

# Exam Summer Semester 2021

## Student Group

First Name	Surname	Matrikel Nr.

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# Exam Summer Semester 2021

## Additional permitted Aids

- non-programmable calculator,
- formulary (4 one-sided DIN A4 pages)

## Hits

- The duration of the exam is 120 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.
  
- Sub-tasks, which are independently solvable are marked with: (independent)
- Sub-tasks, which are hard are marked with: (hard)

## Only EEE1-relevant Part

**This part is only for about 65 minutes !**

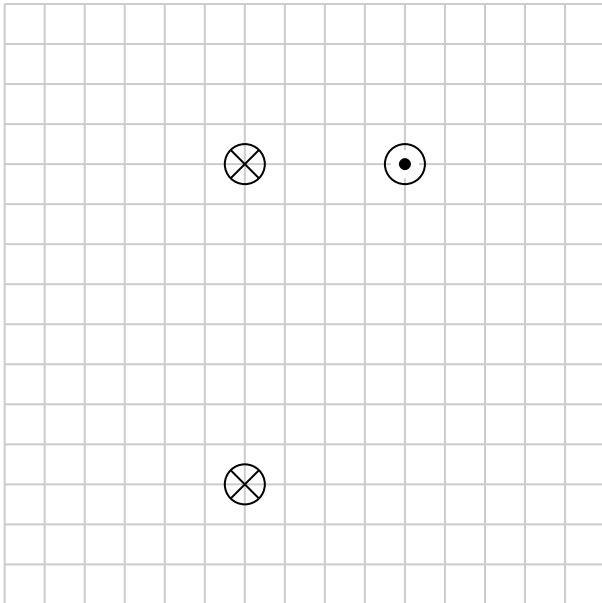
## Exercise E2 Magnetic Field Lines

**(written test, approx. 4 % of a 120-minute written test, SS2021)**

Several parallel conductors are projecting out of the plane.

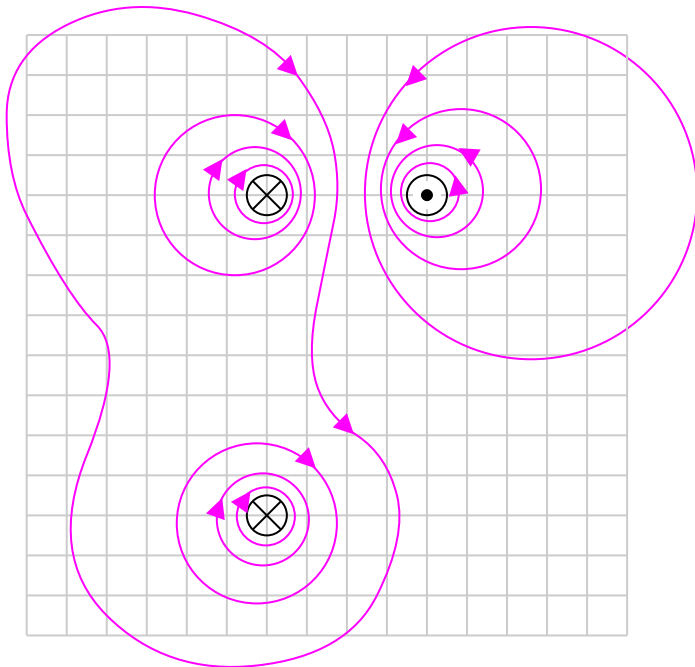
The same current  $I$  flows through all the conductors in different directions (see image below).

Sketch at least 10 field lines of the magnetic field strength  $\vec{H}$  in such a way that the different properties of the field lines (e.g. direction and density) can be seen.



### Result

- high density of field lines near the conductors
- direction of the field lines given by the right-hand rule
- magnetic field has closed field lines
- resulting field given by superposition of field lines



### Exercise E1 Magnetic Flux Density (written test, approx. 6 % of a 120-minute written test, SS2021)

A) The circuit is operated for experiments in the laboratory. A source  $\hat{I} = 100 \text{ A}$  with an amplitude of  $\hat{I} = 100 \text{ A}$  is operated.

How is the distance to the cable about which this value has been calculated? (3 points, independent)

The figure below shows the top view of the laboratory with the supply line between  $\text{A}$  and  $\text{B}$ .

$$B = \mu_0 \mu_r \frac{I}{2\pi r}$$

$$\mu_0 = 4\pi \cdot 10^{-7} \frac{\text{Vs}}{\text{Am}}, \mu_r = 1$$

The formula for the magnetic field strength can be rearranged: 
$$H = \frac{I}{2\pi \cdot r} \quad r = \frac{I}{2\pi \cdot H}$$

Again, the magnetic flux density  $B$  is given as:  $B = \mu_0 \mu_r H$

Therefore: 
$$r = \frac{\mu_0 \mu_r I}{2\pi B} = \frac{4\pi \cdot 10^{-7} \frac{\text{Vs}}{\text{Am}} \cdot \{100 \text{ A}\}}{2\pi \cdot 100 \cdot 10^{-6} \text{ T}}$$

a) What is the highest magnetic flux density through the line in your body? (3 points)

Path

The magnetic field strength for a conducting wire is given as:

$$\begin{aligned} H &= \frac{I}{2\pi \cdot r} \end{aligned}$$

The magnetic flux density  $B$  is given as:  $B = \mu_0 \mu_r H$

Here, the maximum current is  $\hat{I} = 100 \text{ A}$  and the distance to the cable is  $r = \sqrt{(0.1 \text{ m})^2 + (0.4 \text{ m})^2} = 0.412... \text{ m}$ .

$$\begin{aligned} B &= 4\pi \cdot 10^{-7} \frac{\text{Vs}}{\text{Am}} \cdot 1 \\ &\cdot \frac{100 \text{ A}}{2\pi \cdot 0.412... \text{ m}} \end{aligned}$$

### Exercise E2 Toroidal Coil

(written test, approx. 5 % of a 120-minute written test, SS2021)

A magnetic field with a flux density of at least  $50 \text{ mT}$  is to be achieved in a ring-shaped coil (toroidal coil).

The coil has 60 turns, wound around soft iron with  $\mu_r = 1200$ .

The average field line length in the coil should be  $l = 12 \text{ cm}$ .

$$B = 4\pi \cdot 10^{-7} \frac{\text{Vs}}{\text{Am}} \cdot 1200 \cdot \frac{60}{12 \cdot 10^{-2} \text{ m}}$$



What is the minimum current that must flow through a single winding?

Path

The magnetic field strength of a toroidal coil is given as:

$$\begin{aligned} H &= \frac{N \cdot I}{l} \end{aligned}$$

Based on the flux density the magnetic field strength can be derived by  $B = \mu_0 \mu_{\text{r}} \cdot H$ .

