

task_pdkggtyexxy1ktu3_with_calculation

Student Group

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complex impedance, exam ee1 WS2022

Exercise E1 Impedances at different Frequencies (written test, approx. 18 % of a 60-minute written test, WS2022)

Exercise E1: A series circuit consists of a resistor R1 = 1.00 Ω, an inductor L = 4.7 μH, and a capacitor C = 40 nF. The circuit is connected to an AC voltage source with a peak-to-peak voltage of 10 V and a frequency of 450 kHz. Calculate the magnitude of the total impedance Z_T and the current I_T through the circuit.

Solution

$$R_1 = 1.00 \Omega$$

$$R_2 = 10.0 \Omega$$

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by

Parallel circuit means that the voltage is the same on R2 and C2

$$\frac{1}{Z_{parallel}} = \frac{1}{R_2} + \frac{1}{X_{C2}}$$

$$Z_{parallel} = \frac{R_2 \cdot X_{C2}}{R_2 + X_{C2}}$$

$$Z_{parallel} = \frac{10 \cdot (-j47)}{10 - j47} = \frac{-j470}{10 - j47}$$

$$Z_{parallel} = \frac{-j470 \cdot (10 + j47)}{(10 - j47)(10 + j47)} = \frac{-j4700 + 22090}{100 + 2209} = \frac{21620 - j4700}{2309}$$

$$Z_{parallel} = 9.36 - j2.03 \Omega$$

Therefore, the resulting current of the parallel circuit is given as:

$$I_{parallel} = \frac{U}{Z_{parallel}} = \frac{10}{9.36 - j2.03} = 1.07 + j0.22 \text{ A}$$

Back to the first formula:

$$Z_T = R_1 + Z_{parallel} = 1.00 + 9.36 - j2.03 = 10.36 - j2.03 \Omega$$

$$|Z_T| = \sqrt{10.36^2 + 2.03^2} = 10.56 \Omega$$

$$I_T = \frac{U}{|Z_T|} = \frac{10}{10.56} = 0.947 \text{ A}$$

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Last update: 2023/03/31 08:02

