

task_wjttvmydrskzhcim_with_calculation

Student Group

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Table of Contents

Exercise E15 Component Parameters (written test, approx. 10 % of a 120-minute written test, SS2021)	2
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complex voltage divider, RMS, inductor, exam ee2 SS2021

Exercise E15 Component Parameters**(written test, approx. 10 % of a 120-minute written test, SS2021)**

Determine the component parameters of a motor (motor presents a resistive inductive load) for the next exercises consider the following:
 The RMS values of the series resistance R_{M} and the inductance L_{M} are to be determined below. Both results in the impedance of the motor.
 But two different frequencies, f_1 and f_2 was applied.

This resulted in the recorded current of

a) Derive in general the equation for the absolute value of the impedance of the motor.

$$|Z| = \sqrt{(2\pi \cdot f \cdot L_{\text{M}})^2 + R_{\text{M}}^2}$$

$$R_{\text{M}} = \frac{U_{\text{RMS}}}{I_{\text{RMS}}}$$

$$L_{\text{M}} = \frac{U_{\text{RMS}}}{I_{\text{RMS}} \cdot 2\pi \cdot f}$$

b) Since we have the absolute values of the impedances from the specified formulas from a) and this has the advantage that R_{M} will cancel out:

$$Z_2^2 - Z_1^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 - \left((2\pi \cdot f_1 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 \right)$$

The complex impedance \underline{Z} for a resistive inductive load R_{M} and L_{M} in series circuit is given as

$$\underline{Z} = R_{\text{M}} + j\omega L_{\text{M}}$$

$$|Z| = \sqrt{R_{\text{M}}^2 + (\omega L_{\text{M}})^2}$$

Now we can rearrange to L_{M} :

The Pythagorean theorem can derive the absolute value:

$$Z_2^2 - Z_1^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 - \left((2\pi \cdot f_1 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 \right)$$

$$Z_2^2 - Z_1^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 - (2\pi \cdot f_1 \cdot L_{\text{M}})^2$$

$$Z_2^2 - Z_1^2 = (2\pi \cdot L_{\text{M}})^2 (f_2^2 - f_1^2)$$

$$L_{\text{M}} = \frac{Z_2^2 - Z_1^2}{(2\pi)^2 (f_2^2 - f_1^2)}$$

$$L_{\text{M}} = \frac{50^2 - 40^2}{(2\pi)^2 (100^2 - 50^2)} = 14.346 \text{ mH}$$

And then to R_{M} :

$$L_{\text{M}} = \frac{1}{2\pi} \sqrt{\frac{Z_2^2 - Z_1^2}{f_2^2 - f_1^2}}$$

With the values:

$$L_{\text{M}} = \frac{1}{2\pi} \sqrt{\frac{(10 \cdot \Omega)^2 - (6.25 \cdot \Omega)^2}{(100 \text{ s}^{-1})^2 - (50 \text{ s}^{-1})^2}} = 14.346 \text{ mH}$$

The resistance value R_{M} can be derived from

$$Z_2^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 \implies R_{\text{M}}^2 = Z_2^2 - (2\pi \cdot f_2 \cdot L_{\text{M}})^2$$

$$R_{\text{M}} = \sqrt{Z_2^2 - (2\pi \cdot f_2 \cdot L_{\text{M}})^2}$$

The values have to be inserted also for R_{M} :

$$R_{\text{M}} = \sqrt{(10 \text{ V})^2 - (2\pi \cdot 100 \text{ s}^{-1} \cdot 0.014346 \text{ H})^2} = 4.3301 \text{ } \Omega$$

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