

Exam Winter Semester 2022

Student Group

First Name	Surname	Matrikel Nr.

Table of Contents

Exam Winter Semester 2022	2
Additional permitted Aids	2
Hits	2
Tasks	2
Exercise E4 Charging Capacitors (written test, approx. 16 % of a 60-minute written test, WS2022)	2
Exercise E6 Impedances at different Frequencies (written test, approx. 18 % of a 60-minute written test, WS2022)	3
Exercise E5 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)	4
Exercise E7 Complex Impedance Circuit (written test, approx. 15 % of a 60-minute written test, WS2022)	5

Exam Winter Semester 2022

Additional permitted Aids

- non-programmable calculator,
- formulary (4 one-sided DIN A4 pages)

Hits

- The duration of the exam is 120 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.
- Sub-tasks, which are independently solvable are marked with: (independent)
- Sub-tasks, which are hard are marked with: (hard)

Tasks

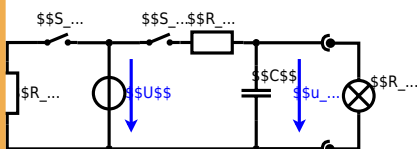
Exercise E4 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (with the realisation) is in the picture. For $t < 0$ the switch S_1 is open and the voltage across the capacitor is again 0 V at the moment $t_0 = 0 \text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1 \text{ ms}$ after closing the switch.

Hint: To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

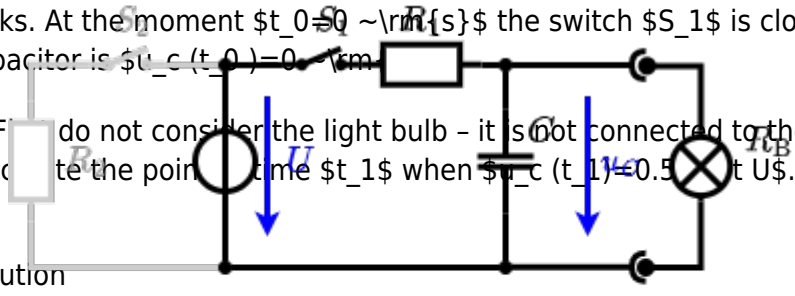
Solution: The internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .



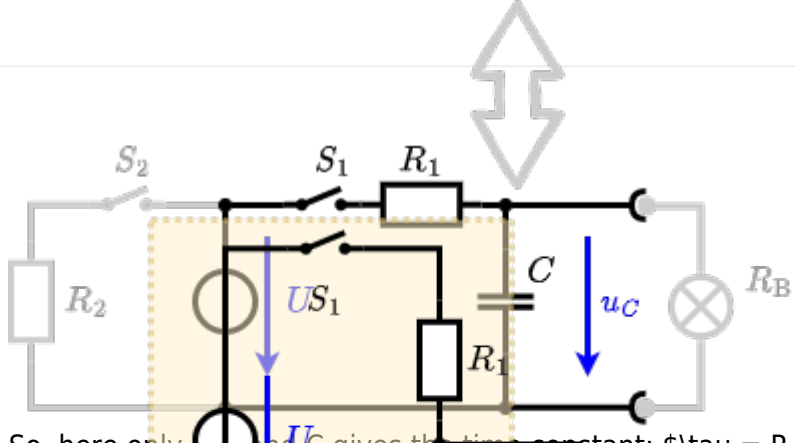
The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ }\Omega$ and a capacitor of $C = 100 \text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first

asks. At the moment $t_0 = 0 \text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0 \text{ V}$.

1. Do not consider the light bulb - it is not connected to the RC circuit. Calculate the point in time t_1 when $u_c(t_1) = 0.5 \cdot U$.



Solution



So, here only U and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_C(t)$ which has to be $u_c(t_1) = 0.5 \cdot U$:
$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to
$$(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5)$$

An equivalent linear voltage source can be given with U , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is:
$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$$
 The internal resistance is given by substituting the ideal voltage source with its resistance ($R_i = 0 \text{ } \Omega$, short-circuit).
$$R_i = R_1 \parallel R_B = 10 \text{ } \Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1 \text{ ms} / (10 \text{ } \Omega \cdot 100 \text{ } \mu\text{F})})$$

Exercise E6 Impedances at different Frequencies
(written test, approx. 18 % of a 60-minute written test, WS2022)

2. A RC circuit with resistor values $R_1 = 1 \text{ } \Omega$, $R_2 = 1 \text{ } \Omega$, $R_3 = 1 \text{ } \Omega$ and a capacitor $C = 1 \text{ } \mu\text{F}$ is shown in the following circuit (of 3S) $U = 1 \text{ V}$.
 Result: $R_B = 2 \text{ } \Omega = 450 \text{ } \Omega$ Hz high frequencies are $f = 50 \text{ } \text{MHz} = 10^8 \text{ } \text{s}^{-1}$ through R_1 and R_3 .
 A resistor R_1 shall have the same absolute value of the impedance as a capacitor $C = 40 \text{ nF}$ at $f_1 = 4 \text{ MHz}$.