By this, the formula can be rearranged:

$$\begin{aligned} H &= \left\{ \frac{N \cdot I}{l} \right\} \parallel \left\{ \frac{B}{\mu_0 \mu_r} \right\} \\ &= \left\{ \frac{N \cdot I}{l} \right\} \parallel \left\{ \frac{B \cdot l}{\mu_0 \mu_r \cdot N} \right\} \end{aligned}$$

Putting in the numbers:

$$I = \frac{0.05 \text{ T} \cdot 0.12 \text{ m}}{4\pi \cdot 10^{-7} \frac{\text{Vs}}{\text{Am}} \cdot 1'200 \cdot 60} \parallel = 0.6631... \frac{\text{T} \cdot \text{m}}{\frac{\text{Vs}}{\text{Am}}}$$

$$= 0.6631... \frac{\text{Vs}}{\text{m}^2} \cdot \text{m} \parallel = 0.6631... \text{ A}$$

**Exercise E4 Cylindrical Coil**  
**(written test, approx. 6 % of a 120-minute written test, SS2021)**

A) the magnetic flux (2 points) information is given:

Result

- Length  $l = 30 \text{ cm}$ ,

Path Winding diameter  $d = 390 \text{ mm}$ ,

- Number of windings  $N = 240$ ,

Current  $I = 500 \text{ mA}$  in the conductor  $I = 500 \text{ mA}$ ,

- Material inside: Air

$\mu_0 = 4\pi \cdot 10^{-7} \frac{\text{Vs}}{\text{Am}}$

The magnetic field strength is  $B = \mu_0 \mu_r \cdot H$ :

The proportion of the magnetic voltage outside the coil can be neglected. Determine the following for the inside of the coil:

$$\begin{aligned} \Phi &= B \cdot A \\ \Phi &= \mu_0 \mu_r \cdot H \cdot A \end{aligned}$$

a) Determine the magnetic field strength  $H$  (2 points)

$$A = \pi r^2 = \pi \left( \frac{d}{2} \right)^2$$

Path

Therefore: 
$$\Phi = B \cdot \pi \left( \frac{d}{2} \right)^2$$

Putting in the numbers:

$$H = \frac{\Phi}{\mu_0 \mu_r \cdot \pi \left( \frac{d}{2} \right)^2} = \frac{0.0005026 \text{ Vs} \cdot \text{m}^2}{4\pi \cdot 10^{-7} \frac{\text{Vs}}{\text{Am}} \cdot \pi \left( \frac{0.39 \text{ m}}{2} \right)^2} \parallel = 0.0006004 \frac{\text{Vs}}{\text{m}}$$

Putting in the numbers:

$$H = \frac{240 \cdot 0.5 \text{ A}}{0.3 \text{ m}}$$

**Exercise E2 effect of induction**  
**(written test, approx. 5 % of a 120-minute written test, SS2021)**

A single conductor loop is penetrated by a changing magnetic flux.

The following figure shows the variation of the flux  $\Phi(t)$  over time.

Calculate the variation of the induced voltage  $u_{\text{ind}}(t)$  over time and draw it in a separate diagram.

\$\$u\_{\text{ind}}(t) = \dots

\$\$\dots

Path

Based on Faraday's Law of Induction the induced voltage is given by: 
$$u_{\text{ind}} = - \frac{d\Phi(t)}{dt}$$

For a linear function, the derivative can be substituted by Deltas ( $d \rightarrow \Delta$ ):

$$u_{\text{ind}} = - \frac{\Delta \Phi(t)}{\Delta t} = - \frac{\Phi(t_{n+1}) - \Phi(t_n)}{t_{n+1} - t_n}$$

For a piece-wise linear function, the induced voltage can be calculated for each interval.

Here, there are 5 different intervals - in the following called  $I$  to  $V$  from left to right:

...

- For the intervals  $I$ ,  $III$ , and  $V$ , the flux  $\Phi(t)$  is constant. Therefore,  $\Delta \Phi(t) = 0$  and  $u_{\text{ind}}(t) = 0$ .

\$\$\dots\$\$

- For the interval  $\Delta t$ :
  - The change in the flux is:  $\Delta \Phi(t) = 1.5 \cdot 10^{-4} \text{ Vs} - 4.5 \cdot 10^{-4} \text{ Vs} = -3.0 \cdot 10^{-4} \text{ Vs}$
  - The time span is:  $0.2 \text{ s}$
  - Conclusively, the induced voltage is:  $u_{\text{ind}}(t) = + \frac{3.0 \cdot 10^{-4} \text{ Vs}}{0.2 \text{ s}} = 1.5 \text{ mV}$

- For the interval  $\text{IV}$ :
  - The change in the flux is:  $\Delta \Phi(t) = 0 \cdot 10^{-4} \text{ Vs} - 1.5 \cdot 10^{-4} \text{ Vs} = -1.5 \cdot 10^{-4} \text{ Vs}$
  - The time span is:  $0.2 \text{ s}$
  - Conclusively, the induced voltage is:  $u_{\text{ind}}(t) = + \frac{1.5 \cdot 10^{-4} \text{ Vs}}{0.2 \text{ s}} = 0.75 \text{ mV}$

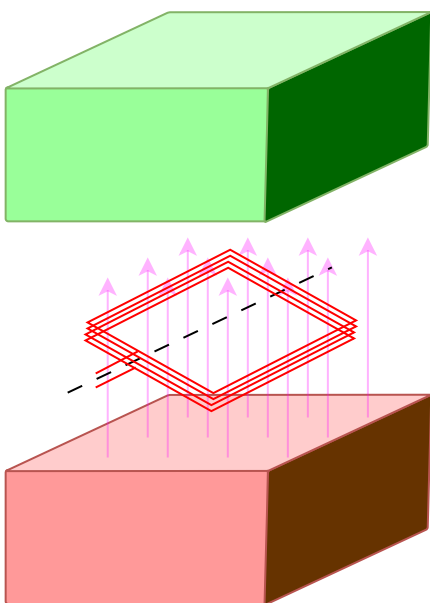
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**Exercise E1 Coil in a magnetic Field**  
**(written test, approx. 4 % of a 120-minute written test, SS2021)**

A coil with  $n = 300$  turns and a cross-sectional area  $A = 600 \text{ cm}^2$  is located in a homogeneous magnetic field.

The rotation of the coil causes a sinusoidal change in the magnetic field in the coil with the frequency  $f = 80 \text{ Hz}$ .

The maximum value of the magnetic flux density in the coil is  $\hat{B} = 2 \cdot 10^{-6} \text{ Vs/cm}^2$ .  
 $\Psi(t) = -181 \text{ V} \cdot \cos(503 \text{ s}^{-1} t)$



Derive the formula for the voltage induced in the coil and calculate the voltage amplitude.

Path

The induced voltage  $u_{\text{ind}}$  is given by:

$$u_{\text{ind}} = - \frac{d\Psi(t)}{dt} = - n \frac{d\Phi(t)}{dt}$$

With  $\Phi(t) = B(t) \cdot A$ , where  $A$  is the constant area of a single winding and  $B(t)$  is the changing field through this winding.

Due to the rotation, the field changes as:

$$B(t) = \hat{B} \cdot \sin(\omega t + \varphi) = \hat{B} \cdot \sin(2\pi f \cdot t + \varphi)$$

$$u_{\text{ind}} = - \frac{d}{dt} (n \cdot A \cdot \hat{B} \cdot \sin(2\pi f \cdot t + \varphi)) = - n \cdot A \cdot \hat{B} \cdot 2\pi f \cdot \cos(2\pi f \cdot t + \varphi)$$

The absolute value of the factor in front of the  $\cos$  is the maximum induced voltage  $\hat{U}_{\text{ind}}$ :

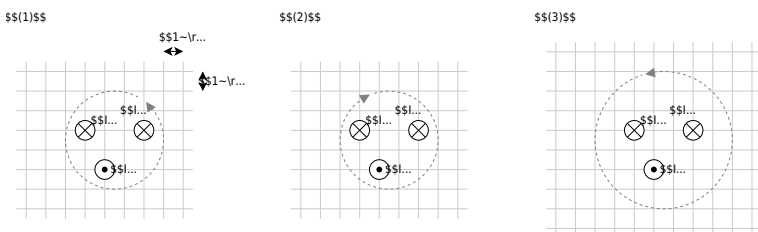
$$\hat{U}_{\text{ind}} = n \cdot A \cdot \hat{B} \cdot 2\pi f = 300 \cdot 0.06 \text{ m}^2 \cdot 2 \cdot 10^{-2} \text{ T} \cdot 2\pi \cdot 80 \text{ s}^{-1} = 180.95... \text{ V}$$

**Exercise E7 Magnetic Voltage**  
**(written test, approx. 6 % of a 120-minute written test, SS2021)**

The following images show cross-sections of electrical cables.  
 Resulted path is shown as a dashed line. The magnetic voltage  $\theta$  on these paths shall be analyzed.

