Block 14 - The steady Conduction Field

Student Group

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Learning objectives

After this 90-minute block, you can

- explain what a **steady (stationary) conduction field** is and relate it to the electrostatic field (cause/effect view: $\vec{E}$ vs. $\vec{D}$; conduction uses $\vec{E}$ and material σ).
- use the **current-density law** $\vec{j}=\sigma\,\vec{E}$ and the **current flux** $I=\iint_A \vec{j}\cdot{\rm d}\vec{A}$ with correct surface orientation.
- derive and calculate **conductance** G and **resistance** R for key geometries (parallel plates $G=\sigma A/l$, coaxial $G=\dfrac{2\pi\sigma l}{\ln(r_a/r_i)}$; hence $R=\rho\,l/A$, $R=\rho\,\ln(r_a/r_i)/(2\pi l)$). :contentReference{index=2}
- reason about **bottlenecks**: constant I along a conductor, compression of equipotential surfaces where cross-section shrinks, and the link to larger local voltage drop. :contentReference{index=3}
- compute **electron drift speed** $v_{\rm e}=\dfrac{I}{n_{\rm e}\,e\,A}$ and interpret its small magnitude vs. the signal speed. :contentReference{index=4}
- apply the **pragmatic derivation** $ {\rm d}U=I\,{\rm d}R \Rightarrow {\rm d}U=\rho\,S\,{\rm d}s$ and with $E=\dfrac{{\rm d}U}{{\rm d}s}$ obtain $\vec{j}=\sigma\,\vec{E}$. :contentReference{index=5}

Preparation at Home

Well, again

- read through the present chapter and write down anything you did not understand.
- Also here, there are some clips for more clarification under 'Embedded resources' (check the text above/below, sometimes only part of the clip is interesting).

For checking your understanding please do the following exercises:

- ...

90-minute plan

1. Warm-up (x min):
    1. ....
2. Core concepts & derivations (x min):
    1. ...
3. Practice (x min): ...
4. Wrap-up (x min): Summary box; common pitfalls checklist.

Conceptual overview

1. ...

Core content

In the discussion of the electrostatic field in principle, no charges in motion were considered.
This lead to multiple fomulas, which are aggregated in the following diagram:

Fig. 1: summary of electro static field

Now the motion of charges shall be considered explicitly.
With the knowledge of th electrostatic field, we want to see, whether we can calulate the resistance of more complicated geometries.

For this we want to introduce the current density J: The current density here describes how charge carriers move together (collectively). The stationary current density describes the charge carrier movement if a **direct voltage** is the cause of the movement.
Then, a constant direct current flows in the stationary electric flow field. Thus, there is no time dependency on the current:

$\large{{{\rm d}I}\over{{\rm d}t}}=0$

Important: Up to now it was considered, that charges had moved through a field in the past or could be moved in the future. Now, the exact moment of moving the charge is considered.

Fig. 2: summary of conduction field

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ele...

$$\vec{J}=\

$$P= \vec{E} \

$$.= \! \! \int \...
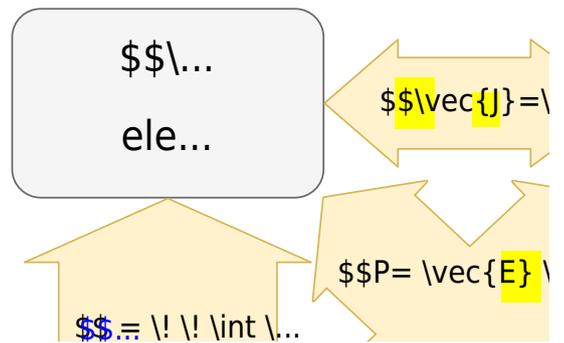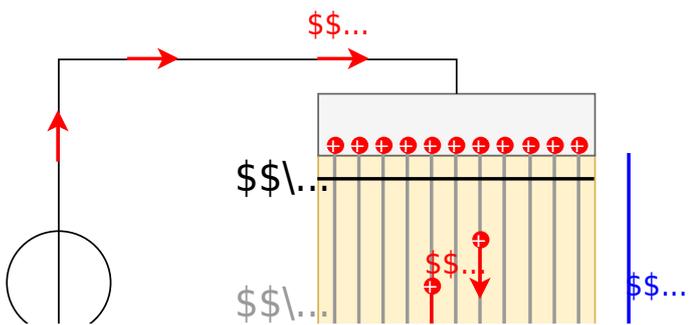
Common pitfalls

- ...

Exercises

Worked examples

...

Embedded resources

Explanation (video): ...

The online book 'University Physics II' is strongly recommended as a reference for this chapter. Especially the following chapters:

- Chapter 9.3 Model of Conduction in Metals

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