

Exam Winter Semester 2022

Student Group

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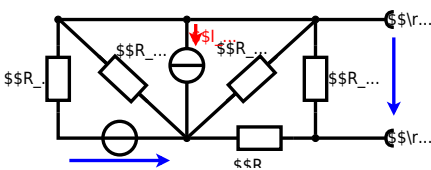
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**Exercise E1 Equivalent linear Source
(written test, approx. 14 % of a 60-minute written test, WS2022)**

The circuit in the following has to be simplified.
Result

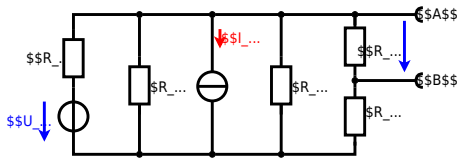
$$\begin{aligned} U_{\text{S}} &= U_{\text{AB}} = 4.5 \text{ V} \\ R_{\text{i}} &= R_{\text{AB}} = 6 \Omega \end{aligned}$$



Calculated the internal resistance R_{i} and the source voltage U_{S} of an equivalent linear voltage source on the connectors A and B .
 $R_1=5.0 \Omega$, $U_2=6.0 \text{ V}$, $R_3= 10 \Omega$, $I_4=4.2 \text{ A}$, $R_5=10 \Omega$, $R_6=7.5 \Omega$, $R_7=15 \Omega$
 Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :
$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4$$
 The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:
$$U_{24} = I_{24} \cdot (R_6 || R_7)$$

$$U_{24} = U_{23} - I_{45} \cdot R_{135} = (U_{23} - I_{45} \cdot R_{135}) \cdot R_{67} / (R_{67} + R_{135})$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_{135}} = (U_{23} - I_{45} \cdot R_{135}) \cdot \frac{R_7}{R_6 + R_7 + R_{135}}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0 \Omega$, so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_{135})$$

with $R_{135} = 5 \Omega \parallel 10 \Omega \parallel 10 \Omega = 5 \Omega \parallel 5 \Omega = 2.5 \Omega$:

$$U_{AB} = \frac{6.0 \text{ V}}{5.0 \Omega} - 4.2 \Omega \cdot \frac{15 \Omega \cdot 2.5 \Omega}{7.5 \Omega + 15 \Omega + 2.5 \Omega} \parallel R_{AB} = 15 \Omega \parallel (7.5 \Omega + 2.5 \Omega)$$

dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022

Exercise E1 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)

2. The diagram shows a circuit with a temperature-dependent resistor R and a constant resistor R_0 . The circuit is connected to a voltage source U_0 . The temperature T inside the refrigeration system can reach down to $-40 \text{ }^\circ\text{C}$. Calculate the resistance of the thermistor at $-40 \text{ }^\circ\text{C}$.

Result: $R = 10 \text{ k}\Omega$ at $25 \text{ }^\circ\text{C}$. Its temperature coefficients are: $\alpha = 0.01 \text{ } \frac{1}{\text{K}}$ and $\beta = 71 \cdot 10^{-6} \text{ } \frac{1}{\text{K}^2}$.

Result: The temperature inside the refrigeration system can reach down to $-40 \text{ }^\circ\text{C}$. Calculate the resistance of the thermistor at $-40 \text{ }^\circ\text{C}$.

Resistor transfer resistor R and R_0 are in series. The power P is given by $P = \frac{U^2}{R}$. Therefore, a solution is to increase the resistance R up the refrigeration system.

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \quad \text{with } \Delta T = T_{\text{end}} - T_{\text{start}}$$

$$R = 10 \text{ k}\Omega \cdot \left(1 + 0.01 \frac{1}{\text{K}} \cdot (-40 \text{ }^\circ\text{C} - 25 \text{ }^\circ\text{C}) + 71 \cdot 10^{-6} \frac{1}{\text{K}^2} \cdot (-40 \text{ }^\circ\text{C} - 25 \text{ }^\circ\text{C})^2 \right)$$

temperature dependent resistance, power, heat, exam ee1 ws2022

Exercise E2 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)

2. Calculate the phasor voltage \underline{U} and the phasor current \underline{I} in the circuit shown in the figure. The components R and X_L shall be given.