The following values are given for the currents:

- $\theta_{(1)} = -4 \text{ A}$
- $\theta_{(2)} = 0 \text{ A}$
- $I_3 = 1 \text{ A}$
- $I_4 = 4 \text{ A}$



Specify which magnetic voltages  $\theta_{(1)}$ ,  $\theta_{(2)}$ , and  $\theta_{(3)}$  result. Note the direction of the path in each case!

Path

For the resulting current the direction of the path has to be considered with the right-hand rule:

- $I_{(1)} = +I_2 - I_1 - I_3 \quad \rightarrow \quad \theta_{(1)} = 2 \text{ A} - 5 \text{ A} - 1 \text{ A}$
- $I_{(2)} = +I_3 + I_4 - I_1 \quad \rightarrow \quad \theta_{(2)} = 1 \text{ A} + 4 \text{ A} - 5 \text{ A}$
- $I_{(3)} = +I_3 - I_4 - I_2 \quad \rightarrow \quad \theta_{(3)} = 1 \text{ A} - 4 \text{ A} - 2 \text{ A}$

### Exercise E9 Lorentz Force (hard!)

(written test, approx. 10 % of a 120-minute written test, SS2021)

A) ~~300 picture below shows straight high voltage line where the direction is shown as the result. A component of  $F = (1/20) \text{ N}$  of the resulting force is? (Independent)~~

A homogeneous geomagnetic field is assumed. The magnetic field strength has a vertical component of  $B_{\text{v}} = 40 \text{ } \mu\text{T}$  and a horizontal component of  $B_{\text{h}} = 20 \text{ } \mu\text{T}$ .

~~Only 10/100/7/9 is perpendicular to  $\vec{B}_{\text{v}}$  and to  $\vec{B}_{\text{h}}$  and points in the right direction by the right-hand rule.~~

The picture on the right shows the line (black), the field strength components, and the angle in front and top view for illustration purposes.

a) Calculate the force that results from the current flow on the entire conductor.  
 First, calculate the vertical and horizontal components and combine them accordingly.

Path  
Top View

Path

The force on the transmission line can be calculated via the Lorentz force

$$\vec{F} = I \cdot (\vec{l} \times \vec{B})$$

- The horizontal component  $F_h$  of the force is based on the vertical component  $B_v$  of the magnetic field.
- The vertical component  $F_v$  of the force is based on the horizontal component  $B_h$  of the magnetic field.

Here, we have two components for the current and therefore for the force - to evaluate.

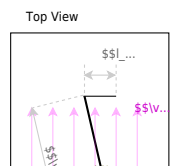
Considering the right-hand rule (and the cross product), the vertical field  $B_v$  generates a horizontal force  $F_h$  and vice versa.

The **horizontal component** is given by



$$\begin{align*}
 F_{\text{h}} &= l \cdot (l \cdot B_{\text{v}}) \cdot 1'200 \cdot 300 \\
 &\cdot 10^3 \cdot 40 \cdot 10^{-6} \cdot \frac{V_s}{m^2} = 14'400 \cdot \frac{V_s}{m} \\
 &= 14'400 \cdot W = 14'400 \cdot N
 \end{align*}$$

For the **vertical component** the angle  $\alpha$  has to be considered.  
 For the maximum  $F_{\text{v}}$  the angle  $\alpha$  has to be  $90^\circ$ , therefore the  $\sin$  has to be used.



$$\begin{align*}
 F_{\text{v}} &= l \cdot l \cdot B_{\text{h}} \cdot \sin \alpha \cdot 1'200 \\
 &\cdot 300 \cdot 10^3 \cdot 40 \cdot 10^{-6} \cdot \frac{V_s}{m^2} \cdot \sin 20^\circ = 2'462.545... \cdot N
 \end{align*}$$

For the **overall force**  $F$  the Pythagorean theorem has to be used:

$$\begin{align*}
 F &= \sqrt{F_{\text{v}}^2 + F_{\text{h}}^2} = \sqrt{(14'400 \cdot N)^2 + (2'462.545... \cdot N)^2} = 14'609.04... \cdot N
 \end{align*}$$

