

Exam Winter Semester 2022

Student Group

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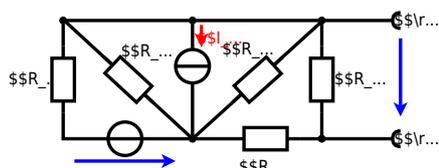
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**Exercise E1 Equivalent linear Source
(written test, approx. 14 % of a 60-minute written test, WS2022)**

The circuit in the following has to be simplified.
Result

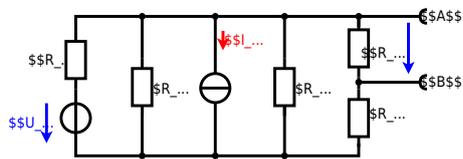
$$\begin{aligned} U_{\text{rs}} &= U_{\text{AB}} = 4.5 \text{ V} \\ R_{\text{i}} &= R_{\text{AB}} \\ &= 6 \text{ } \Omega \end{aligned}$$



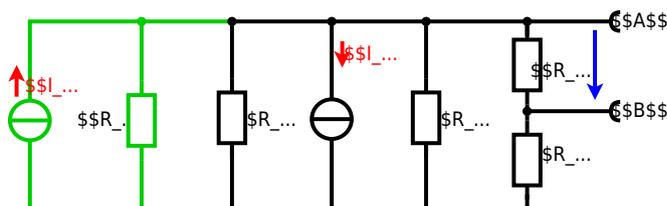
Calculated the internal resistance R_{i} and the source voltage U_{rs} of an equivalent linear voltage source on the connectors A and B .
$$R_1=5.0 \text{ } \Omega, \quad U_2=6.0 \text{ V}, \quad R_3= 10 \text{ } \Omega, \quad I_4=4.2 \text{ A}, \quad R_5=10 \text{ } \Omega, \quad R_6=7.5 \text{ } \Omega, \quad R_7=15 \text{ } \Omega$$
 Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:

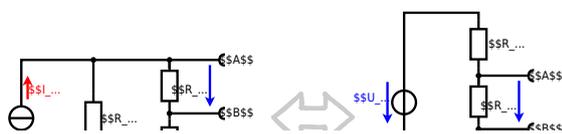


The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :
$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4$$
 The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:
$$U_{24} = I_{24} \cdot R_{135}$$

$$U_{24} = U_2 \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} - I_4 \cdot R_1 \parallel R_3 \parallel R_5$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} - (U_2 \cdot \frac{R_7}{R_1} - I_4) \cdot \frac{R_7 \cdot R_1 \parallel R_3 \parallel R_5}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

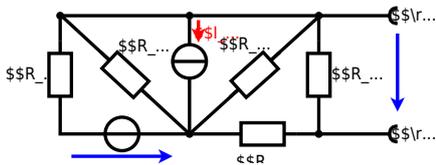
with $R_1 \parallel R_3 \parallel R_5 = 5\Omega \parallel 10\Omega \parallel 10\Omega = 5\Omega \parallel 5\Omega = 2.5\Omega$:

$$U_{AB} = \frac{6.0\text{V}}{5.0\Omega} - 4.2\Omega \cdot \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega} \parallel R_{AB} = 15\Omega \parallel (7.5\Omega + 2.5\Omega)$$

Exercise E3 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

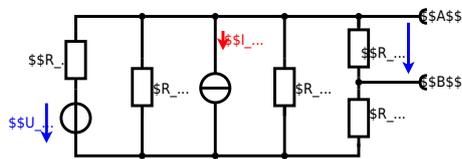
$$U_s = U_{AB} = 4.5\text{V} \parallel R_i = R_{AB} = 6\Omega$$



