task_tb6pi8dgh0m2e2pw_with_calculation

Student Group

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Charging Capacitors, dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 WS2022
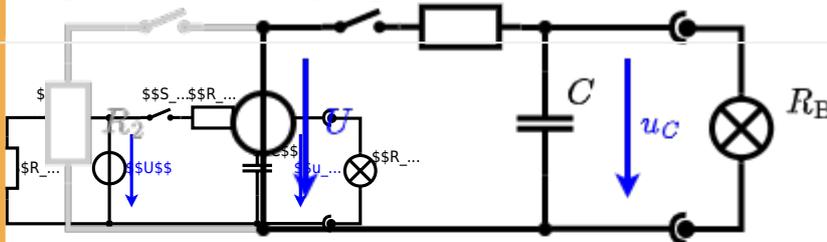
Exercise E4 Charging Capacitors
**(written test, approx. 16 % of a 60-minute written test, WS2022)**

The circuit contains a voltage source $U=12 ~\rm{V}$, a switch S_1, a resistor of $R_1=20 ~\Omega$ and a capacitor of $C=100 ~\rm{µF}$.
The switch S_2 to an additional consumer R_2 will be considered to be open for the first tasks. At the moment $t_0=0 ~\rm{s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c (t_0)=0 ~\rm{V}$.

1. First do not consider the light bulb – it is not connected to the RC circuit.
Calculate the point of time t_1 when $u_c (t_1)=0.5\cdot U$.

Solution
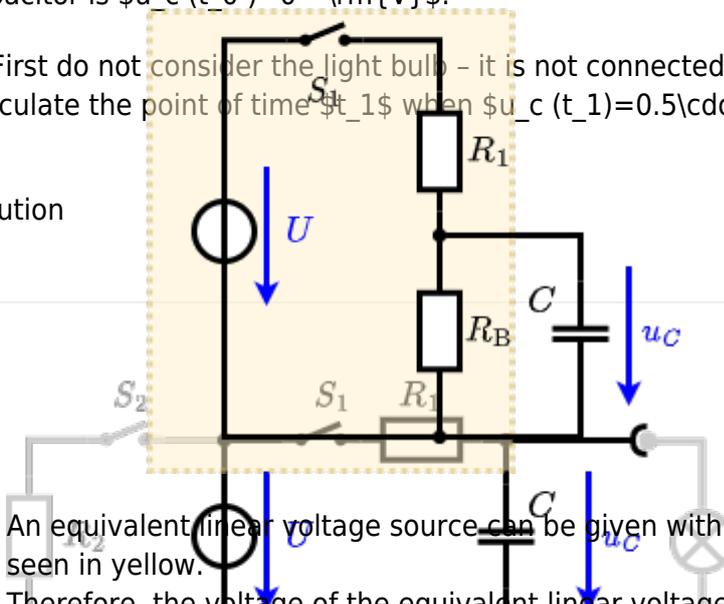
An equivalent linear voltage source can be given with U, R_1, and $R_\rm B$ as seen in yellow.
Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot {{R_\rm B}\over {R_1 + R_\rm B}} = 1/2 \cdot U$ The internal resistance is given by substituting the ideal voltage source with its resistance ($=0 ~\Omega$, short-circuit).

So, $\begin{align*} R_1 &= R \text{ (the resistance constant } \Omega = R_1 \end{align*}$

The following formula describes the time course of $R \cdot C$ which has $\frac{1}{2}$

$\begin{align*} t &= 0.5 \cdot (1 - e^{t/\tau}) \\ &= 0.5 \end{align*}$

\end{align*} It has to be rearranged to t \begin{align*} (1- e^{t/\tau}) &= 0.5 \\ e^{t/\tau} &= 0.5 \\ t/\tau &= ln(0.5) \\ t &= \tau \cdot ln(0.5) \\ t &= R_1 \cdot C \cdot ln(0.5) \end{align*}