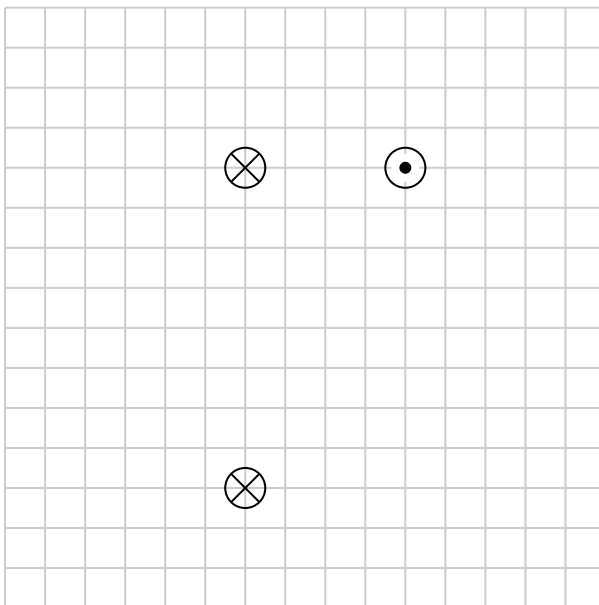
## Full Exam

These is the full exam

Full exam

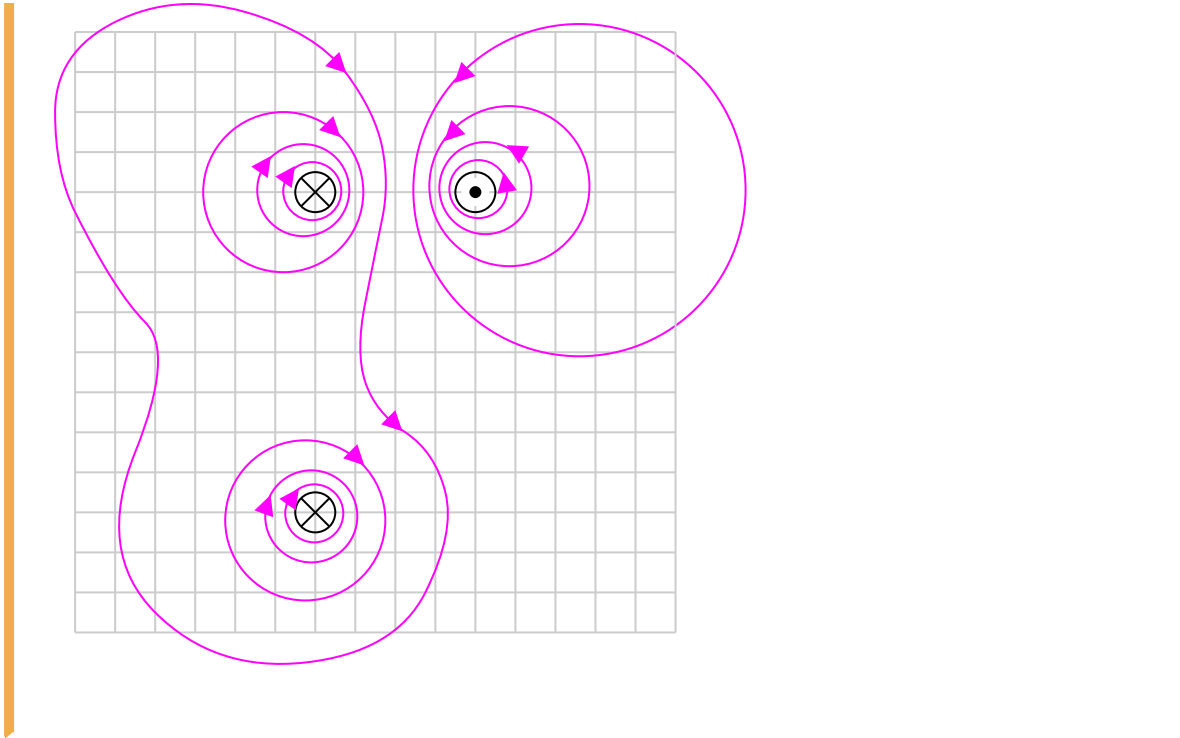
### Exercise E2 Magnetic Field Lines (written test, approx. 4 % of a 120-minute written test, SS2021)

Several parallel conductors are projecting out of the plane.  
The same current  $I$  flows through all the conductors in different directions (see image below).  
Sketch at least 10 field lines of the magnetic field strength  $\vec{H}$  in such a way that the different properties of the field lines (e.g. direction and density) can be seen.



Result

- high density of field lines near the conductors
- direction of the field lines given by the right-hand rule
- magnetic field has closed field lines
- resulting field given by superposition of field lines



electrical\_engineering\_and\_electronics:task\_76ksbc114ylxftfl\_with\_calculation magnetostatic, field lines, exam ee2 ss2021

**Exercise E1 Magnetic Flux Density (written test, approx. 6 % of a 120-minute written test, SS2021)**

A) The electric motor is operated for experiments in the laboratory. A series  $I_0 = 100$  A current is supplied to the motor.

What is the distance  $r$  and the magnetic flux density  $B$  at the center of the motor? (3 points, independent) about. The figure below shows the top view of the laboratory with the supply line between A and B.

Path  $B = 0.12$  m  
 $\mu_0 = 4\pi \cdot 10^{-7} \frac{Vs}{Am}$ ,  $\mu_r = 1$

The formula for the magnetic field strength can be rearranged: 
$$H = \frac{I}{2\pi \cdot r} \quad \parallel \quad r = \frac{I}{2\pi \cdot H}$$

Again, the magnetic flux density  $B$  is given as:  $B = \mu_0 \mu_r H$   
 Therefore: 
$$r = \frac{\mu_0 \mu_r \cdot I}{2\pi \cdot B} \quad \parallel \quad = \frac{4\pi \cdot 10^{-7} \frac{Vs}{Am} \cdot \{100 \sim A\}}{2\pi \cdot \{100 \cdot 10^{-6} \sim T\}}$$

a) What is the highest magnetic flux density through the line in your body? (3 points)

Path

The magnetic field strength for a conducting wire is given as:

$$\begin{aligned} H &= \frac{I}{2\pi \cdot r} \end{aligned}$$

The magnetic flux density  $B$  is given as:  $B = \mu_0 \mu_r H$

Here, the maximum current is  $\hat{I} = 100 \text{ A}$  and the distance to the cable is  $r = \sqrt{(0.1 \text{ m})^2 + (0.4 \text{ m})^2} = 0.412... \text{ m}$ .

$$\begin{aligned} B &= 4\pi \cdot 10^{-7} \frac{\text{Vs}}{\text{Am}} \\ &\cdot 1 \cdot \frac{100 \text{ A}}{2\pi \cdot 0.412... \text{ m}} \end{aligned}$$

electrical\_engineering\_and\_electronics:task\_ti7loik6aurfewkb\_with\_calculation  
magnetostatic, flux density, exam ee2 ss2021

**Exercise E2 Toroidal Coil**  
**(written test, approx. 5 % of a 120-minute written test, SS2021)**

A magnetic field with a flux density of at least  $50 \text{ mT}$  is to be achieved in a ring-shaped coil (toroidal coil).

The coil has 60 turns, wound around soft iron with  $\mu_r = 1200$ .

The average field line length in the coil should be  $l = 12 \text{ cm}$ .

$I = 4 \text{ A}$



What is the minimum current that must flow through a single winding?

Path

The magnetic field strength of a toroidal coil is given as:

$$H = \frac{N \cdot I}{l}$$

Based on the flux density the magnetic field strength can be derived by  $B = \mu_0 \mu_r \cdot H$ .

By this, the formula can be rearranged:

$$H = \frac{N \cdot I}{l} \iff I = \frac{B \cdot l}{\mu_0 \mu_r \cdot N}$$

Putting in the numbers:

$$I = \frac{0.05 \text{ T} \cdot 0.12 \text{ m}}{4\pi \cdot 10^{-7} \frac{\text{Vs}}{\text{Am}} \cdot 1200 \cdot 60} \iff I = 0.6631... \frac{\text{T} \cdot \text{m}}{\frac{\text{Vs}}{\text{m}^2} \cdot \text{m}} \iff I = 0.6631... \text{ A}$$

[electrical\\_engineering\\_and\\_electronics:task\\_w3m7fo4hjzkzgw\\_with\\_calculation\\_magnetostatic, flux density, coil, toroid, exam ee2 ss2021](#)

**Exercise E4 Cylindrical Coil**  
**(written test, approx. 6 % of a 120-minute written test, SS2021)**

A) The magnetic flux (2 points) information is given:

Result

- Length  $l = 30 \text{ cm}$ ,

Path Winding diameter  $d = 390 \text{ mm}$ ,

- Number of windings  $N = 240$ ,
- Current through the inductor  $I = 500 \text{ mA}$ ,
- Material inside: Air

The magnetic field strength is  $B = \mu_0 \mu_r \cdot H$ .