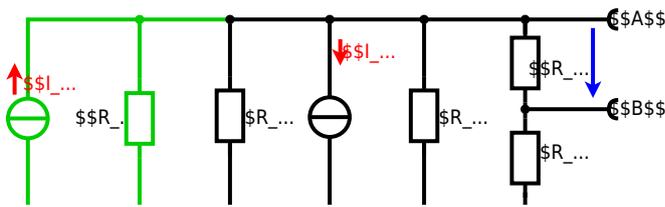
Calculate the internal resistance R_{int} and the source voltage U_{s} of an equivalent linear voltage source on the connectors A and B . $R_1=5.0 \Omega$, $U_2=6.0 \text{ V}$, $R_3=10 \Omega$, $I_4=4.2 \text{ A}$, $R_5=10 \Omega$, $R_6=7.5 \Omega$, $R_7=15 \Omega$. Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :
$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4$$
 The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:
$$U_{24} = I_{24} \cdot R_{135}$$

$$U_{24} = R_{135} \cdot I_{24} \quad \&= \left(\frac{U_2}{R_1} - I_4 \right) \cdot R_1 \parallel R_3 \parallel R_5$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} \quad \&= \left(\frac{U_2}{R_1} - I_4 \right) \cdot \frac{R_7 \cdot R_1 \parallel R_3 \parallel R_5}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

with $R_1 \parallel R_3 \parallel R_5 = 5 \Omega \parallel 10 \Omega \parallel 10 \Omega = 5 \Omega \parallel 5 \Omega = 2.5 \Omega$:

$$U_{AB} = \frac{6.0 \text{ V}}{5.0 \Omega} - 4.2 \Omega \cdot \frac{15 \Omega \cdot 2.5 \Omega}{7.5 \Omega + 15 \Omega + 2.5 \Omega} \quad R_{AB} = 15 \Omega \parallel (7.5 \Omega + 2.5 \Omega)$$

Exercise E2 Analyzing complex Impedances
(written test, approx. 14 % of a 60-minute written test, WS2022)

2. Calculate the phasor voltage \underline{U}_X in the circuit shown in the figure. The components (R and \underline{X}_1) shall be given.

After analysis, the full dimensional circuit impedance Z can be extracted and \underline{U}_X in phasor notation $\underline{U}_X = \left(\frac{2}{\sqrt{2}} + 4(\sqrt{2} + 5j) \right) \Omega$

Solution
.. Calculate the physical values of the components.

$$R = 0.1 \Omega \quad \underline{X}_1 = 2.8 \Omega \quad \underline{X}_2 = 8.1 \Omega$$

Solution

$$\underline{I} = \frac{\underline{U}}{Z} \quad \&= \frac{50 \text{ V}}{0.24 \Omega + j4.68 \Omega} = \frac{50}{4.72 \angle 87.1^\circ} = 10.6 \angle -87.1^\circ \text{ A}$$

The current and voltage are in phase and the voltage \underline{U}_X is pure real resulting in $\underline{U}_X = \underline{I} \cdot \underline{X}_1 = 10.6 \angle -87.1^\circ \cdot 2.8 \angle 90^\circ = 29.7 \angle 3.9^\circ \text{ V}$

Therefore, the component 4.68Ω is in parallel with the same absolute value of impedance $\underline{X}_2 = 8.1 \angle 90^\circ \Omega$ and $\underline{X}_1 = 2.8 \angle 90^\circ \Omega$ in series.

$$\underline{Z} = \left(\frac{2}{\sqrt{2}} + 4(\sqrt{2} + 5j) \right) \Omega = \left(1.41 + 5.65j \right) \Omega \parallel \left(8.1j \right) \Omega + 0.1 \Omega$$

$$\underline{Z} = \frac{(1.41 + 5.65j) \cdot 8.1j}{1.41 + 5.65j + 8.1j} + 0.1 \Omega = \frac{4.54 - 45.8j}{9.75 + 13.75j} + 0.1 \Omega$$

$$\underline{Z} = \frac{4.54 - 45.8j}{13.75 + 9.75j} + 0.1 \Omega = \frac{4.54 - 45.8j}{13.75 + 9.75j} + 0.1 \Omega$$

$$\underline{Z} = \frac{(4.54 - 45.8j) \cdot (13.75 - 9.75j)}{(13.75 + 9.75j)(13.75 - 9.75j)} + 0.1 \Omega = \frac{62.1 - 49.1j - 500j - 447.1}{191.25 - 95.25j - 95.25j - 191.25} + 0.1 \Omega$$

$$\underline{Z} = \frac{-385.0 - 549.1j}{-191.25} + 0.1 \Omega = 2.01 + 2.87j + 0.1 \Omega = 2.11 + 2.87j \Omega$$

$$\underline{I} = \frac{50 \text{ V}}{2.11 + 2.87j \Omega} = \frac{50}{3.58 \angle 53.7^\circ} = 13.97 \angle -53.7^\circ \text{ A}$$