After analysis, the following phasors shall be determined and extracted in the form $\underline{U} = U \cdot e^{j(\omega t + \varphi)}$ and $\underline{I} = I \cdot e^{j(\omega t + \varphi)}$.

Solution
.. Calculate the physical values of the components.
Solution $R = 10 \Omega$, $X_L = 20 \Omega$, $X_C = -10 \Omega$

Solution
$$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{10 + j20 - j10} = \frac{50 \angle 0^\circ}{10 + j10} = 4.47 \angle -45^\circ \text{ A}$$

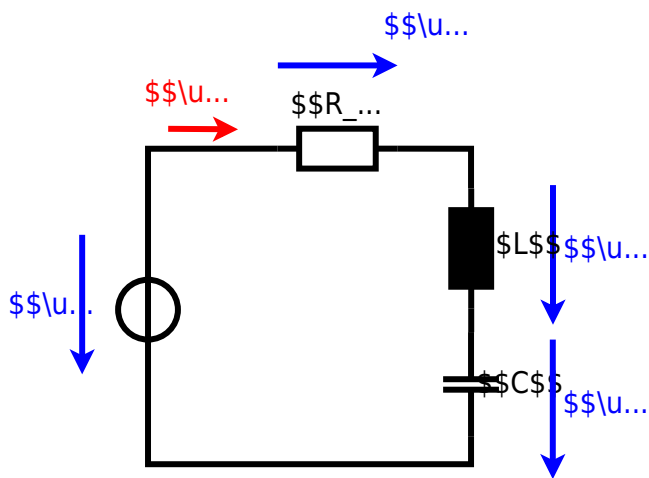
The current and voltage are in phase since the circuit is purely resistive.
The voltage across the capacitor is $\underline{U}_C = \underline{I} \cdot X_C = 4.47 \angle -45^\circ \cdot (-j10) = 44.7 \angle 45^\circ \text{ V}$
The voltage across the inductor is $\underline{U}_L = \underline{I} \cdot X_L = 4.47 \angle -45^\circ \cdot j20 = 89.4 \angle 45^\circ \text{ V}$
The voltage across the resistor is $\underline{U}_R = \underline{I} \cdot R = 4.47 \angle -45^\circ \cdot 10 = 44.7 \angle -45^\circ \text{ V}$
The total voltage is $\underline{U} = \underline{U}_R + \underline{U}_L + \underline{U}_C = 44.7 \angle -45^\circ + 89.4 \angle 45^\circ + 44.7 \angle 45^\circ = 134.1 \angle 45^\circ \text{ V}$
The phase angle φ can be calculated as $\varphi = \arctan\left(\frac{\text{Im}(\underline{U})}{\text{Re}(\underline{U})}\right) = \arctan\left(\frac{96.6}{96.6}\right) = 45^\circ$
With the complex part comes the magnitude $U = 134.1 \text{ V}$
 $\varphi = \arctan\left(\frac{4.47 \cdot 20}{4.47 \cdot 10}\right) = \arctan(2) = 63.4^\circ$
The phase angle φ can be calculated as $\varphi = \arctan\left(\frac{\text{Im}(\underline{I})}{\text{Re}(\underline{I})}\right) = \arctan\left(\frac{-4.47 \cdot \sin(45^\circ)}{4.47 \cdot \cos(45^\circ)}\right) = -45^\circ$

complex impedance, exam ee1 ws2022

Exercise E1 Complex Impedance Circuit (written test, approx. 15 % of a 60-minute written test, WS2022)

2. Calculate the resulting phasor voltage \underline{U} and the phasor current \underline{I} in the circuit shown in the figure. The components R and X_L shall be given. The voltage source $u(t) = 3.0 \cdot \sin(2\pi \cdot 15 \cdot t) \text{ V}$ is connected to a series combination of a resistor of 10Ω and a capacitor of $30 \mu\text{F}$.