The proportion of the magnetic voltage outside the coil can be neglected. Determine the following for the inside of the coil:

$$\Phi = B \cdot A$$

By putting in the numbers, the magnetic field strength is given by:

$$H = \frac{I \cdot N}{2 \cdot \pi \cdot \left(\frac{d}{2}\right)^2}$$

Path

Therefore:  $\Phi = B \cdot \pi \cdot \left(\frac{d}{2}\right)^2$

```

\end{align*}

Putting in the numbers: \begin{align*} \Phi &= 0.0005026 \over{\rm V} \over{\rm m} \\ & \cdot \pi \left( \frac{0.39 \rm m}{2} \right)^2 \quad \&= 0.00006004... \\ \end{align*}

Putting in the numbers: \begin{align*} H &= \frac{240 \cdot 0.5 \rm A}{0.3 \rm m} \end{align*}

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[electrical\\_engineering\\_and\\_electronics:task\\_0j7accfimmemytq9\\_with\\_calculation\\_magnetostatic, flux density, magnetic field strength, coil, flux, exam ee2 ss2021](#)

**Exercise E2 effect of induction  
(written test, approx. 5 % of a 120-minute written test, SS2021)**

A single conductor loop is penetrated by a changing magnetic flux.  
The following figure shows the variation of the flux  $\Phi(t)$  over time.

Calculate the variation of the induced voltage  $u_{\text{ind}}(t)$  over time and draw it in a separate diagram.

\$\$u\_{\text{ind}}(t)\$\$

\$\$\dots\$\$

Path