With the complex part comes the physical value $I = \frac{13.97}{\sqrt{2}} = 9.87 \text{ A}$

$$\underline{U}_X = \underline{I} \cdot \underline{X}_1 = 9.87 \text{ A} \cdot 2.8 \Omega = 27.6 \text{ V}$$

Solution

$$\underline{R}_1 \dot{I} = \underline{R}_2 + \underline{X}_{L2} \dot{I} \quad \text{||} \quad \underline{R}_2 + \underline{X}_{L2} \dot{I} \perp \underline{R}_3 \dot{I}$$

$$\underline{R}_3 \dot{I} \perp \underline{R}_2 + \underline{X}_{L2} \dot{I} \quad \text{||} \quad \underline{R}_3 \dot{I} \perp \underline{R}_2 + \underline{X}_{L2} \dot{I}$$

$$\underline{R}_3 \dot{I} \perp \underline{R}_2 + \underline{X}_{L2} \dot{I} \quad \text{||} \quad \underline{R}_3 \dot{I} \perp \underline{R}_2 + \underline{X}_{L2} \dot{I}$$

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Exercise E6 Impedances at different Frequencies
 (written test, approx. 18 % of a 60-minute written test, WS2022)

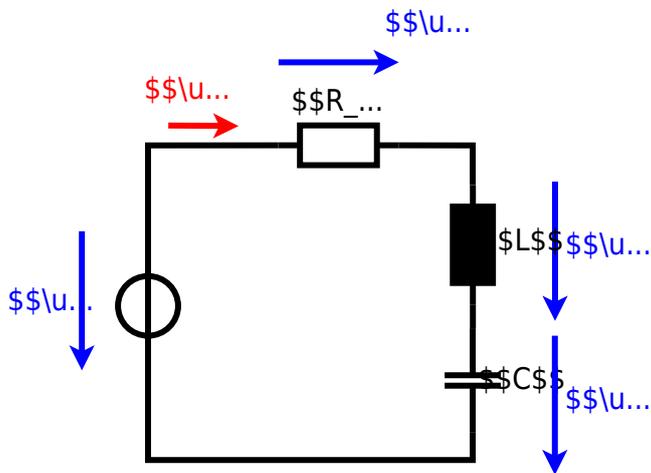
A series circuit means that the current is constant on every component.
 The equivalent impedance for R and L combined is given by $\underline{R} + j\omega L$. Since $j\omega L$ is perpendicular to R , this can be simplified to $\sqrt{R^2 + (\omega L)^2}$. So it gets clear that $\underline{R}_3 \dot{I}$ is perpendicular to $\underline{R}_2 + \underline{X}_{L2} \dot{I}$ (It has to, since $\underline{R}_3 \dot{I}$ is perpendicular to $j\omega L \dot{I}$, too).
 Therefore the resulting current of the parallel circuit is given as: $\underline{I}_3 = \frac{\underline{I}_2 + \underline{I}_3}{\sqrt{R_2^2 + (\omega L)^2}}$
 $\underline{I}_3 \sqrt{R_2^2 + (\omega L)^2} = \underline{I}_2 + \underline{I}_3$
 $\underline{I}_3 (\sqrt{R_2^2 + (\omega L)^2} - 1) = \underline{I}_2$
 $\underline{I}_3 = \frac{\underline{I}_2}{\sqrt{R_2^2 + (\omega L)^2} - 1}$
 Back to the first formula: $\underline{R}_3 \dot{I} = \underline{X}_{L3} \dot{I} + \underline{I}_3 \sqrt{R_2^2 + (\omega L)^2}$
 $\underline{R}_3 \dot{I} = \underline{X}_{L3} \dot{I} + \frac{\underline{I}_2 \sqrt{R_2^2 + (\omega L)^2}}{\sqrt{R_2^2 + (\omega L)^2} - 1}$

