \sim \Omega$   
impedance  $\underline{U}_R = \underline{U} - \underline{U}_C = \frac{1}{\sqrt{2}} \sqrt{0.24^2 + (4.68 \sim \Omega)^2} \cdot \cos(\varphi) \cdot \sin(\omega t + \varphi) + j \cdot 4.68 \sim \text{V}$   
$$\underline{U}_R = \frac{1}{\sqrt{2}} \sqrt{0.24^2 + (4.68 \sim \Omega)^2} \cdot \cos(\varphi) \cdot \sin(\omega t + \varphi) + j \cdot 4.68 \sim \text{V}$$
  
The absolute value  $U_R = \sqrt{0.24^2 + (4.68 \sim \Omega)^2} \cdot \cos(\varphi)$  is calculated as  $\begin{aligned} \cos(\varphi) &= \frac{U_R}{U} = \frac{\sqrt{0.24^2 + (4.68 \sim \Omega)^2} \cdot \cos(\varphi)}{50 \sim \text{V}} \\ \cos(\varphi) &= \frac{0.24 \sim \text{V}}{50 \sim \text{V}} \implies \varphi = \arccos\left(\frac{0.24}{50}\right) \approx 89.76^\circ \end{aligned}$   
With the complex part comes the physical values  $\begin{aligned} R &= 1.00 \sim \Omega \\ X_L &= 4.68 \sim \Omega \end{aligned}$   
The phase  $\varphi$  can be calculated as  $\begin{aligned} \varphi &= \arctan\left(\frac{\text{Im}(\underline{U})}{\text{Re}(\underline{U})}\right) = \arctan\left(\frac{-4.68 \sim \Omega}{0.24 \sim \Omega}\right) \approx -89.76^\circ \end{aligned}$

electrical\_engineering\_and\_electronics:task\_jti0uzudcmg4u22t\_with\_calculation  
complex impedance, exam ee1 ws2022

**Exercise E6 Impedances at different Frequencies**  
(written test, approx. 18 % of a 60-minute written test, WS2022)

2. A RC parallel circuit with  $R=1 \sim \Omega$  and  $C=10 \sim \text{nF}$  is driven at  $f=1 \sim \text{MHz}$ . Determine the value of  $R_1$  such that the absolute value of the impedance is the same as a capacitor  $C_1=40 \sim \text{nF}$  at  $f_1=4 \sim \text{MHz}$ .

Solution  
Solution  $\begin{aligned} R_1 &= 1.00 \sim \Omega \\ R_2 &= 10.0 \sim \Omega \end{aligned}$

A series circuit means that the current is constant on every component.  
 The equivalent resistance for the parallel combination is given by  $\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$ .  
 Since the voltage across the parallel combination is  $V_{parallel} = V_{total} - V_{R1}$ , the current through the parallel combination is  $I_{parallel} = \frac{V_{parallel}}{R_{eq}}$ .  
 The total current is  $I_{total} = I_{R1} + I_{parallel}$ .  
 The power dissipated in the parallel combination is  $P_{parallel} = I_{parallel}^2 R_{eq}$ .  
 The power dissipated in the series resistor is  $P_{R1} = I_{R1}^2 R_1$ .  
 The total power dissipated is  $P_{total} = P_{R1} + P_{parallel}$ .  
 The equivalent resistance for the parallel combination is  $R_{eq} = \frac{R_1 R_2 R_3}{R_1 R_2 + R_1 R_3 + R_2 R_3}$ .  
 The voltage across the parallel combination is  $V_{parallel} = V_{total} - I_{R1} R_1$ .  
 The current through the parallel combination is  $I_{parallel} = \frac{V_{parallel}}{R_{eq}}$ .  
 The total current is  $I_{total} = I_{R1} + I_{parallel}$ .  
 The power dissipated in the parallel combination is  $P_{parallel} = I_{parallel}^2 R_{eq}$ .  
 The power dissipated in the series resistor is  $P_{R1} = I_{R1}^2 R_1$ .  
 The total power dissipated is  $P_{total} = P_{R1} + P_{parallel}$ .

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 complex impedance, exam ee1 ws2022

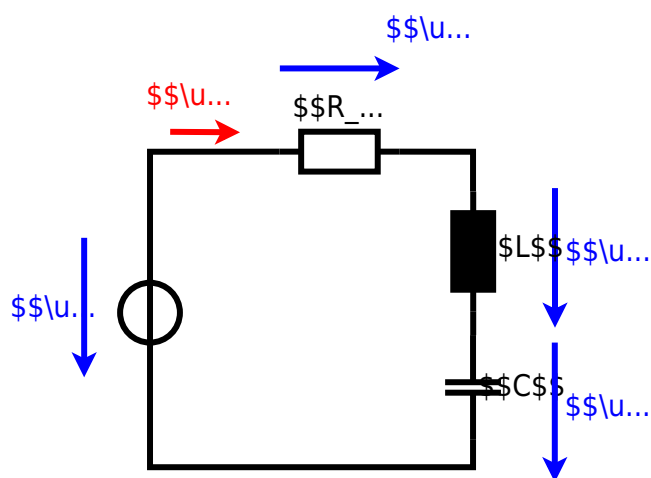
**Exercise E7 Complex Impedance Circuit**  
 (written test, approx. 15 % of a 60-minute written test, WS2022)

2. Consider the circuit below. The voltage source is  $u(t) = 3.0 \sin(2\pi \cdot 15 \cdot t)$  V. The circuit consists of a series combination of a resistor  $R = 10 \Omega$ , an inductor  $L = 330 \mu\text{H}$ , and a capacitor  $C = 0.22 \mu\text{F}$ .  
 a) Calculate the complex impedance  $Z$  of the circuit.  
 b) Calculate the magnitude of the total current  $I$  and the phase angle  $\phi$  between the voltage and the current.  
 c) Calculate the average power  $P_{avg}$  dissipated in the circuit.

**Solution**  
 Result:  $Z = 10 + j19.8 - j48.2 \Omega$   
 $I = 0.192 \text{ A}$   
 $\phi = 68.7^\circ$   
 $P_{avg} = 0.35 \text{ W}$

Draw the circuit diagram of the given circuit with all components, voltages, and currents.  
 $Z = \frac{U}{I}$   
 $Z_C = \frac{1}{j\omega C}$   
 Result:  $Z = 10 + j19.8 - j48.2 \Omega$   
 With  $I = 0.192 \text{ A}$   
 $P_{avg} = 0.35 \text{ W}$





electrical\_engineering\_and\_electronics:task\_kricv9fh7haauo6q\_with\_calculation  
complex impedance, exam ee1 ws2022

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