```

Based on Faraday's Law of Induction the induced voltage is given by:
\begin{align*} u_{\text{ind}} &= - \frac{d}{dt} \Psi(t) \\ \bigg|_{n=1} &= - \frac{d}{dt} \Phi(t) \end{align*}

```

For a linear function, the derivative can be substituted by Deltas ( $\Delta$ ):

$$u_{\text{ind}} = - \frac{\Delta \Phi(t)}{\Delta t} = - \frac{\Phi(t_{n+1}) - \Phi(t_n)}{t_{n+1} - t_n}$$

For a piece-wise linear function, the induced voltage can be calculated for each interval.

Here, there are 5 different intervals - in the following called  $I$  to  $V$  from left to right:

...

- For the intervals  $I$ ,  $III$ , and  $V$ , the flux  $\Phi(t)$  is constant. Therefore,  $\Delta \Phi(t) = 0$  and  $u_{\text{ind}}(t) = 0$  ( $\sim V$ )

in

- For the interval  $\Delta t$ :
  - The change in the flux is:  $\Delta \Phi(t) = 1.5 \cdot 10^{-4} \text{ Vs} - 4.5 \cdot 10^{-4} \text{ Vs} = -3.0 \cdot 10^{-4} \text{ Vs}$
  - The time span is:  $0.2 \text{ s}$
  - Conclusively, the induced voltage is:  $u_{\text{ind}}(t) = + \frac{3.0 \cdot 10^{-4} \text{ Vs}}{0.2 \text{ s}} = 1.5 \text{ mV}$

- For the interval  $\Delta t$ :
  - The change in the flux is:  $\Delta \Phi(t) = 0 \cdot 10^{-4} \text{ Vs} - 1.5 \cdot 10^{-4} \text{ Vs} = -1.5 \cdot 10^{-4} \text{ Vs}$
  - The time span is:  $0.2 \text{ s}$
  - Conclusively, the induced voltage is:  $u_{\text{ind}}(t) = + \frac{1.5 \cdot 10^{-4} \text{ Vs}}{0.2 \text{ s}} = 0.75 \text{ mV}$

ssL..in\$SL..

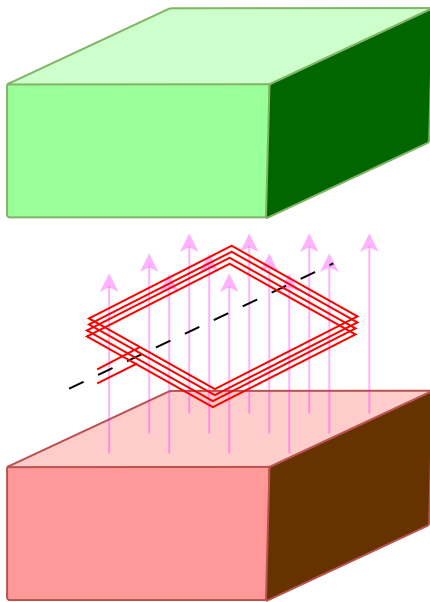
[electrical\\_engineering\\_and\\_electronics:task\\_ludzwiuhjxitz85b\\_with\\_calculation](https://mexle.te.hs-heilbronn.de/)  
induction, flux, induced voltage, exam ee2 ss2021

### Exercise E1 Coil in a magnetic Field (written test, approx. 4 % of a 120-minute written test, SS2021)

A coil with  $n = 300$  turns and a cross-sectional area  $A = 600 \text{ cm}^2$  is located in a homogeneous magnetic field.

The rotation of the coil causes a sinusoidal change in the magnetic field in the coil with the frequency  $f = 80 \text{ Hz}$ .

The maximum value of the magnetic flux density in the coil is  $\hat{B} = 2 \text{ V} \cdot \cos(503 t)$ .



Derive the formula for the voltage induced in the coil and calculate the voltage amplitude.

Path

The induced voltage  $u_{\text{ind}}$  is given by:

$$u_{\text{ind}} = - \frac{d\Phi(t)}{dt} = - n \frac{d\Phi(t)}{dt}$$

With  $\Phi(t) = B(t) \cdot A$ , where  $A$  is the constant area of a single winding and  $B(t)$  is the changing field through this winding.

Due to the rotation, the field changes as:

$$B(t) = \hat{B} \cdot \sin(\omega t + \varphi) = \hat{B} \cdot \sin(2\pi f \cdot t + \varphi)$$

This leads to:  $u_{\text{ind}} = - n \frac{d}{dt} (\hat{B} \cdot \sin(2\pi f \cdot t + \varphi)) = - n \cdot A \cdot \hat{B} \cdot 2\pi f \cdot \cos(2\pi f \cdot t + \varphi)$

$$\cdot \cos(2\pi \cdot f \cdot t + \varphi) \quad \text{\textbackslash\end{align*}}$$

The absolute value of the factor in front of the  $\cos$  is the maximum induced voltage  $\hat{U}_{\text{ind}}$ :

$$\hat{U}_{\text{ind}} = n \cdot A \cdot \hat{B} \cdot 2\pi \cdot f = 300 \cdot 0.06 \text{ m}^2 \cdot 2 \cdot 10^{-2} \text{ Vs/m}^2 \cdot 2\pi \cdot 80 \text{ 1/s} = 180.95... \text{ V}$$

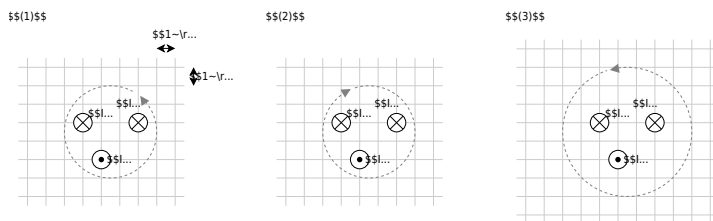
[electrical\\_engineering\\_and\\_electronics:task\\_rdz03rspbwusy7wk\\_with\\_calculation](#)  
[induction, coil, induced voltage, exam ee2 ss2021](#)

**Exercise E7 Magnetic Voltage**  
**(written test, approx. 6 % of a 120-minute written test, SS2021)**

The following images show cross-sections of electrical cables.  
 A dashed path is shown as a dashed line. The magnetic voltage  $\theta$  on these paths shall be analyzed.

The following values are given for the currents:

- $$\theta_{(1)} = -4 \text{ A} \quad \theta_{(2)} = 0 \text{ A}$$
- $$\theta_{(3)} = 5 \text{ A} \quad \theta_{(4)} = 1 \text{ A}$$
- $I_3 = 1 \text{ A}$
  - $I_4 = 4 \text{ A}$



Specify which magnetic voltages  $\theta_{(1)}$ ,  $\theta_{(2)}$ , and  $\theta_{(3)}$  result.

Note the direction of the path in each case!

Path

For the resulting current the direction of the path has to be considered with the right-hand rule:

- $I_{(1)} = +I_2 - I_1 - I_3 \quad \rightarrow \quad \theta_{(1)} = 2 \text{ A} - 5 \text{ A} - 1 \text{ A}$
- $I_{(2)} = +I_3 + I_4 - I_1 \quad \rightarrow \quad \theta_{(2)} = 1 \text{ A} + 4 \text{ A} - 5 \text{ A}$
- $I_{(3)} = +I_3 - I_4 - I_2 \quad \rightarrow \quad \theta_{(3)} = 1 \text{ A} - 4 \text{ A} - 2 \text{ A}$

[electrical\\_engineering\\_and\\_electronics:task\\_jfzlmucghsqvop5\\_with\\_calculation](#)  
 magnetic voltage, exam ee2 ss2021

**Exercise E9 Lorentz Force (hard!)  
(written test, approx. 10 % of a 120-minute written test, SS2021)**

A) ~~300 picture below shows a straight high voltage direct current transmission line with a current of  $I = 2000 \text{ A}$ . The resulting force act? (Independent)~~  
 A homogeneous geomagnetic field is assumed. The magnetic field strength has a vertical component of  $B_{\text{v}} = 40 \text{ } \mu\text{T}$  and a horizontal component of  $B_{\text{h}} = 20 \text{ } \mu\text{T}$ .  
 Only ~~11500~~  $7 \text{ m}$  is perpendicular to  $\vec{B}_{\text{v}}$  and to  $\vec{I}$  and points in the right direction by the right-hand rule.  
 The picture on the right shows the line (black), the field strength components, and the angle in front and top view for illustration purposes.

Top View

Path

a) Calculate the force that results from the current flow on the entire conductor. First, calculate the vertical and horizontal components and combine them accordingly.

Path

- The horizontal component  $\vec{F}_{\text{h}}$  of the force is based on the vertical component  $\vec{B}_{\text{v}}$  of the magnetic field.