Solution

$$R_1 = 1.00 \text{ } \Omega$$

Solution

A series circuit means that the current is constant on every component. Parallel circuit means that the voltage is the same on R_3 and C_3 .

$$\underline{U} = \underline{U}_3 + \underline{U}_C$$

$$\underline{U} = \underline{I} \cdot R_3 + \underline{I} \cdot X_C$$

So it gets clear that perpendicular components can be summed over $\sqrt{}$ (Pythagoras). It is not added, since R_3 is $\sqrt{}$ over ω and X_C is $\sqrt{}$ over ω .

Therefore the resulting current of the parallel circuit is given as:

$$I_3 = \sqrt{I_{R3}^2 + I_{C3}^2}$$

$$I_3 = \sqrt{1^2 + 2^2} = \sqrt{5} \text{ A}$$

This can be rearranged to get R_3 :

$$R_3 = \frac{U}{I_3} = \frac{50 \text{ V}}{\sqrt{5} \text{ A}} = 10\sqrt{5} \text{ } \Omega$$

Back to the first formula:

$$I = \frac{U}{\sqrt{R^2 + X_C^2}}$$

$$I = \frac{50 \text{ V}}{\sqrt{R^2 + \left(\frac{1}{\omega C}\right)^2}}$$

Exercise E5 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)

2. Calculate the phase angle and the effective value of the current $i(t)$ through the components (R and X_L) shall be given.

After analysis, the full dimensional complex impedance has to be extracted and given in phase form $Z = R + jX_L = 10 + j20 \text{ } \Omega$.

Solution

.. Calculation of physical values of the components.

$$R = 10 \text{ } \Omega$$

$$X_L = \omega L = 200 \text{ rad/s} \cdot 0.1 \text{ H} = 20 \text{ } \Omega$$

Solution

$$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \text{ V}}{10 + j20}$$

The current and voltage are in phase since there is only a real part.

resulting $I = \frac{50}{\sqrt{10^2 + 20^2}} = \frac{50}{\sqrt{500}} = \frac{50}{22.36} = 2.24 \text{ A}$

Therefore, the component R is in phase with the voltage and X_L is in phase with R .

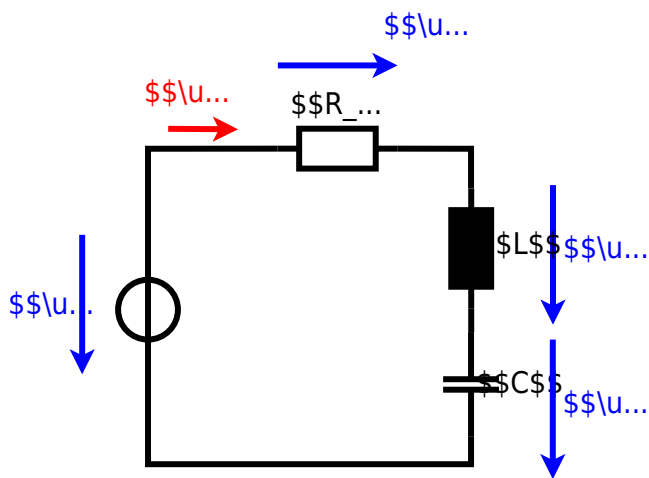
$$\underline{I} = \frac{50 \text{ V}}{10 + j20} = \frac{50}{\sqrt{500}} \cdot \frac{10 - j20}{10 - j20} = \frac{50(10 - j20)}{500} = \frac{500 - j1000}{500} = 1 - j2 \text{ A}$$

The phase angle φ is calculated as:

$$\varphi = \arctan\left(\frac{\text{Im}(\underline{I})}{\text{Re}(\underline{I})}\right) = \arctan\left(\frac{-2}{1}\right) = -63.4^\circ$$

With the complex part comes the complex value:

$$i(t) = 2.24 \cos(\omega t - 63.4^\circ) \text{ A}$$



From:
<https://mexle.te.hs-heilbronn.de/> - **MEXLE Wiki**

Permanent link:
https://mexle.te.hs-heilbronn.de/electrical_engineering_and_electronics_2/ws2022_exam

Last update: **2026/04/03 15:54**

