

task_wjttvmydrskzhcim_with_calculation

Student Group

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complex voltage divider, RMS, inductor, exam ee2 SS2021

Exercise E15 Component Parameters**(written test, approx. 10 % of a 120-minute written test, SS2021)**

Determine the component parameters of a motor (motor M) presents a resistive inductive load! For the next exercises consider the following: The RMS values of the series resistance R_{M} and the inductance L_{M} are to be determined below. Both results in the impedance of the motor.

This resulted in the recorded current of

Derive in general the equation for the absolute value of the impedance of the motor.

$$Z = \sqrt{(2\pi \cdot f \cdot L_{\text{M}})^2 + R_{\text{M}}^2}$$

$$R_{\text{M}} = \frac{U_{\text{RMS}}}{I_{\text{RMS}}}$$

$$L_{\text{M}} = \frac{Z^2 - R_{\text{M}}^2}{(2\pi \cdot f)^2}$$

Since we have Z_1 and Z_2 from b) we can subtract two of the formulas from I_1 and I_2 (independent). This has the advantage that R_{M} will cancel out:

$$Z_2^2 - Z_1^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 - \left((2\pi \cdot f_1 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 \right)$$

The complex impedance Z for a resistive inductive load R_{M} and L_{M} in series circuit is given as

$$\underline{Z} = R_{\text{M}} + j\omega L_{\text{M}}$$

$$|Z|^2 = R_{\text{M}}^2 + (\omega L_{\text{M}})^2$$

Now we can rearrange to L_{M} :

The Pythagorean theorem can derive the absolute value:

$$Z_2^2 - Z_1^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 - \left((2\pi \cdot f_1 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 \right)$$

$$Z_2^2 - Z_1^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 - (2\pi \cdot f_1 \cdot L_{\text{M}})^2$$

$$Z_2^2 - Z_1^2 = L_{\text{M}}^2 \cdot (2\pi \cdot f_2)^2 - L_{\text{M}}^2 \cdot (2\pi \cdot f_1)^2$$

$$Z_2^2 - Z_1^2 = L_{\text{M}}^2 \cdot (2\pi)^2 \cdot (f_2^2 - f_1^2)$$

$$L_{\text{M}} = \frac{Z_2^2 - Z_1^2}{(2\pi)^2 \cdot (f_2^2 - f_1^2)}$$

And then to L_{M} :

$$L_{\text{M}} = \frac{1}{2\pi} \sqrt{\frac{Z_2^2 - Z_1^2}{f_2^2 - f_1^2}}$$

With the values:

$$L_{\text{M}} = \frac{1}{2\pi} \sqrt{\frac{(10 \cdot \Omega)^2 - (6.25 \cdot \Omega)^2}{(100 \cdot \text{s}^{-1})^2 - (50 \cdot \text{s}^{-1})^2}} = 14.346 \dots \text{ mH}$$

The resistance value R_{M} can be derived from

$$Z_2^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 \implies R_{\text{M}}^2 = Z_2^2 - (2\pi \cdot f_2 \cdot L_{\text{M}})^2$$

$$R_{\text{M}} = \sqrt{Z_2^2 - (2\pi \cdot f_2 \cdot L_{\text{M}})^2}$$

The values have to be inserted also for R_{M} :

$$R_{\text{M}} = \sqrt{(10 \cdot \Omega)^2 - (2\pi \cdot 100 \cdot \text{s}^{-1} \cdot 0.014346 \dots \text{ H})^2} = 4.3301 \dots \cdot \Omega$$

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Last update: **2024/07/04 01:51**