- The vertical component  $\vec{B}_{\text{v}}$  of the magnetic field is not shown in the image but is pointing into the ground.
- It has to be perpendicular to  $\vec{B}_{\text{v}}$  and to  $\vec{I}$ . The force on the transmission line can be calculated via the Lorentz force  $\vec{F}_{\text{L}}: \vec{F} = I \cdot (\vec{I} \times \vec{B})$

Here, we have two components for the current - and therefore for the force - to evaluate.

Considering the right-hand rule (and the cross product), the vertical field  $B_{\text{v}}$

$v$  generates a horizontal force  $F_{\text{h}}$  and vice versa.

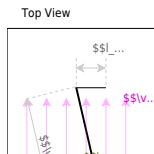
The **horizontal component** is given by



$$\begin{aligned} F_{\text{h}} &= I \cdot (l \cdot B_{\text{v}}) = 1'200 \text{ A} \\ &\cdot 300 \cdot 10^3 \text{ m} \cdot 40 \cdot 10^{-6} \frac{\text{Vs}}{\text{m}^2} \\ &= 14'400 \frac{\text{VA}}{\text{m}} = 14'400 \frac{\text{W}}{\text{m}} = 14'400 \text{ N} \end{aligned}$$

For the **vertical component** the angle  $\alpha$  has to be considered.

For the maximum  $F_{\text{v}}$  the angle  $\alpha$  has to be  $90^\circ$ , therefore the  $\sin$  has to be used.



$$\begin{aligned} F_{\text{v}} &= I \cdot l \cdot B_{\text{h}} \cdot \sin \alpha = 1'200 \text{ A} \\ &\cdot 300 \cdot 10^3 \text{ m} \cdot 40 \cdot 10^{-6} \frac{\text{Vs}}{\text{m}^2} \cdot \sin 20^\circ \\ &= 2'462.545... \text{ N} \end{aligned}$$

For the **overall force**  $F$  the Pythagorean theorem has to be used:

$$\begin{aligned} F &= \sqrt{F_{\text{v}}^2 + F_{\text{h}}^2} = \sqrt{(14'400 \text{ N})^2 + (2'462.545... \text{ N})^2} \\ &= 14'609.04... \text{ N} \end{aligned}$$

[electrical\\_engineering\\_and\\_electronics:task\\_elndbo3xwi2klxuu\\_with\\_calculation](#)  
 lorentz force, exam ee2 ss2021

### Exercise E11 Impedance Characteristics (written test, approx. 6 % of a 120-minute written test, SS2021)

A coil has an inductive reactance of  $X_0 = X(f_0) = 80 \text{ } \Omega$  at a frequency  $f_0 = 60 \text{ kHz}$ .

Calculate the frequencies  $f_1$ ,  $f_2$ ,  $f_3$  at which the following reactances are measured:

- $X_1 = 50 \text{ } \Omega$
- $f_1 = 37.5 \text{ kHz}$
- $X_2 = 121 \text{ } \Omega$
- $f_2 = 90.75 \text{ kHz}$
- $X_3 = 147 \text{ } \Omega$
- $f_3 = 110.25 \text{ kHz}$

Path

There are multiple ways to solve this question.

One way would be, to calculate the inductance  $L$  first by rearranging  $X(f) = 2\pi \cdot f \cdot L$ .

Another way uses ratios (or "rule of three"), since  $X(f) = f \cdot k$  with a constant  $k$ .

Therefore one can set up two formulas  $X_n = f_n \cdot k$ ,  $X_0 = f_0 \cdot k$ , and divide the formulae by each other.

This leads to: 
$$\frac{X_n}{X_0} = \frac{f_n}{f_0} \quad \parallel f_n = \frac{X_n}{X_0} \cdot f_0$$

Putting in the numbers: 
$$f_n = \frac{60 \text{ kHz}}{80 \text{ } \Omega} \cdot X_n = 0.75 \frac{\text{ } \Omega}{\text{kHz}} \cdot X_n$$

[electrical\\_engineering\\_and\\_electronics:task\\_okznhljycuqkbsb\\_with\\_calculation](#)  
 impedance, inductor, exam ee2 ss2021

### Exercise E13 Complex series circuit (written test, approx. 8 % of a 120-minute written test, SS2021)

Results: Determine the absolute value of the resulting impedance of the series circuit using an impedance vector diagram. Pay attention to the correct dimensioning.

a) Determine the complex impedance  $\underline{Z}_C$ .

Result:  $\underline{Z}_C = -j \cdot 804 \text{ } \Omega$

Path:

The complex impedance  $\underline{Z}_C$  is given as 
$$\underline{Z}_C = \frac{1}{j \cdot 2\pi \cdot f \cdot C} = \frac{-j}{2\pi \cdot 40 \cdot 10^3 \text{ Hz} \cdot 4.95 \cdot 10^{-9} \text{ F}} = -j \cdot 803.81... \text{ } \Omega$$

Based on the diagram:  $|\underline{Z}| = 828 \text{ } \Omega$

electrical\_engineering\_and\_electronics:task\_9xy69axg3gi3nr26\_with\_calculation  
 complex voltage divider, exam ee2 ss2021

**Exercise E15 Component Parameters**  
 (written test, approx. 10 % of a 120-minute written test, SS2021)

The diagram shows the circuit diagram of a fan motor. The motor presents a resistive inductive load! The values of the series resistance  $R_M$  and the inductance  $L_M$  are to be determined below. Both result in the impedance of the motor.

This resulted in the recorded current of  $I_M$ . Derive in general the equation for the absolute value of the impedance of the motor.

Path: 
$$|\underline{Z}_M| = \sqrt{R_M^2 + X_L^2} = \sqrt{R_M^2 + (2\pi f L_M)^2}$$

b) Determine the absolute values of the impedances from the specified RMS values at  $f_1$  and  $f_2$  (independent).

This has the advantage that  $R_M$  will cancel out: 
$$|\underline{Z}_2|^2 - |\underline{Z}_1|^2 = (R_M^2 + X_{L2}^2) - (R_M^2 + X_{L1}^2) = X_{L2}^2 - X_{L1}^2 = (2\pi f_2 L_M)^2 - (2\pi f_1 L_M)^2$$

Now we can rearrange to  $L_M^2$ : 
$$L_M^2 = \frac{|\underline{Z}_2|^2 - |\underline{Z}_1|^2}{4\pi^2 (f_2^2 - f_1^2)}$$

The absolute value of the impedance is given as 
$$|\underline{Z}| = \sqrt{R_M^2 + (2\pi f L_M)^2}$$

And then to  $L_M$ :

$$\begin{aligned} L_{\text{M}} &= \frac{1}{2\pi} \sqrt{\frac{Z_2^2 - Z_1^2}{f_2^2 - f_1^2}} \end{aligned}$$

With the values:

$$\begin{aligned} L_{\text{M}} &= \frac{1}{2\pi} \sqrt{\frac{(10 - \Omega)^2 - (6.25 - \Omega)^2}{(100 \frac{1}{s})^2 - (50 \frac{1}{s})^2}} \\ &= 14.346... \text{ mH} \end{aligned}$$

The resistance value  $R_{\text{M}}$  can be derived from  $Z_2^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 \implies R_{\text{M}}^2 = Z_2^2 - (2\pi \cdot f_2 \cdot L_{\text{M}})^2 \implies R_{\text{M}} = \sqrt{Z_2^2 - (2\pi \cdot f_2 \cdot L_{\text{M}})^2}$

The values have to be inserted also for  $R_{\text{M}}$ :  $R_{\text{M}} = \sqrt{(10 - \Omega)^2 - (2\pi \cdot 100 \frac{1}{s} \cdot 0.014346... \text{ mH})^2} = 4.3301... - \Omega$