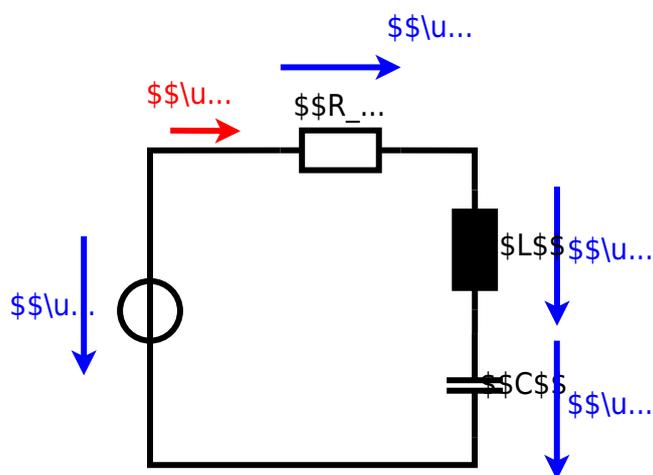
Solution

$$\underline{R}_1 = 1.00 \sim \Omega$$

$$\underline{R}_2 = 10.0 \sim \Omega$$

A series circuit means that the current is constant on every component.
 The equivalent impedance for R and L combined is given by $\underline{R} + j\omega L$. Since $j\omega L$ is perpendicular to R , this can be simplified to $\sqrt{R^2 + (\omega L)^2}$. So it gets clear that $\underline{R}_3 \dot{I}$ is perpendicular to $\underline{R}_2 + \underline{X}_{L2} \dot{I}$ (It has to, since $\underline{R}_3 \dot{I}$ is perpendicular to $j\omega L \dot{I}$, too).
 Therefore the resulting current of the parallel circuit is given as: $\underline{I}_3 = \frac{\underline{I}_2 + \underline{I}_3}{\sqrt{R_2^2 + (\omega L)^2}}$
 $\underline{I}_3 \sqrt{R_2^2 + (\omega L)^2} = \underline{I}_2 + \underline{I}_3$
 $\underline{I}_3 (\sqrt{R_2^2 + (\omega L)^2} - 1) = \underline{I}_2$
 $\underline{I}_3 = \frac{\underline{I}_2}{\sqrt{R_2^2 + (\omega L)^2} - 1}$
 Back to the first formula: $\underline{R}_3 \dot{I} = \underline{X}_{L3} \dot{I} + \underline{I}_3 \sqrt{R_2^2 + (\omega L)^2}$
 $\underline{R}_3 \dot{I} = \underline{X}_{L3} \dot{I} + \frac{\underline{I}_2 \sqrt{R_2^2 + (\omega L)^2}}{\sqrt{R_2^2 + (\omega L)^2} - 1}$





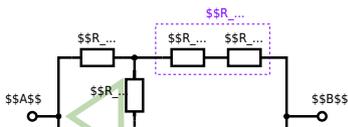
Exercise E6 Pure Resistor Network Simplification
(written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall be solved at once, $R_2 = R_3 = 100 \Omega$ and the switch shall be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution

$$R_{eq} = 132.8 \Omega$$

Now a wye-delta transformation is necessary.



Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:

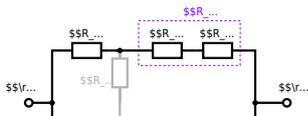
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \Omega)^2}{3 \cdot 100 \Omega} = \frac{1}{3} \cdot 100 \Omega = 33.33 \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{eq} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel (R_Y + R_2)$$

.. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = (100 \sim \Omega + 200 \sim \Omega + 200 \sim \Omega) \parallel (100 \sim \Omega + 100 \sim \Omega) \parallel R_{\text{eq}} = (500 \sim \Omega) \parallel (200 \sim \Omega) \parallel R_{\text{eq}} = \frac{\{500 \sim \Omega \cdot 200 \sim \Omega\}}{500 \sim \Omega + 200 \sim \Omega}$$

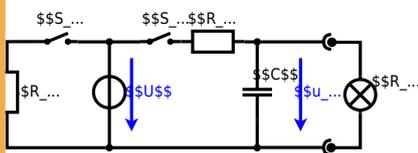
Exercise E5 Charging Capacitors
 (written test, approx. 16 % of a 60-minute written test, WS2022)

The capacitor is initially open, the voltage across the capacitor is again U_0 at the moment $t_0 = 0$ s when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1$ ms after closing the switch.