Solution
Result
.. Draw the circuit diagram of the given circuit.
Label all components, voltages, and currents.



complex impedance, exam ee1 ws2022

Exercise E3 Impedances at different Frequencies
 (written test, approx. 18 % of a 60-minute written test, WS2022)

A series circuit with a resistor $R_1 = 1.00 \text{ k}\Omega$ and a capacitor $C_1 = 40 \text{ nF}$ is connected to an AC voltage source $U = 50 \text{ V}$ at $f = 4 \text{ MHz}$. The resistor R_1 shall have the same absolute value of the impedance as a capacitor C_2 at $f = 10 \text{ MHz}$. Calculate the value of C_2 .

Solution

$$R_1 = 1.00 \text{ k}\Omega$$

$$R_2 = 10.0 \text{ k}\Omega$$

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by $Z = R + jX_L$

Parallel circuit means that the voltage is the same on R_2 and C_2 . $Z = R_2 + jX_{C2}$

Since $R_1 = R_2$ and $X_L = X_C$ (in absolute value), we have $R_1 = R_2 = 10.0 \text{ k}\Omega$

$$R_1 = R_2 = 10.0 \text{ k}\Omega$$

$$X_L = 2\pi f L = 2\pi \cdot 4 \cdot 10^6 \cdot 4.7 \cdot 10^{-6} = 118.3 \text{ }\Omega$$

$$X_C = \frac{1}{2\pi f C} = \frac{1}{2\pi \cdot 10 \cdot 10^6 \cdot C}$$

Therefore, the resulting current of the parallel circuit is given as:

$$I = \frac{U}{Z} = \frac{50 \text{ V}}{\sqrt{R^2 + X_L^2}} = \frac{50}{\sqrt{10000^2 + 118.3^2}} \approx 5 \text{ mA}$$

Back to the first formula: $R_1 \cdot I = R_2 \cdot I + X_{C2} \cdot I$

$$R_1 = R_2 + X_{C2}$$

$$10.0 \text{ k}\Omega = 10.0 \text{ k}\Omega + X_{C2}$$

$$X_{C2} = 0$$

complex impedance, exam ee1 ws2022

Exercise E4 Resistance of a Wire by Resistivity
 (written test, approx. 6 % of a 60-minute written test, WS2022)

A heating element made of nichrome wire with a diameter of $d = 0.357 \text{ mm}$ and a length of $l = 3 \text{ m}$ is used. The power dissipation ($P = 40 \text{ W}$) is necessary. Calculate the resistance R of the heating element.

Solution

$$R = \frac{U^2}{P} = \frac{230^2}{40} = 1304.5 \text{ }\Omega$$

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \sqrt{\frac{P}{R}} = \sqrt{\frac{40 \text{ W}}{0.33 \text{ } \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad | \quad A = r^2 \cdot \pi \\ \frac{1}{4} d^2 \cdot \pi \quad | \quad R &= \rho \cdot \frac{l}{d^2 \cdot \pi} \quad | \quad R = 1.10 \cdot 10^{-6} \text{ } \Omega \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \end{aligned}$$

resistivity, power, exam ee1 ws2022

Exercise E5 Charging Capacitors
(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (with the initially open switch) is in the position of the circuit shown in the figure. The voltage across the capacitor is again U_c at the moment $t_0 = 0 \text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1 \text{ ms}$ after closing the switch.