[electrical\\_engineering\\_and\\_electronics:task\\_wjttvmydrskzhcim\\_with\\_calculation\\_complex\\_voltage\\_divider, rms, inductor, exam ee2 ss2021](#)

**Exercise E1 Signal Analysis (written test, approx. 6 % of a 120-minute written test, SS2021)**

A) Determine the frequency of a signal  $i(t)$  and the amplitude  $\hat{I}$  and the RMS value  $I_{\text{RMS}}$  of the current  $i(t)$  if the voltage  $u(t)$  and the current  $i(t)$  are available in the consumer arrow system. (hard)

- $u(t) = 50 \text{ V} \cdot \cos(6000 \frac{1}{s} \cdot t + 4)$
- $i(t) = 30 \text{ A} \cdot \sin(6000 \frac{1}{s} \cdot t + 5)$

Result

a) Determine the amplitude values  $\hat{U}$ ,  $\hat{I}$  and the RMS values  $U$ ,  $I$

- $f = 955 \text{ Hz}$
- $\hat{U} = 50 \text{ V}$
- $\hat{I} = 30 \text{ A}$

The phase shift can be determined by the time difference  $\Delta t$  between the zero-crossings of the voltage and current.  $\Delta t = 5 \mu\text{s} - 4 \mu\text{s} = 1 \mu\text{s}$ .  $\varphi = 2\pi \cdot f \cdot \Delta t = 2\pi \cdot 955 \text{ Hz} \cdot 1 \mu\text{s} = 6.000 \text{ rad}$ .  $f = 954.93... \text{ Hz}$

$U = 35.4 \text{ V}$

The amplitude values  $\hat{U}$ ,  $\hat{I}$  are given directly by the coefficient of the cosine and sine functions. For the phase  $\varphi$  we have to subtract  $\varphi_i$  from  $\varphi_u$ . But to get these values, both the  $u(t)$  and  $i(t)$  need to have the same sinusoidal function! Therefore:

- For the RMS values of sinusoidal functions the amplitudes have to be multiplied with  $\frac{1}{\sqrt{2}}$

- $\varphi_i = 5$
- $\varphi_u = 4 + \frac{\pi}{2}$

By this we get for  $\varphi$   $\varphi = \varphi_u - \varphi_i = 4 + \frac{\pi}{2} - 5 = 2.14159... \text{ rad}$

Converted in degree:  $\varphi = 2.14159... \cdot \frac{180}{\pi}$

$$\left\{ \frac{360^\circ}{2\pi} \right\} \quad \&= \quad 32.7042...^\circ \quad \end{align*}$$

electrical\_engineering\_and\_electronics:task\_abh4vhlgczdbni37\_with\_calculation  
 signal analysis, rms, exam ee2 ss2021

**Exercise E18 Resonant Circuit**  
**(written test, approx. 4 % of a 120-minute written test, SS2021)**

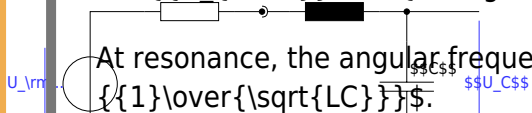
Given a resonant RLC circuit that is fed by a sine wave of the voltage  $u_{\text{rms}} = 12 \cdot \sin(2\pi \cdot f_0 \cdot t)$  V (independent of  $\omega$ ). The inductance  $L$  and capacitance  $C$  are fixed. The resistance  $R$  can be varied.

Path:  $u_{\text{rms}} = 12 \cdot \sin(2\pi \cdot f_0 \cdot t)$  V  
 $R = 20 \cdot 10^{-3} \Omega$   
 •  $L = 20 \text{ mH}$   
 •  $C = 30 \mu\text{F}$   
 For the following calculation, the internal resistance  $R_i$  and the resistance  $R$  have to be combined:  $R_\Sigma = R_i + R$

Here, either one knows that the gain factor  $Q$  stands for  $Q = \frac{U_C}{U_{\text{rms}}}$  and therefore can directly use the following formula:  $Q = \frac{U_C}{U_{\text{rms}}} = \frac{1}{R_\Sigma} \sqrt{\frac{L}{C}}$

When the gain factor is not known, one has to derive it:  
 The voltage  $U$  at resonance is only given by the total ohmic resistance  $R_\Sigma$  and the source voltage  $U_{\text{rms}}$ :  $I = \frac{U_{\text{rms}}}{R_\Sigma}$

This current flow also through the impedance of the capacitor  
 $U_C = Z_C \cdot I = \frac{1}{\omega C} \cdot I = \frac{U_{\text{rms}}}{\omega C R_\Sigma}$



At resonance, the angular frequency  $\omega$  is given by  $\omega = \frac{1}{\sqrt{LC}}$ .  
 $U_C = \frac{U_{\text{rms}}}{\frac{1}{\sqrt{LC}} R_\Sigma} = \frac{U_{\text{rms}} \sqrt{LC}}{R_\Sigma}$

In both cases, we end up with the same formula, where we have to insert the physical values:  $R_\Sigma = R = 20 \cdot 10^{-3} \Omega$   
 $\omega = \frac{1}{\sqrt{4 \cdot 10^{-2} \cdot 30 \cdot 10^{-6}}} = \frac{1}{\sqrt{1200 \cdot 10^{-8}}} = \frac{1}{\sqrt{12 \cdot 10^{-6}}} = \frac{1}{\sqrt{12}} \cdot 10^3 \text{ rad/s} = 6.4549 \cdot 10^2 \text{ rad/s}$

With the values  $R = 20 \text{ }\Omega$ ,  $X_L = 10 \text{ }\Omega$ ,  $X_C = 10 \text{ }\Omega$ ,  $U_{\text{RMS}} = 110 \text{ V}$ ,  $I_{\text{RMS}} = 5 \text{ A}$ ,  $\varphi = 25^\circ$ , the active power  $P$  is given by  $P = U_{\text{RMS}} \cdot I_{\text{RMS}} \cdot \cos(\varphi) = 110 \text{ V} \cdot 5 \text{ A} \cdot \cos(25^\circ) = 488 \text{ W}$ .

electrical\_engineering\_and\_electronics:task\_nyniewamxfshpuwt\_with\_calculation  
 resonance, resonant circuit, rms, exam ee2 ss2021

**Exercise E20 Multiphase systems**  
**(written test, approx. 4 % of a 120-minute written test, SS2021)**

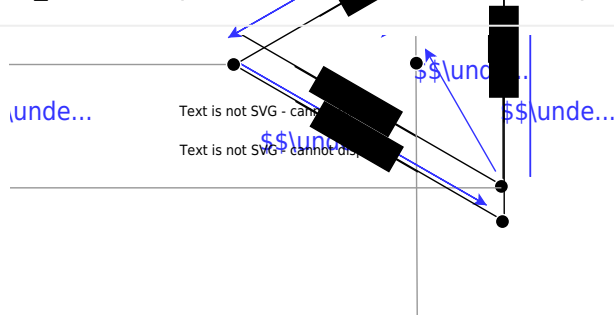
a) Specify the RMS value of the phase current  $I_{\text{RMS}}$  and the active power  $P$  in the  $\Delta$ -winding.

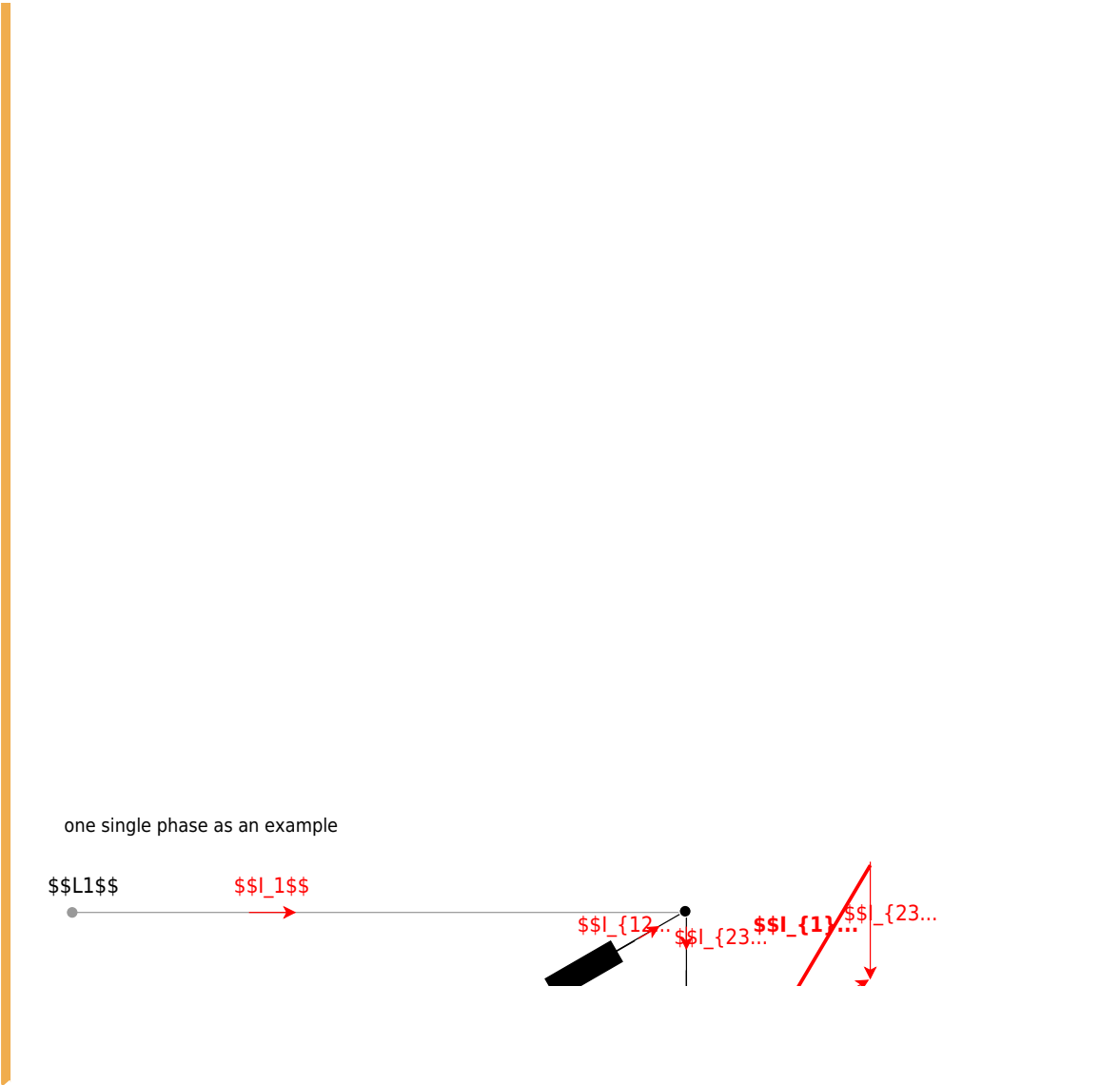
A voltage with the RMS value  $U_{\text{RMS}} = 110 \text{ V}$  is applied between the terminals of each winding.

Through each of the windings, there is a current with an RMS value  $I_{\text{RMS}} = 5 \text{ A}$  and a phase angle  $\varphi = +25^\circ$  compared to the voltage.

a) Draw the circuit diagram. The active power  $P$  is given by  $P = U_{\text{RMS}} \cdot I_{\text{RMS}} \cdot \cos(\varphi)$ . Since  $U_{\text{RMS}} = 110 \text{ V}$ ,  $I_{\text{RMS}} = 5 \text{ A}$ , and  $\varphi = 25^\circ$ , the active power  $P$  is  $P = 110 \text{ V} \cdot 5 \text{ A} \cdot \cos(25^\circ) = 488 \text{ W}$ .

Since the line current  $I_{\text{L}}$  is equal to the string  $I_{\text{L}} = \sqrt{3} \cdot I_{\text{RMS}} = \sqrt{3} \cdot 5 \text{ A}$  (see the example in the image below), one can see, that  $I_{\text{L}} = \sqrt{3} \cdot I_{\text{RMS}} = \sqrt{3} \cdot 5 \text{ A}$ .





[electrical\\_engineering\\_and\\_electronics:task\\_ezrkjzifcegttccp\\_with\\_calculation](#)  
multiphase systems, rms, power, exam ee2 ss2021

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