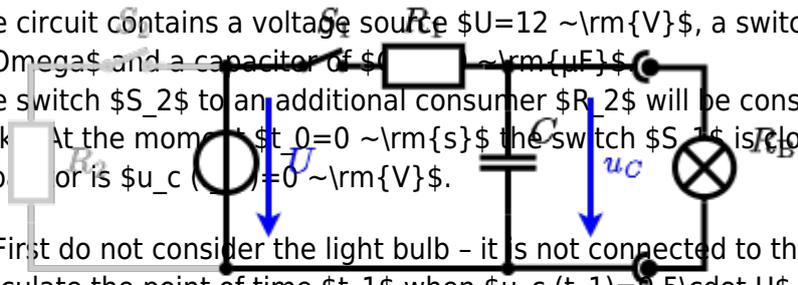
Result: To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

$$U_{\text{eq}} = \frac{U \cdot R_2}{R_1 + R_2} \quad \text{and} \quad R_{\text{eq}} = R_1 \parallel R_2 = \frac{R_1 \cdot R_2}{R_1 + R_2}$$

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

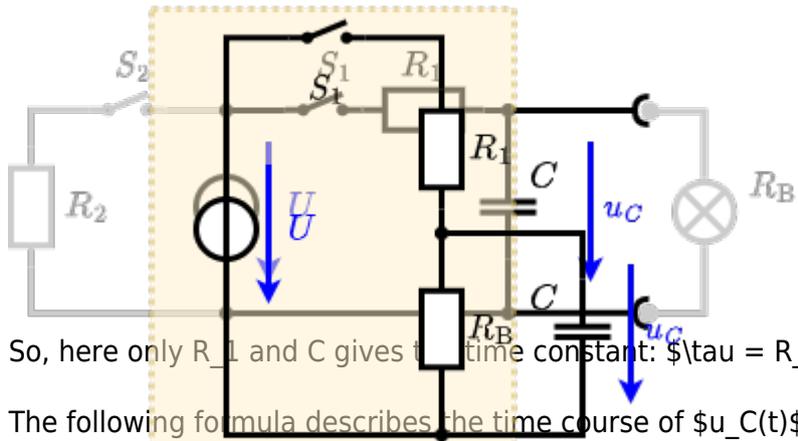
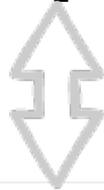


The circuit contains a voltage source $U=12\text{ V}$, a switch S_1 , a resistor of $R_1=20\text{ }\Omega$ and a capacitor of $C=100\text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first task. At the moment $t_0=0\text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0)=0\text{ V}$.



First do not consider the light bulb - it is not connected to the RC circuit. Calculate the point of time t_1 when $u_c(t_1)=0.5 \cdot U$.

Solution



So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1)=0.5 \cdot U$:

$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5$.
 An equivalent linear voltage source can be given with U_s , R_1 and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = 1/2 \cdot U$. The internal resistance is given by substituting the ideal voltage source with its resistance ($r=0\text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1\text{ ms}/(10\text{ }\Omega \cdot 100\text{ }\mu\text{F})})$$

Exercise E4 Charging Capacitors
 (written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (as shown in the figure) consists of a DC voltage source $U=6\text{ V}$, a resistor $R_1=20\text{ }\Omega$, a capacitor $C=20\text{ }\mu\text{F}$ and a light bulb $R_B=20\text{ }\Omega$. The switch S_1 is open. The voltage across the capacitor is again 0 V at the moment $t_0=0\text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2=1\text{ ms}$ after closing the switch.

Solution To solve this, first create an equivalent linear voltage source from U , R_1 , and R_B .