Solution
To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

Solution
The ideal voltage source U is in series with the voltage U_c and the resistor R_1 is in parallel with the capacitor. The voltage U_c is independent of this circuit. On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

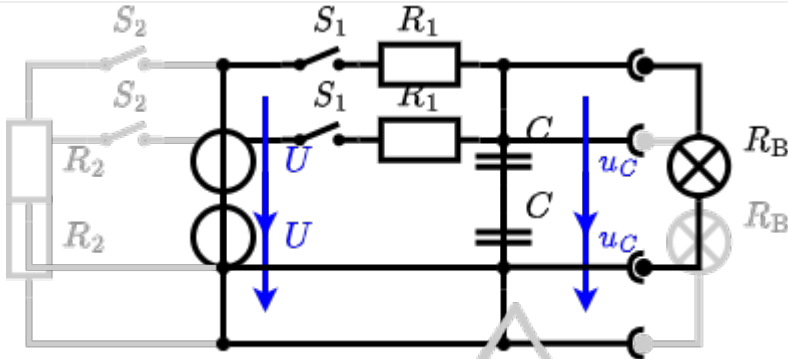


The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ } \Omega$ and a capacitor of $C = 100 \text{ } \mu\text{F}$.

The switch S_2 to an additional consumer R_2 will be considered to be open for the first asks. At the moment $t_0 = 0 \text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0 \text{ V}$.

- .. First do not consider the light bulb - it is not connected to the RC circuit.
- Calculate the point of time t_1 when $u_c(t_1) = 0.5 \cdot U$.

Solution



So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_C(t)$ which has to be $u_C(t_1) = 0.5 \cdot U$:

$$u_C(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5$

$$e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5)$$



An equivalent linear voltage source can be given with U , R_1 , and R_B as seen in yellow.
 Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$
 The internal resistance is given by substituting the ideal voltage source with its resistance ($R_i = 0 \Omega$, short-circuit).
 $R_i = R_1 \parallel R_B = 10 \Omega$

$$u_C(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1 \text{ms}/(10 \Omega \cdot 100 \mu\text{F})})$$

charging capacitors, dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022

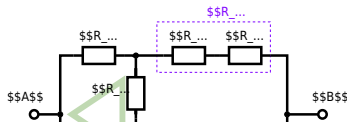
Exercise E6 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall be solved at the $R_1 = 10 \Omega$ and the voltage u_C across the capacitor C shall be determined. $R_2 = 20 \Omega$ and $R_B = 10 \Omega$.

Solution

$$R_{\text{eq}} = 133.8 \, \Omega$$

Now a wye-delta transformation is necessary.



Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:

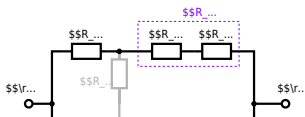
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{\text{eq}} = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega)$$

... The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel R_{\text{eq}} = (500 \, \Omega) \parallel (200 \, \Omega) \parallel R_{\text{eq}} = \frac{500 \, \Omega \cdot 200 \, \Omega}{500 \, \Omega + 200 \, \Omega} \parallel$$

[network simplification, exam ee1 ws2022](#)

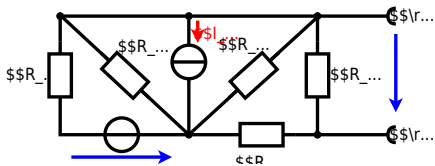
Exercise E3 Equivalent linear Source

(written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.

Result

$$U_{\text{s}} = U_{\text{AB}} = 4.5 \, \text{V} \quad R_{\text{i}} = R_{\text{AB}} = 6 \, \Omega$$



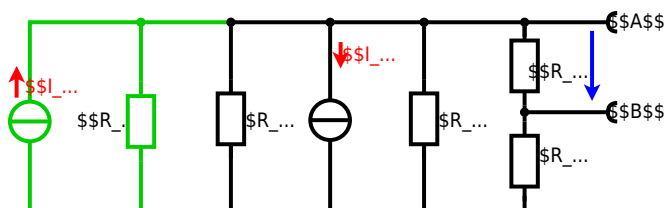
Calculate the internal resistance R_{int} and the source voltage U_{s} of an equivalent linear voltage source on the connectors A and B . $R_1=5.0 \Omega$, $U_2=6.0 \text{ V}$, $R_3=10 \Omega$, $I_4=4.2 \text{ A}$, $R_5=10 \Omega$, $R_6=7.5 \Omega$, $R_7=15 \Omega$. Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :
$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4$$
 The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:
$$U_{24} = I_{24} \cdot (R_6 + R_7)$$

$$U_{AB} = U_{24} \cdot \left(\frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} \right) - I_4 \cdot R_1 || R_3 || R_5$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \left(\frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} \right) - \left(\frac{U_2}{R_1} - I_4 \right) \cdot \left(R_1 || R_3 || R_5 \right)$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0 \Omega$, so a short-circuit):

$$R_{AB} = R_7 || (R_6 + R_1 || R_3 || R_5)$$

with $R_1 || R_3 || R_5 = 5 \Omega || 10 \Omega || 10 \Omega = 5 \Omega || 5 \Omega = 2.5 \Omega$:

$$U_{AB} = \left(\frac{6.0 \text{ V}}{5.0 \Omega} - 4.2 \text{ A} \right) \cdot \left(\frac{15 \Omega \cdot 2.5 \Omega}{7.5 \Omega + 15 \Omega + 2.5 \Omega} \right)$$

$$R_{AB} = 15 \Omega || (7.5 \Omega + 2.5 \Omega)$$

dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022

Exercise E2 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)

2. The diagram shows a circuit with a temperature-sensitive resistor. The resistor has a resistance of $10 \text{ k}\Omega$ at 25°C . Its temperature coefficients are: $\alpha = 0.01 \text{ K}^{-1}$ and $\beta = 71 \cdot 10^{-6} \text{ K}^{-2}$. The temperature inside the refrigeration system can reach down to -40°C . Calculate the resistance of the thermistor at -40°C .

Result: $R = 6.5 \text{ k}\Omega$

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

Therefore, a solution is to use a heat pump up the refrigeration system.

$$R = R_0 \cdot \left(1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2 \right)$$

with $\Delta T = T_{\text{end}} - T_{\text{start}}$

$$R = 10 \text{ k}\Omega \cdot \left(1 + 0.01 \text{ K}^{-1} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \cdot 10^{-6} \text{ K}^{-2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2 \right)$$

temperature dependent resistance, power, heat, exam ee1 ws2022

Exercise E5 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)

2. Calculate the phasor voltage \underline{U} and the phasor current \underline{I} in the circuit shown in the figure. The components R and X_L shall be given.

After analysis, the following phasors can be determined: $\underline{U} = 4.68 \angle -90^\circ \text{ V}$ and $\underline{I} = 0.24 \angle 0^\circ \text{ A}$.
Solution

1. Calculation of the physical values of the components.
Solution $R = 10 \Omega$, $X_L = 20 \Omega$, $X_C = 10 \Omega$

Solution
$$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ \text{ V}}{209 \angle 90^\circ \Omega} = 0.24 \angle -90^\circ \text{ A}$$