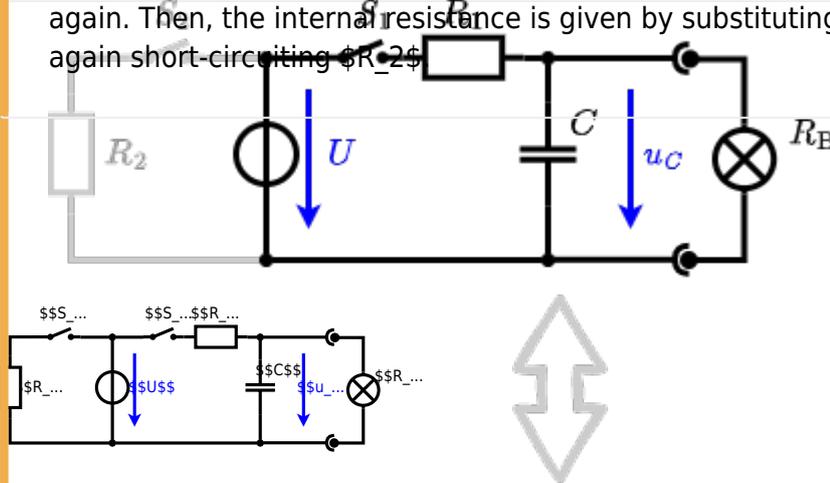
$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = 3\text{ V}$$

$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

Solution

The ideal voltage source is $U = 12 \text{ V}$. The internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

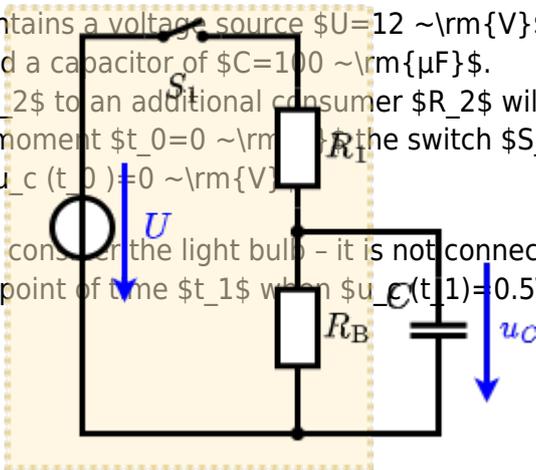
On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .



The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ }\Omega$ and a capacitor of $C = 100 \text{ }\mu\text{F}$.

The switch S_2 to an additional consumer R_2 will be considered to be open for the first asks. At the moment $t_0 = 0$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0$.

First do not consider the light bulb - it is not connected to the RC circuit. Calculate the point of time t_1 when $u_c(t_1) = 0.5 \cdot U$.



Solution

An equivalent linear voltage source can be given with U , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$. The internal resistance is given by substituting the ideal voltage source with its resistance ($R = 0 \text{ }\Omega$, short-circuit). $R_i = R_1 \parallel R_B = 10 \text{ }\Omega$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2 / (R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-t_2 / (10 \text{ }\Omega \cdot 100 \text{ }\mu\text{F})})$$

So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_C(t)$ which has to be $u_c(t_1) = 0.5 \cdot U$: $u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$. It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$

Exercise E1 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)

2. A refrigerator, explains a thermodynamic process in a refrigeration system. The food has a resistance of $10 \text{ k}\Omega$ at 25°C . Your answer.

Its temperature coefficients are: $\alpha=0.01 \text{ K}^{-1}$ and $\beta=71 \cdot 10^{-6} \text{ K}^{-2}$

Result: The temperature inside the refrigeration system can reach down to -40°C .

Calculate the resistance of the thermistor at -40°C .

The power transfer is $P = U \cdot I$ and $I = \frac{U}{R}$. Therefore, a solution is to increase the resistance of the thermistor. Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \quad \Delta T = T_{\text{end}} - T_{\text{start}}$$
$$R = 10 \text{ k}\Omega \cdot \left(1 + 0.01 \text{ K}^{-1} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \cdot 10^{-6} \text{ K}^{-2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2\right)$$

Exercise E2 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)

2. A refrigerator, explains a thermodynamic process in a refrigeration system. The food has a resistance of $10 \text{ k}\Omega$ at 25°C . Your answer.