The current and voltage are in phase since the circuit is purely resistive.
The voltage across the capacitor is $\underline{U}_C = \underline{I} \cdot X_C = 0.24 \angle -90^\circ \text{ A} \cdot 10 \angle -90^\circ \Omega = 2.4 \angle 0^\circ \text{ V}$
The voltage across the inductor is $\underline{U}_L = \underline{I} \cdot X_L = 0.24 \angle -90^\circ \text{ A} \cdot 20 \angle -90^\circ \Omega = 4.8 \angle 0^\circ \text{ V}$
The voltage across the resistor is $\underline{U}_R = \underline{I} \cdot R = 0.24 \angle -90^\circ \text{ A} \cdot 10 \angle 0^\circ \Omega = 2.4 \angle -90^\circ \text{ V}$
The total voltage is $\underline{U} = \underline{U}_C + \underline{U}_L + \underline{U}_R = 2.4 \angle 0^\circ \text{ V} + 4.8 \angle 0^\circ \text{ V} + 2.4 \angle -90^\circ \text{ V} = 4.68 \angle -90^\circ \text{ V}$
The phase angle φ can be calculated as $\varphi = \arctan\left(\frac{\text{Im}(\underline{U})}{\text{Re}(\underline{U})}\right) = \arctan\left(\frac{-4.68}{0.24}\right) = -90^\circ$
With the complex power $S = \underline{U} \cdot \underline{I}^* = 4.68 \angle -90^\circ \text{ V} \cdot 0.24 \angle 90^\circ \text{ A} = 1.1232 \text{ VA}$
 $P = \text{Re}(S) = 1.1232 \text{ W}$
The phase angle φ can be calculated as $\varphi = \arctan\left(\frac{\text{Im}(S)}{\text{Re}(S)}\right) = \arctan\left(\frac{-0.468}{1.1232}\right) = -22.6^\circ$

complex impedance, exam ee1 ws2022

Exercise E7 Complex Impedance Circuit (written test, approx. 15 % of a 60-minute written test, WS2022)

2. Calculate the resulting phasor voltage \underline{U} and the phasor current \underline{I} in the circuit shown in the figure. The components R and X_L shall be given. The source is $u(t) = 3.0 \sin(2\pi \cdot 15 \cdot t) \text{ V}$.
Solution

This linear source is connected with an inductor of $330 \mu\text{H}$ and a capacitor of $30.22 \mu\text{F}$, all in series.
Result
1. Calculation of the physical values of the components.
Solution $R = 10 \Omega$, $X_L = 3.3 \Omega$, $X_C = 1.66 \Omega$
2. Draw the circuit diagram of the given circuit. Label all components, voltages, and currents.
Solution $\underline{U} = 1.97 \angle 19.8^\circ \text{ V}$, $\underline{I} = 0.198 \angle 19.8^\circ \text{ A}$

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Result
\begin{align*} Z &= \frac{\hat{U}}{\hat{I}} \quad \hat{I} = \frac{\hat{U}}{Z} \\
&\end{align*}
\begin{align*} Z_C &= \frac{1}{2\pi \cdot f \cdot C} \quad \omega = 2\pi \cdot 15 \\
&\text{kHz} \cdot \frac{1}{2\pi \cdot 10^{-8} \text{F}} = 10^8 \text{ Ohm} \\
&\end{align*}
\begin{align*} Z_L &= 2\pi \cdot f \cdot L = 2\pi \cdot 15 \text{ kHz} \cdot \\
&30 \cdot 10^{-6} \text{H} = 2837 \text{ Ohm} \\
&\end{align*}
\begin{align*} Z_C &= \frac{1}{2\pi \cdot f \cdot C} \quad \omega = 2\pi \cdot 15 \\
&\sim \text{kHz} \cdot 330 \sim \mu\text{H}} \\
&\end{align*}
\begin{align*} \underline{Z} &= R + \underline{Z}_L + \underline{Z}_C \quad \underline{Z} = R + j \\
&\cdot \underline{Z}_L - j \cdot \underline{Z}_C \quad \underline{Z} = R + j \cdot (\underline{Z}_L - \underline{Z}_C) \\
&|\underline{Z}| = \sqrt{R^2 + (\underline{Z}_L - \underline{Z}_C)^2} \\
&\end{align*}

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Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \sqrt{\frac{P}{R}} = \sqrt{\frac{40 \text{ W}}{0.33 \text{ } \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad | \quad A = r^2 \cdot \pi \\ \frac{1}{4} d^2 \cdot \pi \quad | \quad R &= \rho \cdot \frac{l}{d^2 \cdot \pi} \quad | \quad R = 1.10 \cdot 10^{-6} \text{ } \Omega \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \end{aligned}$$

resistivity, power, exam ee1 ws2022

Exercise E4 Charging Capacitors
(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (with the real battery) also takes into account the internal resistance r of the battery. The voltage across the capacitor is again $U_c(t_0) = 0 \text{ V}$ at the moment $t_0 = 0 \text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1 \text{ ms}$ after closing the switch.