Its temperature coefficients are: $\alpha=0.01 \text{ K}^{-1}$ and $\beta=71 \cdot 10^{-6} \text{ K}^{-2}$

Result: The temperature inside the refrigeration system can reach down to -40°C .

Calculate the resistance of the thermistor at -40°C .

The power transfer is $P = U \cdot I$ and $I = \frac{U}{R}$. Therefore, a solution is to increase the resistance of the thermistor. Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \quad \Delta T = T_{\text{end}} - T_{\text{start}}$$
$$R = 10 \text{ k}\Omega \cdot \left(1 + 0.01 \text{ K}^{-1} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \cdot 10^{-6} \text{ K}^{-2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2\right)$$

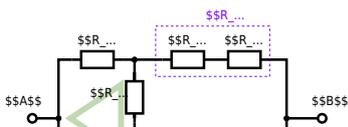
Exercise E3 Pure Resistor Network Simplification
(written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall be solved at once, $R_2 = R_3 = 100 \Omega$ and the switch shall be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution

$$R_{eq} = 133.8 \Omega$$

Now a wye-delta transformation is necessary.



Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:

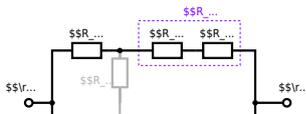
$$R_Y = \frac{R_2 \cdot R_3}{R_2 + R_3} = \frac{100 \cdot 100}{100 + 100} = 50 \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{eq} = R_Y + (R_Y + R_1) \parallel (R_Y + R_2) \parallel (R_Y + R_3) \parallel R_4$$

The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = (100 \sim\Omega + 200 \sim\Omega + 200 \sim\Omega) \parallel (100 \sim\Omega + 100 \sim\Omega) \parallel R_{\text{eq}} = (500 \sim\Omega) \parallel (200 \sim\Omega) \parallel R_{\text{eq}} = \frac{500 \sim\Omega \cdot 200 \sim\Omega}{500 \sim\Omega + 200 \sim\Omega}$$

Exercise E4 Resistance of a Wire by Resistivity
(written test, approx. 6 % of a 60-minute written test, WS2022)

2. The heating element is used to heat the wire with a temperature of $180 \sim\text{C}$. Electric power dissipation (= heat flow) of $P=40 \sim\text{W}$ is necessary. Determine the current I needed to operate it for heating elements. The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \sim\Omega \cdot \text{m}$.

The heating element is $3 \sim\text{m}$ long and has a diameter of $3.57 \sim\text{mm}$.
 Solution: Calculate the resistance R of the heating element.

Solution

$$P = U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \sqrt{\frac{P}{R}} = \sqrt{\frac{40 \sim\text{W}}{0.33 \sim\Omega}}$$

$$R = \rho \cdot \frac{l}{A} \quad | \quad \text{with } A = r^2 \cdot \pi = \frac{1}{4} d^2 \cdot \pi \quad \parallel \quad R = \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad \parallel \quad R = 1.10 \cdot 10^{-6} \sim\Omega \cdot \text{m} \cdot \frac{4 \cdot 3 \sim\text{m}}{(3.57 \cdot 10^{-3} \sim\text{m})^2 \cdot \pi}$$

Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)

2. Heating element made of solid nichrome wire with a temperature coefficient of $1.80 \cdot 10^{-5} \text{ } ^\circ\text{C}^{-1}$. Electric power dissipation (= heat flow) of $P=40 \text{ W}$ is necessary.

Determine the current I needed to operate it.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \text{ } \Omega \cdot \text{m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

∴ Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \\ &= \sqrt{\frac{P}{R}} = \sqrt{\frac{40 \text{ W}}{0.33 \text{ } \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad \text{with } A = r^2 \cdot \pi = \\ &= \frac{1}{4} d^2 \cdot \pi \quad \text{|| } R = \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad \text{|| } R = \\ &= 1.10 \cdot 10^{-6} \text{ } \Omega \cdot \text{m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \end{aligned}$$

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