Solution
Hint: To solve this, first create an equivalent linear voltage source from U , R_1 , and r .

Solution
The ideal voltage source U is in series with the internal resistance r and the resistor R_1 . The voltage across the capacitor is $u_c(t) = U \cdot (1 - e^{-t/\tau})$, where $\tau = (R_1 + r) \cdot C$.
On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

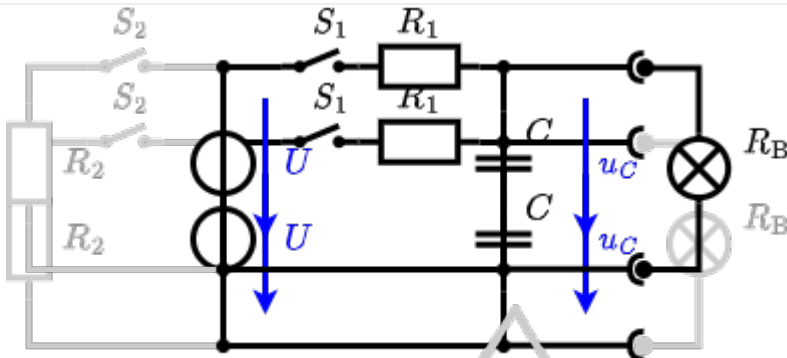


The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ } \Omega$ and a capacitor of $C = 100 \text{ } \mu\text{F}$.

The switch S_2 to an additional consumer R_2 will be considered to be open for the first asks. At the moment $t_0 = 0 \text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0 \text{ V}$.

- 1. First do not consider the light bulb - it is not connected to the RC circuit.
- 2. Calculate the point of time t_1 when $u_c(t_1) = 0.5 \cdot U$.

Solution



So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_C(t)$ which has to be $u_C(t_1) = 0.5 \cdot U$:

$$u_C(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5$

$$e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$$



An equivalent linear voltage source can be given with U , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$
 The internal resistance is given by substituting the ideal voltage source with its resistance ($R_i = 0 \Omega$, short-circuit).
 $R_i = R_1 \parallel R_B = 10 \Omega$

$$u_C(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1 \text{ms} / (10 \Omega \cdot 100 \mu\text{F})})$$

charging capacitors, dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022

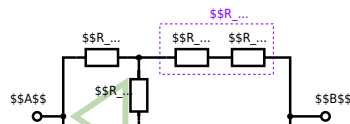
Exercise E3 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall be solved at the $R_1 = 10 \Omega$ and the voltage u_C across R_B .

Solution

$$R_{\text{eq}} = 133.8 \, \Omega$$

Now a wye-delta transformation is necessary.



Since $R_2=R_3$ and based on the equations for the transformation, the transformed R_Y is given as:

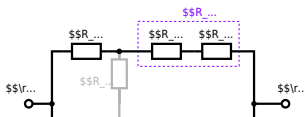
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{\text{eq}} = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega)$$

.. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = (100 \sim \Omega + 200 \sim \Omega + 200 \sim \Omega) \parallel (100 \sim \Omega + 100 \sim \Omega) \parallel R_{\text{eq}} = \{500 \sim \Omega\} \parallel (200 \sim \Omega) \parallel R_{\text{eq}} = \{500 \sim \Omega \cdot 200 \sim \Omega\} \over {500 \sim \Omega + 200 \sim \Omega}$$

network simplification, exam ee1 ws2022

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